

# Renormalon subtraction and precision QCD

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Research Goal : Precision QCD prediction using pert. QCD

→ helps precision physics  
(ILC, HL-LHC,⋯)

🔑 OPE : factorization of **UV(pert.)** and **IR(non-pert.)** contributions of observable

Observable  $A = \sum_i C_i(\alpha_s) \langle \mathcal{O}_i \rangle$  → The most use of **pert.** QCD calculation

💀 Renormalon problem :  $C_i$  has inevitable ambiguity  $\delta C_i$  (**pert.** is affected by **non-pert.**)  
→ Pert. QCD is useless??

Our strategy : Renormalon subtraction in the framework of OPE

RF : Renormalon Free

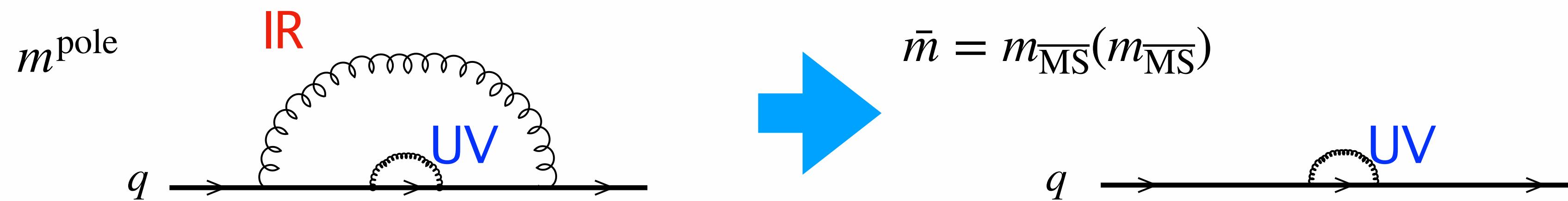
$$\left. \begin{aligned} A &= C_0 + C_1 \langle \mathcal{O}_1 \rangle + \dots \\ C_0 &= C_0^{\text{RF}} + \delta C_0 \end{aligned} \right\} \xrightarrow{\text{absorb } \delta C_0 \text{ into } \langle \mathcal{O}_1 \rangle} A = C_0^{\text{RF}} + C_1 \langle \mathcal{O}_1 \rangle^{\text{RF}} + \dots$$

: precise prediction

## Recent status of my research

- ◆ Renormalon subtraction of  $m_{\text{pole}}(\bar{m})$  in large- $\beta_0$  approx.

YH, Sumino (2019)



- ◆ Formulation of generalized renormalon subtraction method

YH's master thesis (2020)

Applicable to a wide class of observables

**NEW**

- ◆ Application of generalized renormalon subtraction method

YH, Sumino, Takaura (in prep.)

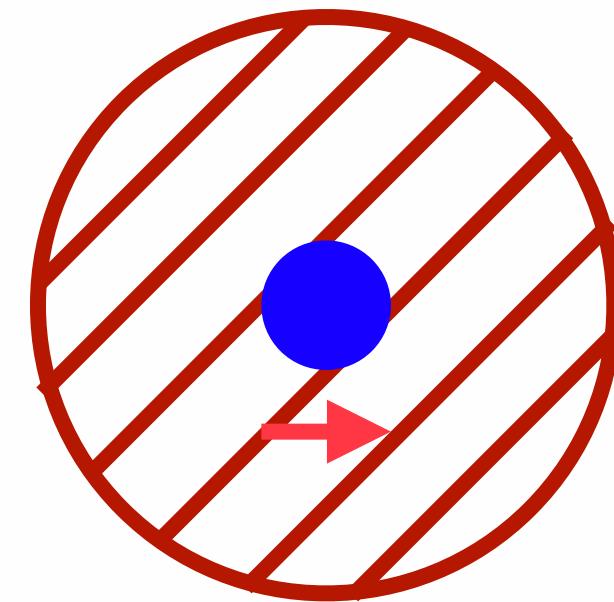
Observables : Adler function, B (D) meson mass, Decay width of B meson

## Application : B (D) meson mass $M_H$ ( $H = B, D$ )

OPE of  $M_H$  :  $M_H = m_{\text{pole}}^{\text{PT}}(\bar{m}) + \bar{\Lambda} + \frac{\mu_\pi^2}{2m_{\text{pole}}} + \dots$   
 (HQET)

$$\begin{aligned} & \text{renormalons} \quad \downarrow \\ &= m_{\text{pole}}^{\text{RF}}(\bar{m}) + \delta m_1 + \frac{\delta m_2}{\bar{m}} + \bar{\Lambda} + \frac{\mu_\pi^2}{2m_{\text{pole}}^{\text{RF}}} + \dots \\ & \quad \quad \quad \text{absorb} \quad \quad \quad \uparrow \\ &= m_{\text{pole}}^{\text{RF}}(\bar{m}) + \bar{\Lambda}^{\text{RF}} + \frac{\mu_\pi^{2,\text{RF}}}{2m_{\text{pole}}^{\text{RF}}} + \dots \end{aligned}$$

$H = B, D$



$\bar{\Lambda}$  : light degrees of freedom of meson  
 $\sim \mathcal{O}(\Lambda_{\text{QCD}})$

$\mu_\pi^2$  : kinetic energy of b quark  
 $\sim \mathcal{O}(\Lambda_{\text{QCD}}^2)$

$m_{\text{pole}}^{\text{RF}}(\bar{m})$  : convergent series

$\bar{\Lambda}^{\text{RF}}, \mu_\pi^{2,\text{RF}}$  : less ambiguous prediction

**5-loop calculation achieve the NEXT precision of flavor physics**

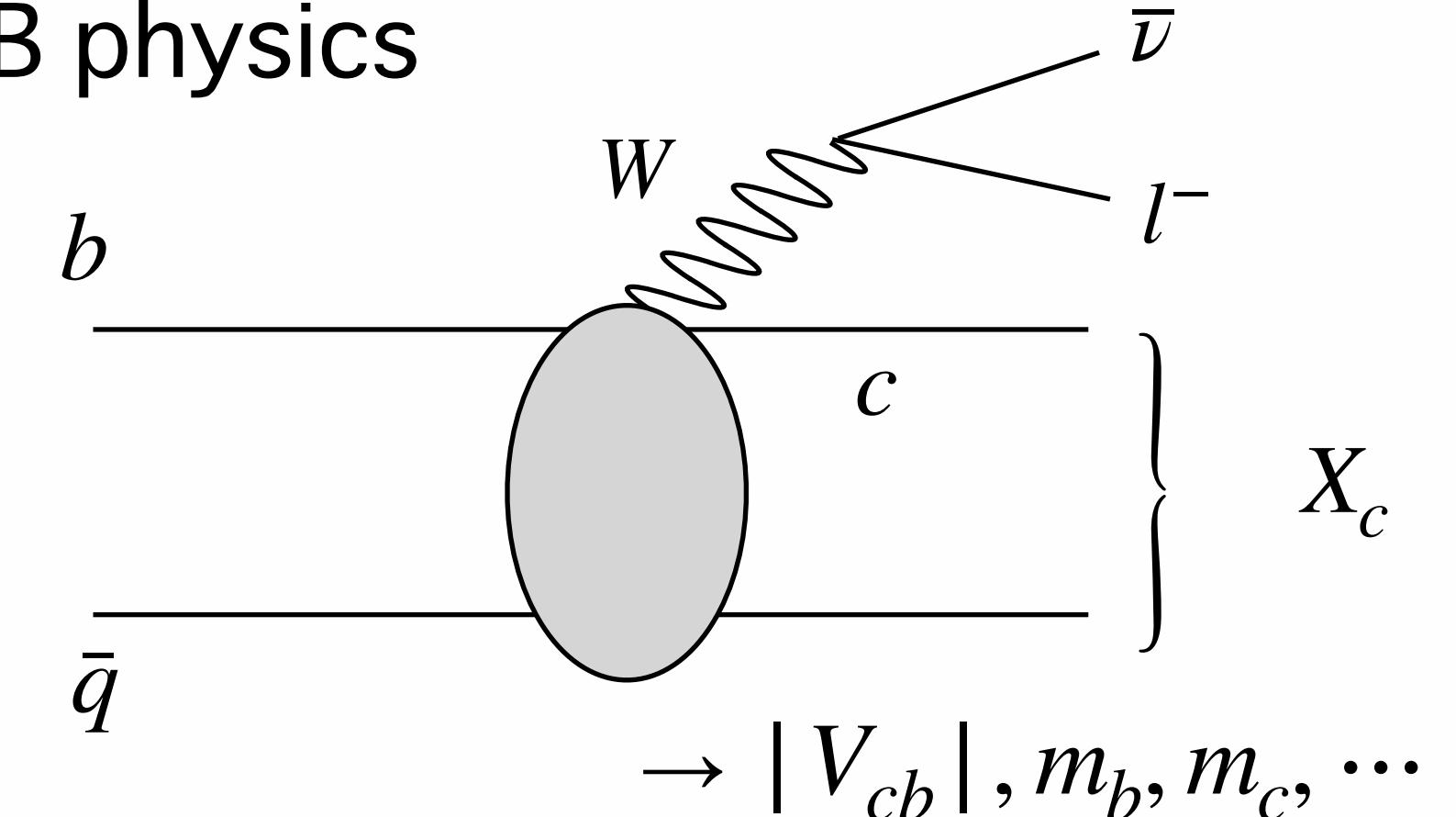
## Research plan during GPPU curriculum

- ◆ Renormalon subtraction method
  - : consistency checks, examinations
- ◆ Precise determination of fundamental parameters
  - :  $|V_{cb}|, m_b, m_c$ , non-pert. matrix elements

## Overseas Training (online)

- ◆ 2,3-loop calculation of  $q\bar{q} \rightarrow \gamma$  (done for 30 days)  
*Supervised by M. Steinhauser (KIT)*
- ◆ Practice of 4-loop calculation (future training plan)

e.g. B physics



: could be useful for ILC physics

## Award and Grant

- ◆ 東北大学物理学専攻賞
- ◆ 学振DC2 (2021/4~)