

2014/9/25 熱川

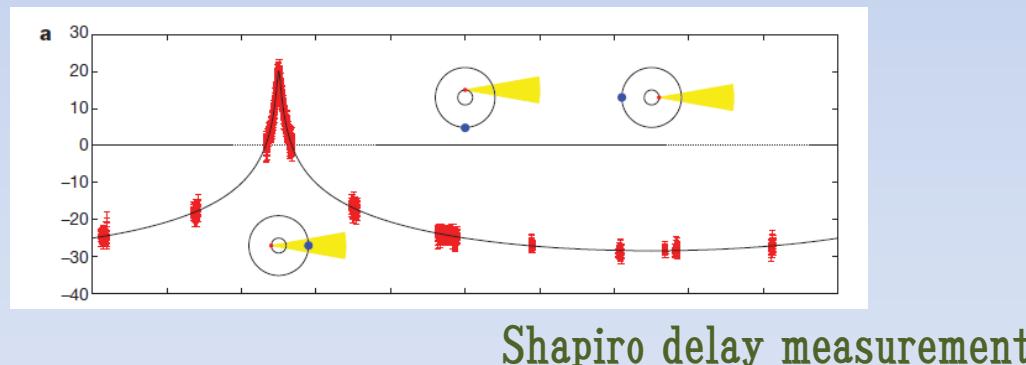
ハイペロンパズルとユニバーサル3体斥力

Y. Yamamoto

Collaborators:

T. Furumoto
N. Yasutake
Th.A. Rijken

2010 PSR J1614-2230 $(1.97 \pm 0.04) M_{\odot}$



Shapiro delay measurement

2013 PSR J0348-0432 $(2.01 \pm 0.04) M_{\odot}$

RMF



Lagrangian in Baryon-Meson system

MF近似

Many parameters

相互作用模型
2体力 + 3体力

NN・YN散乱
多体现象

Almost no parameter

Nuclear saturation properties
EOS in neutron-star matter

核力から核構造

核力は自然認識における重要な結節点である

RMFでHyperon Puzzle は解ける？

$2M_{\text{solar}}$ とconsistentなparameter setがあるというだけでパズルが解けたと言えるか？

Our strategy for neutron stars

Neutron-star EOS derived from
Baryon-Baryon interaction model
in relation to Earth-based experiments

without ad hoc parameter for stiffness of EOS

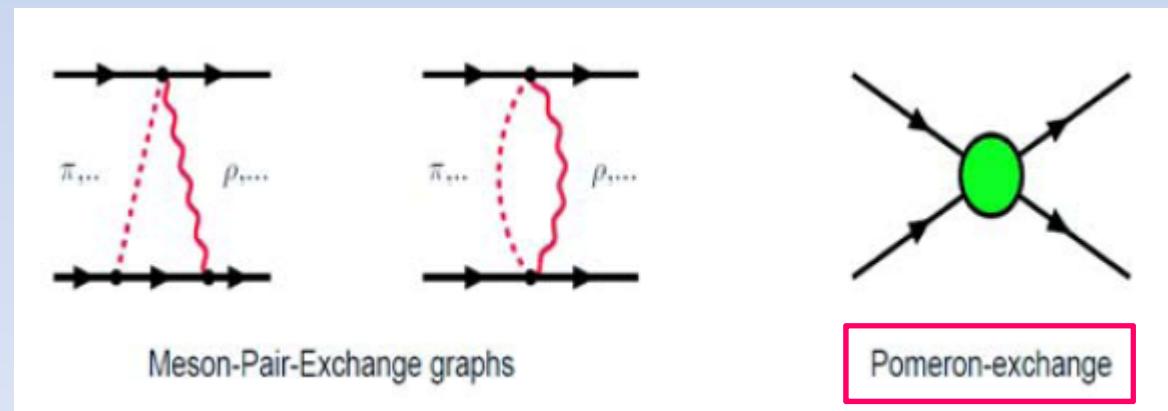
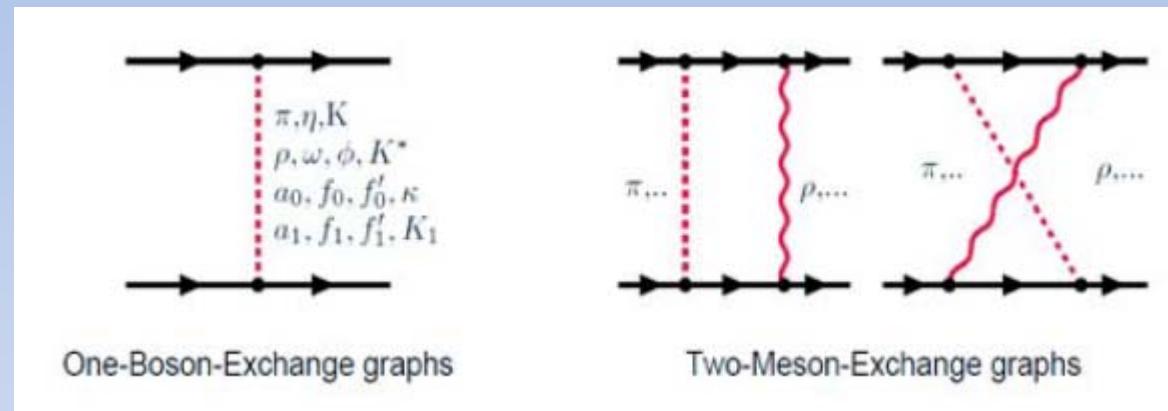
on the basis of G-matrix theory

Our story of neutron-star matter
starts from some interaction model

We adopt here Nijmegen ESC model

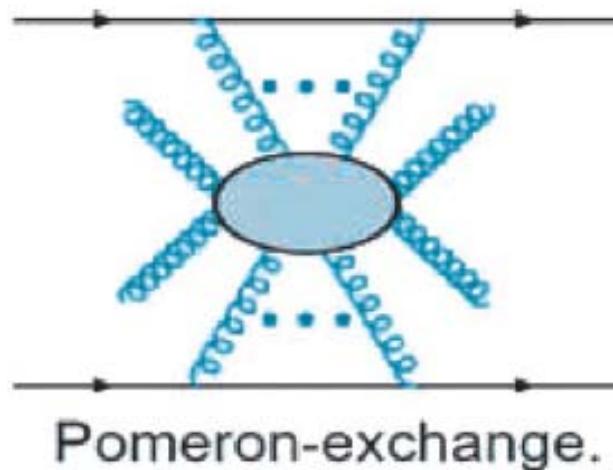
Extended Soft-Core Model (ESC)

- Two-meson exchange processes are treated explicitly
- Meson-Baryon coupling constants are taken consistently with Quark-Pair Creation model



repulsive cores

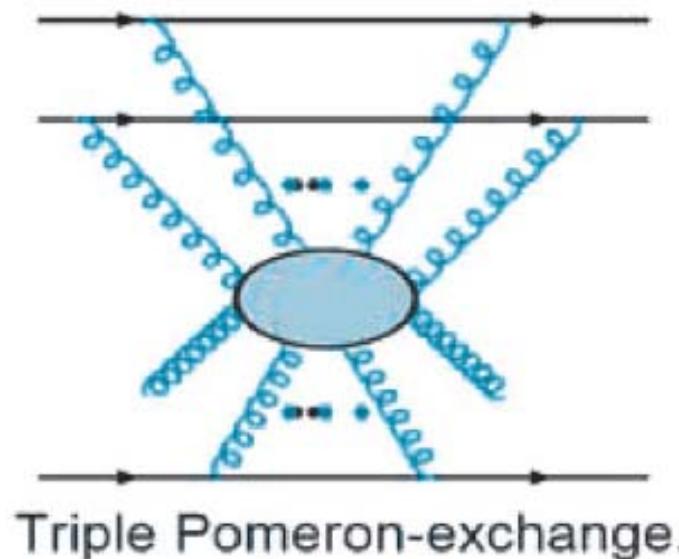
What is pomeron ?



g_P

Why pomeron ?

SU3 scalar



g_{3P}

Pomeron is a model for multi-gluon exchange

ポメロン交換は斥力芯効果に
対する実体論的模型であり
多体斥力効果が自然に導かれる

ざっくり云うと

現象論: hard (soft) cores

実体論: ω meson, pomeron, quark Pauli, SJM

本質論: LQCD, ...

How to determine coupling constants g_{3P} and g_{4P} ?



Nucleus-Nucleus scattering data
with G-matrix folding potential

Y. Yamamoto, T. Furumoto, N. Yasutake and Th. A. Rijken: Phys. Rev. C 88
(2013) 022801(R).

Double folding Potential

$$\begin{aligned}
 U(\mathbf{R}) &= \int \rho_1(\mathbf{r}_1) \rho_2(\mathbf{r}_2) v_D(\mathbf{s}; \rho, E) d\mathbf{r}_1 d\mathbf{r}_2 \\
 &\quad + \int \rho_1(\mathbf{r}_1, \mathbf{r}_1 - \mathbf{s}) \rho_2(\mathbf{r}_2, \mathbf{r}_2 + \mathbf{s}) v_{EX}(\mathbf{s}; \rho, E) \exp\left[i \frac{\mathbf{K} \cdot \mathbf{s}}{M}\right] d\mathbf{r}_1 d\mathbf{r}_2 \\
 &= V_{DFM}(\mathbf{R}) + iW_{DFM}(\mathbf{R})
 \end{aligned}$$

Projectile(1) Target(2)

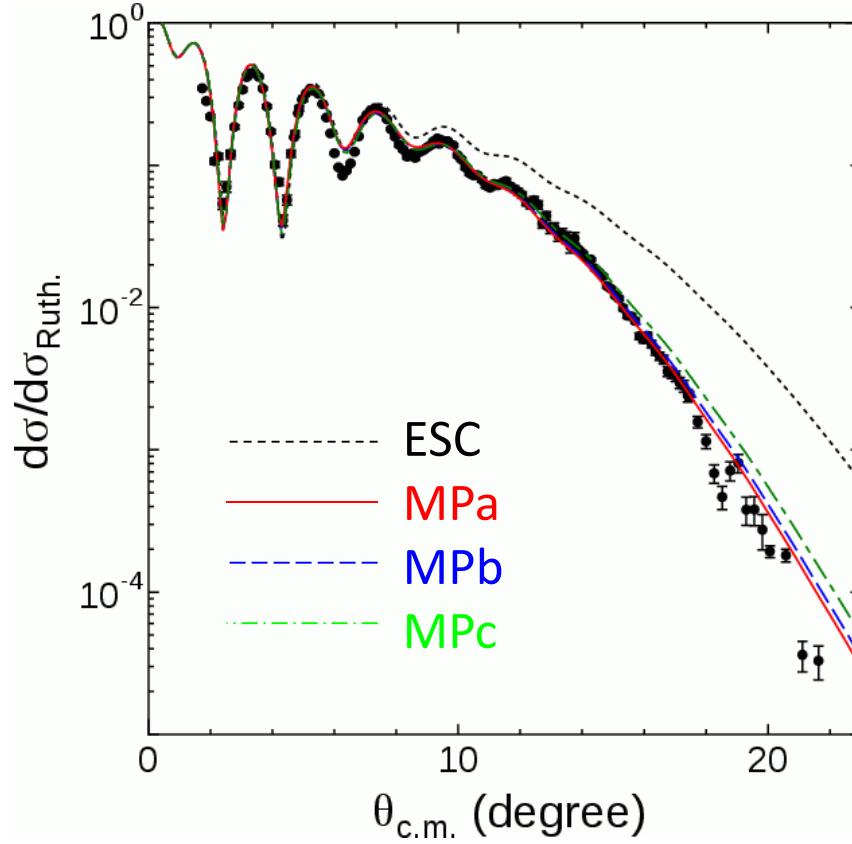
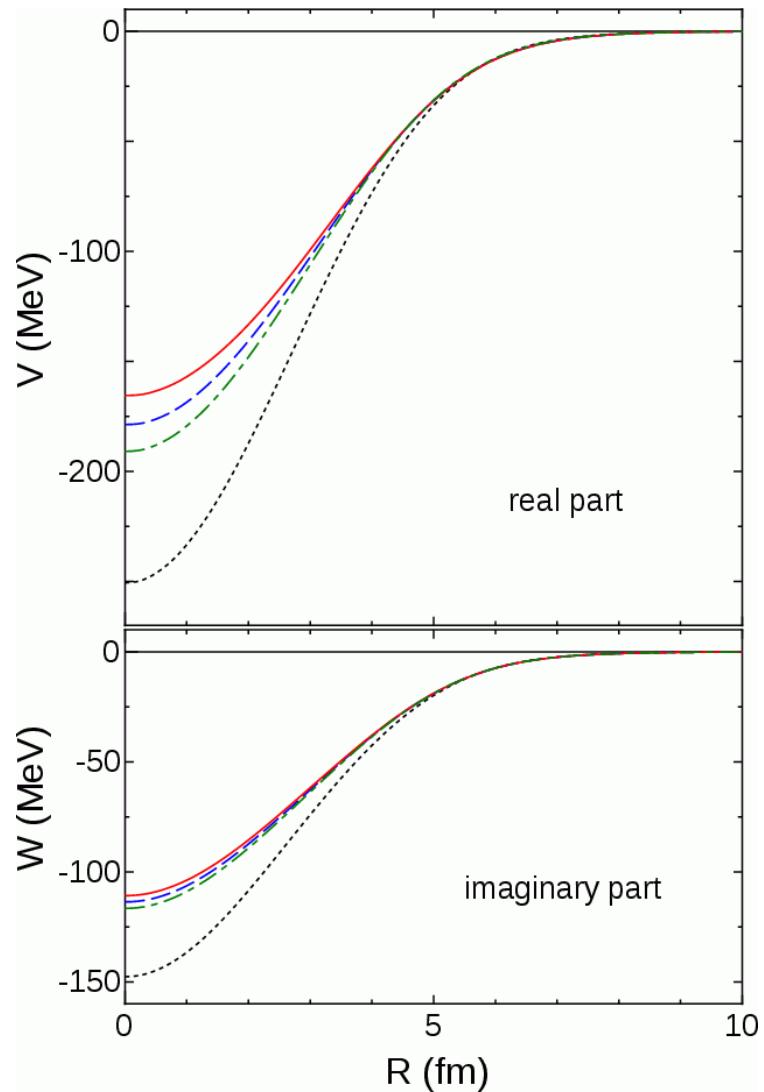
Frozen-density approx. (FDA)
 $\rho = \rho_1 + \rho_2$

Complex G-matrix interaction (CEG07)

$$v_{D,EX} = v_{D,EX}^{(real)} + i v_{D,EX}^{(imag)}$$

T. Furumoto, Y. Sakuragi and Y. Yamamoto, (Phys. Rev. C79 (2009) 011601(R))
T. Furumoto, Y. Sakuragi and Y. Yamamoto, (Phys. Rev. C.80 (2009) 044614)

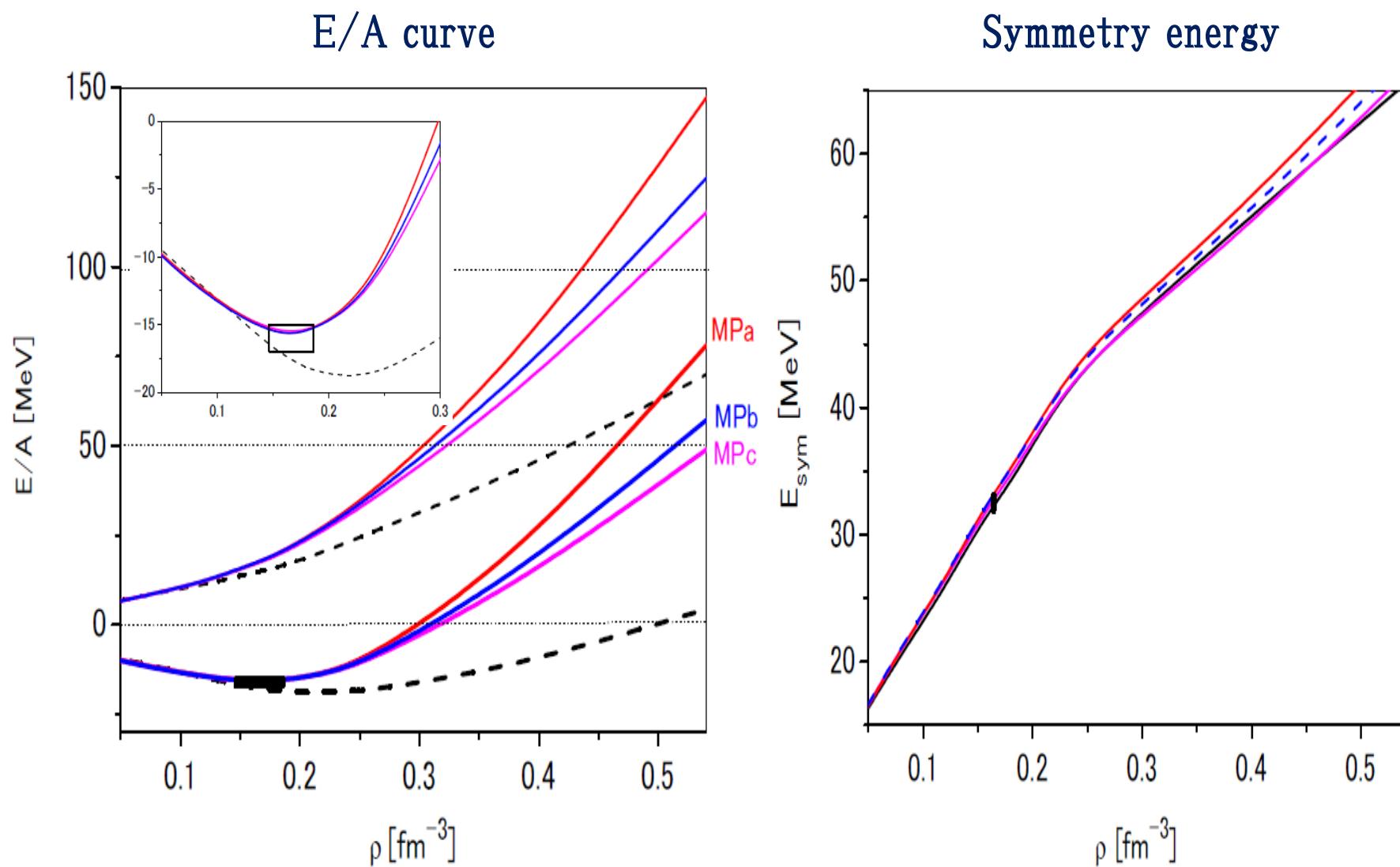
$^{16}O + ^{16}O$ elastic scattering cross section
at $E/A = 70$ MeV



Y. Yamamoto, T. Furumoto, N. Yasutake and Th. A. Rijken,
submitted to Phys. Rev. C

Frozen-Density Approximation is crucial in our approach !

Two Fermi-spheres separated in momentum space
can overlap in coordinate space without
disturbance of Pauli principle



ESC08c + MPP + TNA

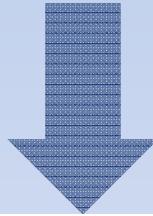
repulsive attractive

MPP and TNA parts are determined to reproduce

- * $^{16}\text{O} + ^{16}\text{O}$ scattering data ($E/A = 70 \text{ MeV}$)
- * nuclear saturation property

$$V_{TNA}(r; \rho) = V_0 \rho \exp(-\eta\rho) \exp(-(r/2.0)^2) (1 + P_r)/2$$

phenomenological

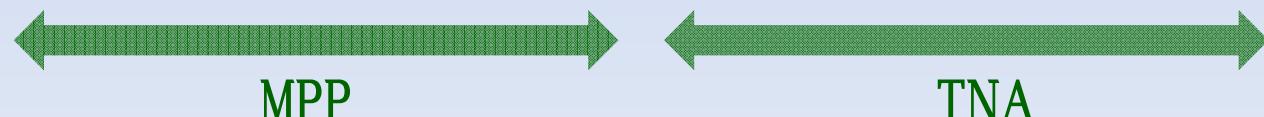


V_0 and η are determined so as to
reproduce saturation density/energy

$$\text{MPa} : (g_P^{(3)}, g_P^{(4)}) = (2.34, 30.) \quad V_0 = -32.8 \quad \eta = 3.5$$

$$\text{MPb} : (g_P^{(3)}, g_P^{(4)}) = (2.94, 0.0) \quad V_0 = -45.0 \quad \eta = 5.4$$

$$\text{MPc} : (g_P^{(3)}, g_P^{(4)}) = (2.34, 0.0) \quad V_0 = -43.0 \quad \eta = 7.3$$



Ratio g_{4P}/g_{3P} is not determined in our analysis \dashrightarrow three versions MPa/b/c

$$E_{sym}(\rho) = \frac{E}{A}(\rho, \beta = 1) - \frac{E}{A}(\rho, \beta = 0)$$

$$L = 3\rho_0 \left[\frac{\partial E_{sym}(\rho)}{\partial \rho} \right]_{\rho=\rho_0}$$

$$K = 9\rho_0^2 \left[\frac{d^2}{d\rho^2} \frac{E}{A}(\rho, \beta = 0) \right]_{\rho=\rho_0}$$

$$\beta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$$

$E/A(\rho_0) = -15.8$ (MPa/b), -15.5 (MPc) MeV at $\rho_0 = 0.16$ fm $^{-3}$

$E_{sym}(\rho_0) = 33.1$ MeV $L(\rho_0) = 70.4$ MeV $K = 310$ MeV for MPa

$E_{sym}(\rho_0) = 33.1$ MeV $L(\rho_0) = 69.2$ MeV $K = 280$ MeV for MPb

$E_{sym}(\rho_0) = 32.7$ MeV $L(\rho_0) = 67.1$ MeV $K = 260$ MeV for MPc

AV8' +UIX : $E_{sym}=35.1$ MeV $L=63.6$ MeV (Gandolfi et al.)

Medium effect in high density region probed by nucleus-nucleus elastic scattering

T. Furumoto,^{1,*} Y. Sakuragi,² and Y. Yamamoto³

PRC(R) accepted

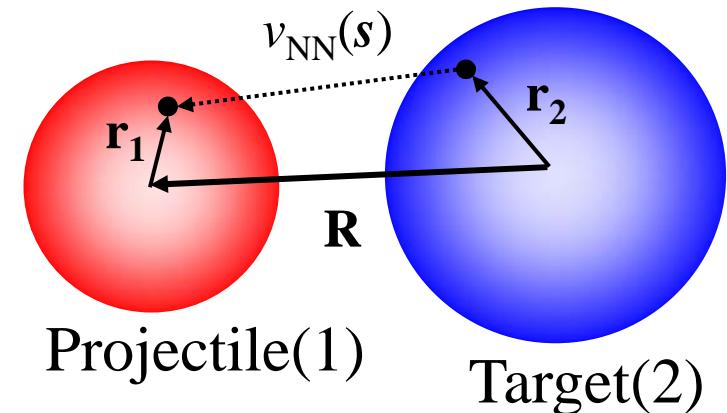
The paper contains some warnings about the use of others widely accepted folding-like methods like JLM. It is important and timely for the community to start a discussion on this subject.

by the referee

crucial role of the TBF effect up to $k_F = 1.6 \text{ fm}^{-1}$

Double folding Potential

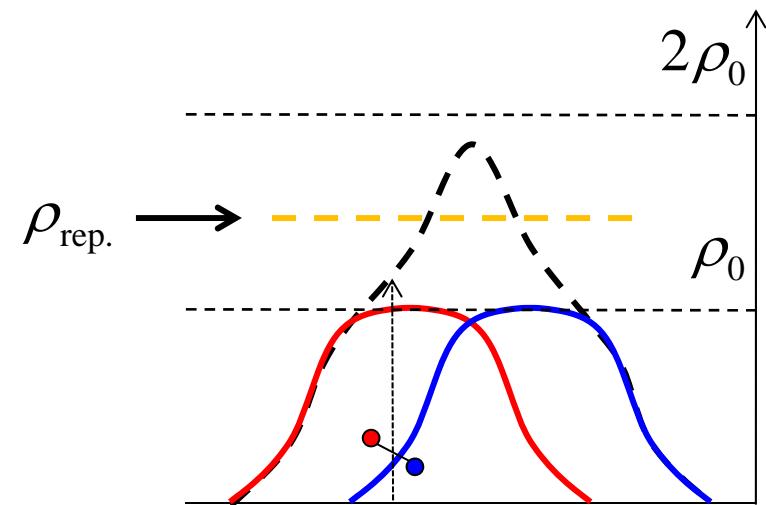
$$U_{DFM}(\mathbf{R}) = V_{DFM}(\mathbf{R}) + iW_{DFM}(\mathbf{R})$$



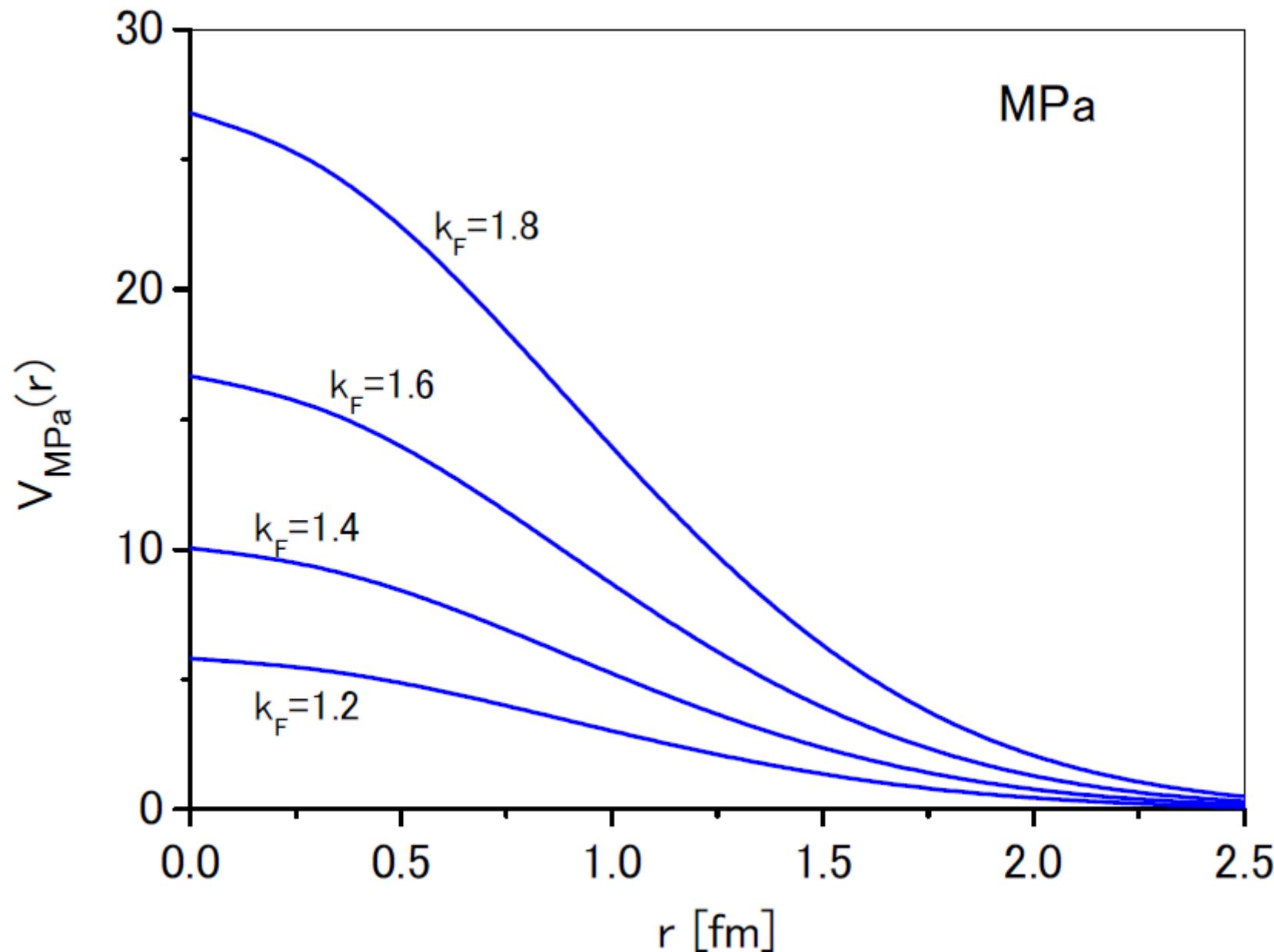
$$U(\mathbf{R}) = \int \rho_1(\mathbf{r}_1) \rho_2(\mathbf{r}_2) v_{NN}^{(D)}(\mathbf{s}; \rho, E) d\mathbf{r}_1 d\mathbf{r}_2 + \int \rho_1(\mathbf{r}_1, \mathbf{r}_1 - \mathbf{s}) \rho_2(\mathbf{r}_2, \mathbf{r}_2 + \mathbf{s}) v_{NN}^{(EX)}(\mathbf{s}; \rho, E) \exp\left[i \frac{\mathbf{K} \cdot \mathbf{s}}{M}\right] d\mathbf{r}_1 d\mathbf{r}_2$$

replace the interaction

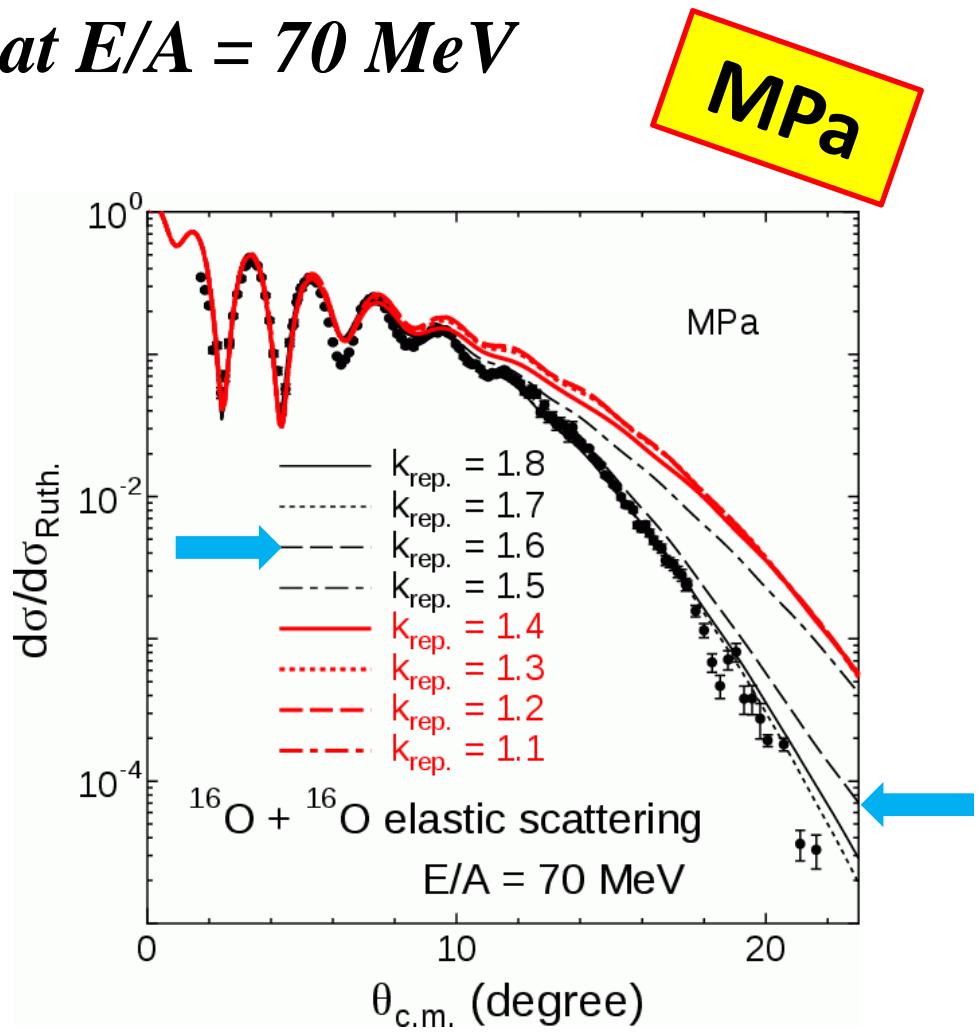
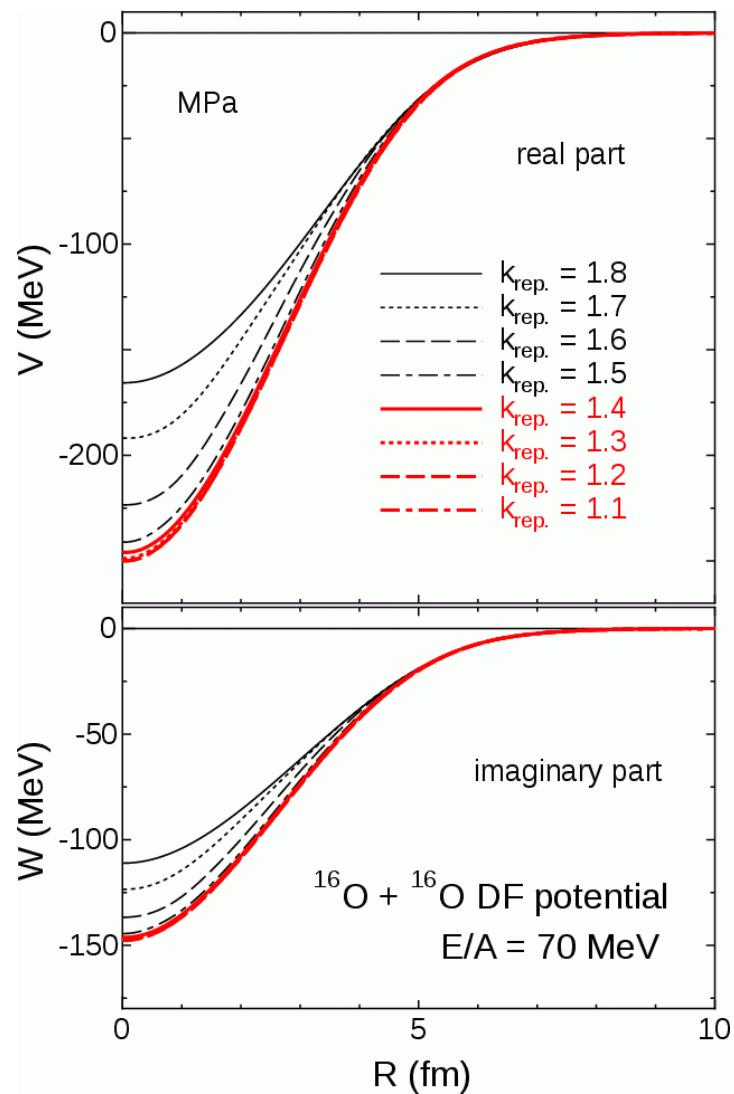
$$v = \begin{cases} \text{MPa } (\rho = \rho_1 + \rho_2 \leq \rho_{\text{rep.}}) \\ \text{ESC } (\rho = \rho_1 + \rho_2 > \rho_{\text{rep.}}) \end{cases}$$



Effective two-body potential derived from MPP



$^{16}\text{O} + ^{16}\text{O}$ elastic scattering cross section at $E/A = 70 \text{ MeV}$

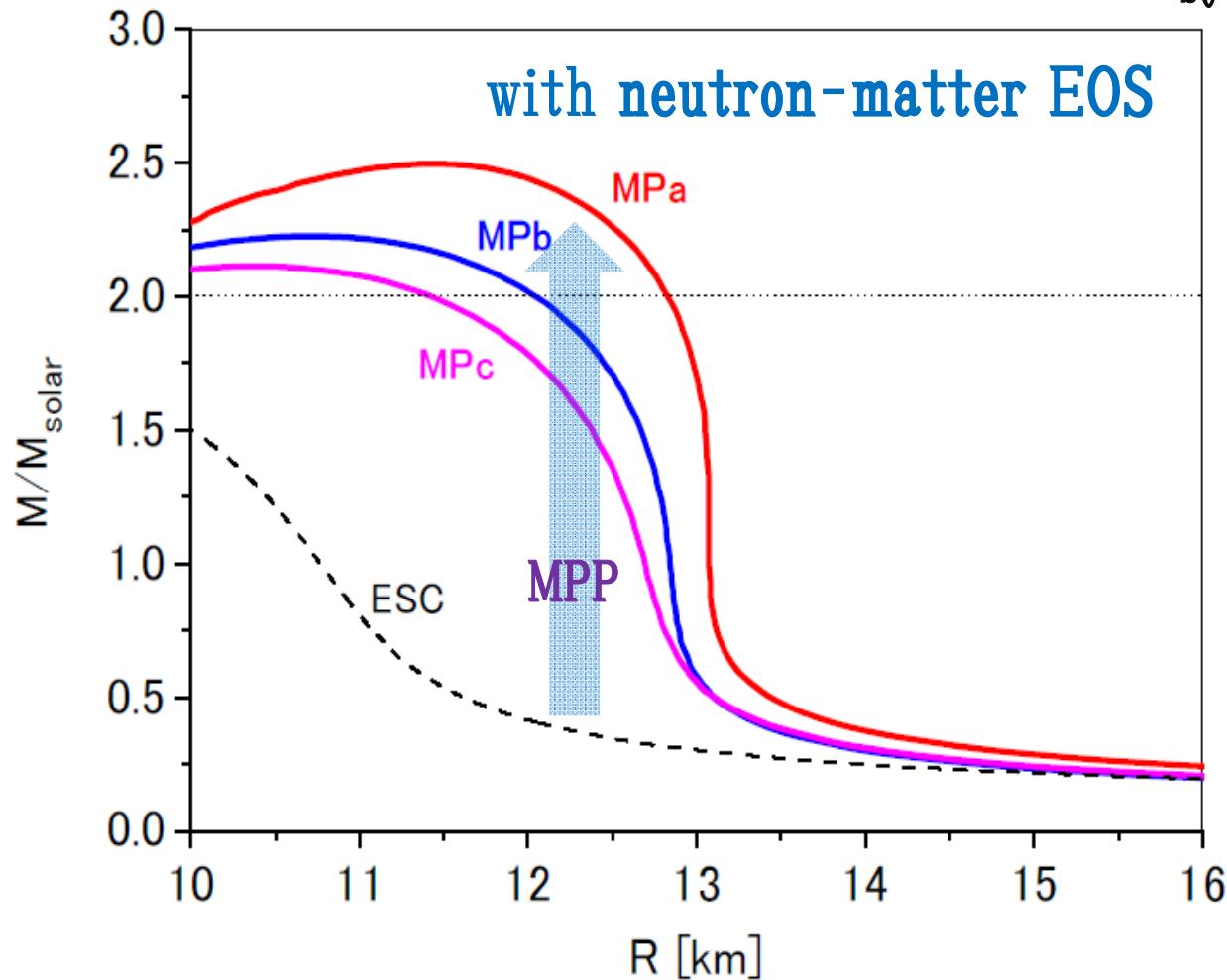


T. Furumoto, Y. Sakuragi and Y. Yamamoto,
 accepted as Rapid Com. in Phys. Rev. C

Medium effect including TBF effect in high density region
- needs up to $k_F = 1.6\text{--}1.7 \text{ fm}^{-1}$ for heavy-ion elastic scattering

Path to high-density EOS

by solving TOV eq.



No ad hoc parameter to adjust stiffness of EOS

MPa : $K=310$ MeV

MPb : $K=280$ MeV

MPc : $K=260$ MeV

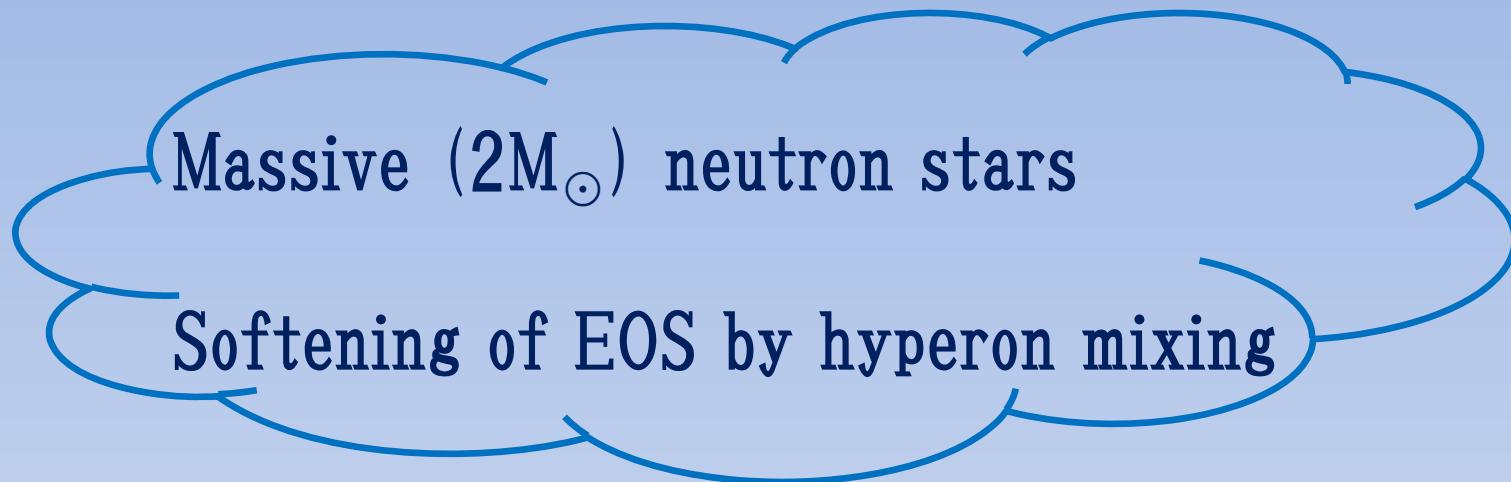
$^{16}\text{O}-^{16}\text{O}$ scattering data

Hyperon-Mixed Neutron-Star Matter

ESC08c
MPP
TNA

defined in S=0,-1,-2 channels
universal in all BB channels
TBA ???

(ESC08c+MPP+TBA) model should be tested in hypernuclei
hyperonic sector



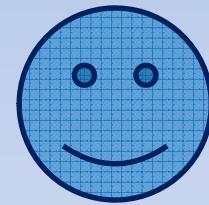
Hyperon puzzle !

An idea is Universal Three-Baryon Repulsion (TBR)
by Takatsuka

Modeling of TBR in ESC = Multi-Pomeron exchange Potential

hypernuclei \longleftrightarrow ? \rightarrow neutron star

YN interactions based on hypernuclear study
→ Hyperon mixing in neutron-star matter



Λ & Σ states based on
ESC08c + MPP + TBA

↑
TNA

Y-nucleus folding potential derived from YN G-matrix interaction $G(r; k_F)$

$$U_Y(\mathbf{r}, \mathbf{r}') = U_{dr} + U_{ex}$$

$$U_{dr} = \delta(\mathbf{r} - \mathbf{r}') \int d\mathbf{r}'' \rho(\mathbf{r}'') V_{dr}(|\mathbf{r} - \mathbf{r}''|; \langle k_F \rangle)$$

$$U_{ex} = \rho(\mathbf{r}, \mathbf{r}') V_{ex}(|\mathbf{r} - \mathbf{r}'|; \langle k_F \rangle) \quad \text{G-matrix interactions}$$

$$V_{dr} = \frac{1}{2(2t_Y + 1)(2s_Y + 1)} \sum_{TS} (2T + 1)(2S + 1) [G_{TS}^{(+)} + G_{TS}^{(-)}]$$

$$V_{ex} = \frac{1}{2(2t_Y + 1)(2s_Y + 1)} \sum_{TS} (2T + 1)(2S + 1) [G_{TS}^{(+)} - G_{TS}^{(-)}]$$

Averaged- k_F Approximation

$$\langle \rho \rangle = \langle \phi_Y(r) | \rho(r) | \phi_Y(r) \rangle$$

$$\langle k_F \rangle = (1.5\pi^2 \langle \rho \rangle)^{1/3}$$

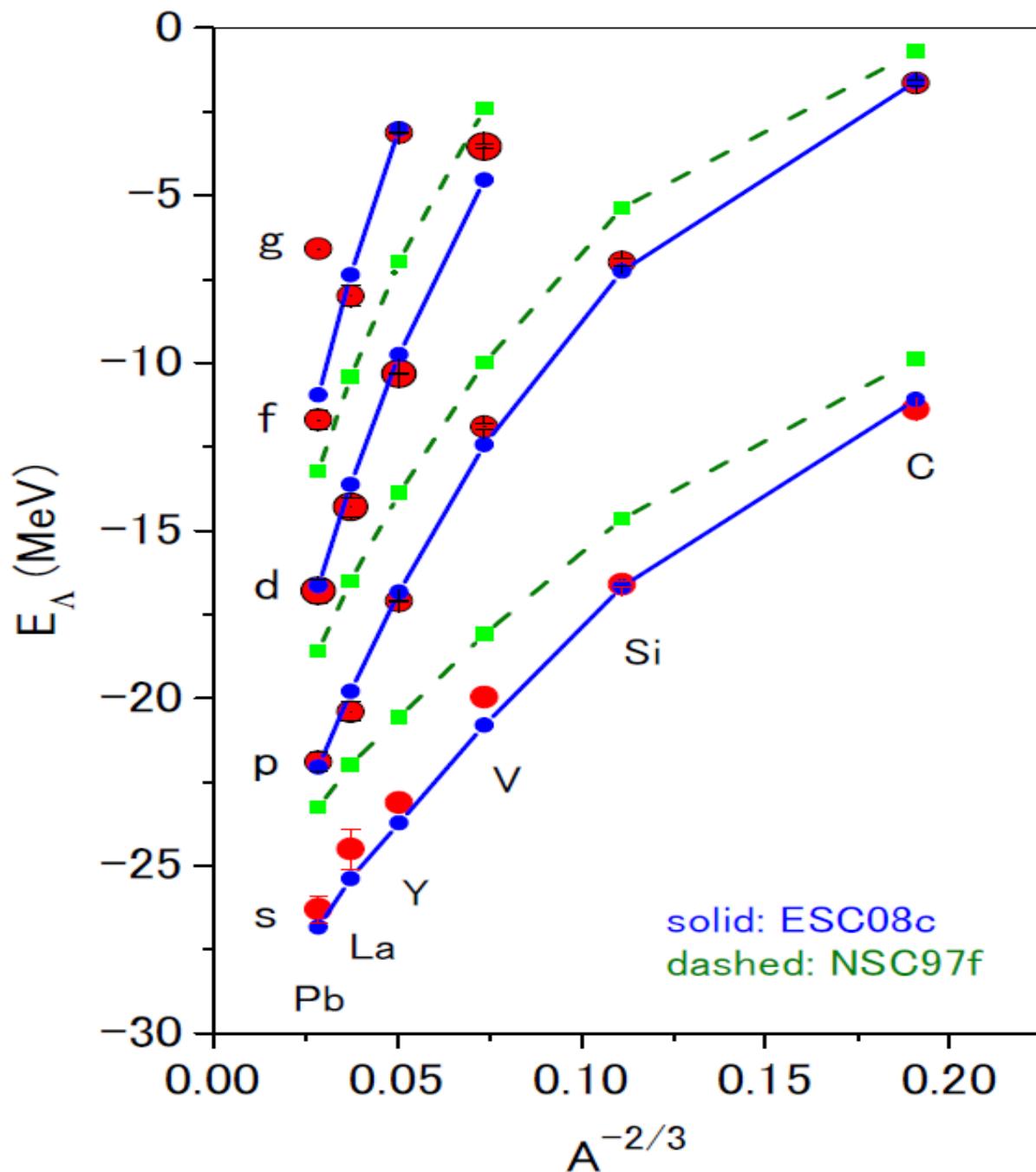
calculated
self-consistently

Mixed density $\rho(\mathbf{r}_1, \mathbf{r}_2) = \sum_j \varphi_j^*(\mathbf{r}_1) \varphi_j(\mathbf{r}_2)$ obtained from SkHF w.f.

ESC08cとNSC97fから導かれるG-matrix interactionの比較 (同じnucleon spectraを用いる)

	1S_0	3S_1	1P_1	3P_0	3P_1	3P_2	D	U_Λ	$U_{\sigma\sigma}$	m_Λ^*
ESC08c	-13.3	-26.7	2.6	0.2	1.8	-3.2	-1.6	-40.0	1.09	0.73
NSC97f	-14.6	-25.0	2.3	0.4	3.7	-0.8	-1.3	-35.4	1.56	0.67

- 違いはodd statesにある (高密度では大きな差)
- ESC08cはIsakaの計算で用いられたバージョン



同じ条件の下では
ESC08cはNSC97f
より優れている

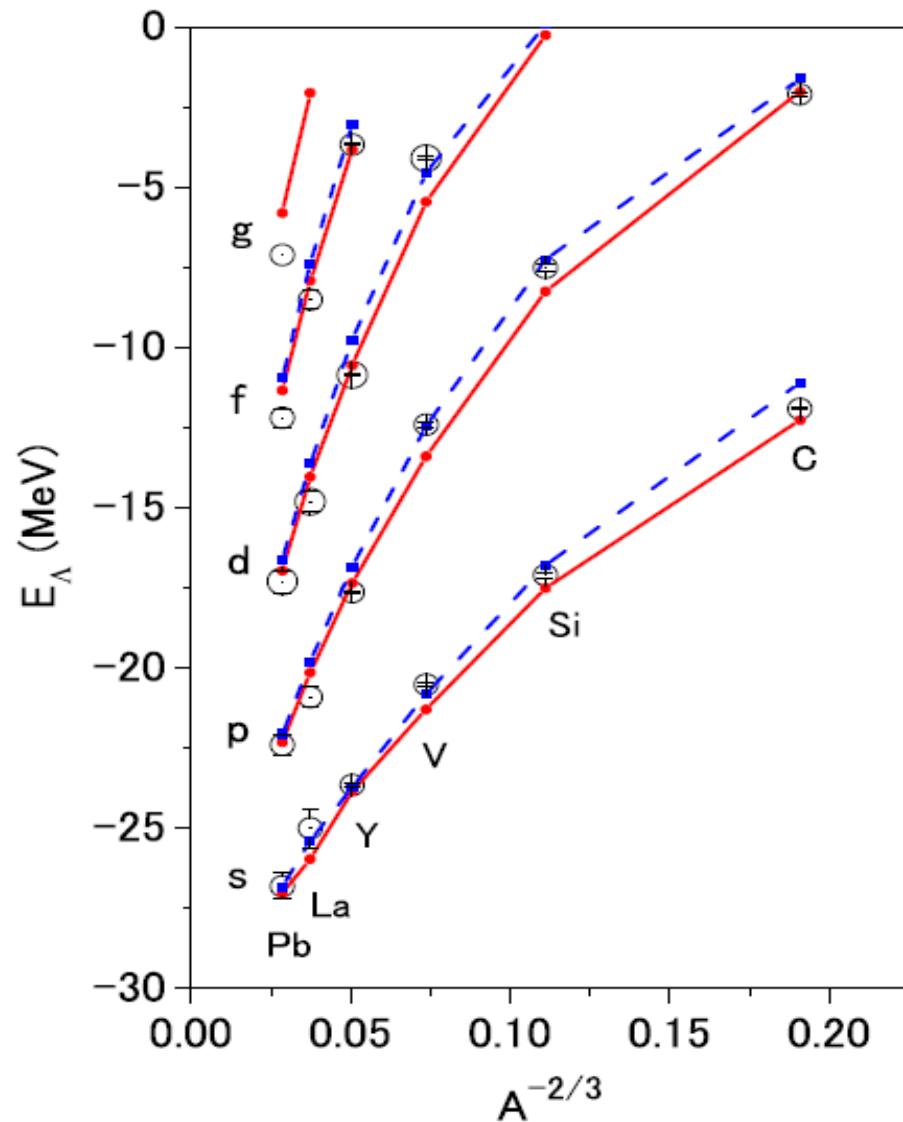
様々なYN相互作用模型(ND/NF, NSC89, NSC97, JA/JB, …)

自然な同一条件(nucleon spectrum等)で比較すれば多くはリジェクトされる

相互作用模型の違いは中性子星における
onset densityに反映される

従来使われたND、NF、NSC89、NSC97eは
それぞれにまずい点を有している

Our Case



	$^{13}_\Lambda C$	$^{12}_\Lambda B$
exp	-11.9	-11.4
MPa	-12.3	-11.6
ESC	-11.1	-10.4

Strong density dependence by (MPP+TBA)
→ mass-dependence of B_Λ

YNN3体力効果を検証するためには
精密で系統的な B_Λ の実験値と
対応する理論計算が必要である

RMF model におけるhyperon sectorへのinput

$$U_{\Lambda}^{(N)} = -30 \text{ MeV} \quad -40.0$$

$$U_{\Sigma}^{(N)} = +30 \text{ MeV} \quad +15.2$$

$$U_{\Xi}^{(N)} = -18 \text{ MeV} \quad -1.2$$

G-matrix with ESC08c

U_YのみがYN interactionの指標ではない
Density dependence, Effective Mass, etc

Quark-Pauli effect in ESC08 models

ESC core = pomeron + ω

Repulsive cores are similar
to each other in all channels

Assuming

“equal parts” of ESC and QM are similar to each other

Almost Pauli-forbidden states in [51] are taken
into account by changing the pomeron strengths
for the corresponding channels phenomenologically

$$g_P \xrightarrow{\text{factor}} \text{factor} * g_P$$

by Oka-Shimizu-Yazaki

Table III. $SU(6)_{fs}$ -contents of the various potentials on the isospin, spin basis.

(S, I)	$V = aV_{[51]} + bV_{[33]}$
$(0, 1)$	$V_{NN} = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$(1, 0)$	$V_{NN} = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$(0, 1/2)$	$V_{\Lambda\Lambda} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$(1, 1/2)$	$V_{\Lambda\Lambda} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$(0, 1/2)$	$V_{\Sigma\Sigma} = \frac{17}{18}V_{[51]} + \frac{1}{18}V_{[33]}$
$(1, 1/2)$	$V_{\Sigma\Sigma} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$(0, 3/2)$	$V_{\Sigma\Sigma} = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$(1, 3/2)$	$V_{\Sigma\Sigma} = \frac{8}{9}V_{[51]} + \frac{1}{9}V_{[33]}$

(S, I)	$V = aV_{[51]} + bV_{[33]}$
$(0, 0)$	$V_{\Lambda\Lambda, \Lambda\Lambda} = \frac{1}{2}V_{[51]} + \frac{1}{2}V_{[33]}$
$(0, 0)$	$V_{\Xi N, \Xi N} = \frac{1}{3}V_{[51]} + \frac{2}{3}V_{[33]}$
$(0, 0)$	$V_{\Sigma\Sigma, \Sigma\Sigma} = \frac{11}{18}V_{[51]} + \frac{7}{18}V_{[33]}$
$(0, 1)$	$V_{\Xi N, \Xi N} = \frac{7}{9}V_{[51]} + \frac{2}{9}V_{[33]}$
$(0, 0)$	$V_{\Sigma\Lambda, \Sigma\Lambda} = \frac{2}{3}V_{[51]} + \frac{1}{3}V_{[33]}$
$(0, 2)$	$V_{\Sigma\Sigma, \Sigma\Sigma} = \frac{4}{9}V_{[51]} + \frac{5}{9}V_{[33]}$
$(1, 0)$	$V_{\Xi N, \Xi N} = \frac{5}{9}V_{[51]} + \frac{4}{9}V_{[33]}$
$(1, 1)$	$V_{\Xi N, \Xi N} = \frac{17}{27}V_{[51]} + \frac{10}{27}V_{[33]}$
$(1, 1)$	$V_{\Sigma\Lambda, \Sigma\Lambda} = \frac{2}{3}V_{[51]} + \frac{1}{3}V_{[33]}$
$(1, 1)$	$V_{\Sigma\Sigma, \Sigma\Sigma} = \frac{16}{27}V_{[51]} + \frac{11}{27}V_{[33]}$

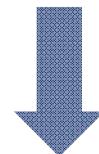
Pauli-forbidden state in $V_{[51]}$  strengthen pomeron coupling

$$V_{BB} = V(\text{pom}) + w_{BB}[51] * \underline{V(\text{PB})}$$

Table 1: Values of U_Σ at normal density and partial wave contributions for ESC08c models (in MeV).

model	T	1S_0	3S_1	1P_1	3P_0	3P_1	3P_2	D	U_Σ
ESC08c	1/2	10.9	-21.6	2.4	2.1	-6.0	-1.0	-0.7	
	3/2	-13.5	31.0	-4.7	-1.8	5.9	-1.5	-0.2	+1.2

Pauli-forbidden state in QCM \rightarrow strong repulsion in T=3/2 3S_1 state



Σ^- in neutron matter

$$U_{\Sigma^-} = +15.2 \text{ MeV}$$

Events of twin Λ hypernuclei in emulsion

Event I (most probable mode) [1]

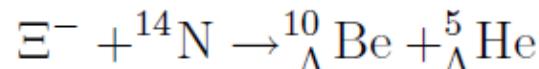
- (A) $\Xi^- + {}^{12}\text{C} \rightarrow {}^9_{\Lambda}\text{Be} + {}^4_{\Lambda}\text{H}$ ($B_{\Xi^-} = 0.82 \pm 0.17$ MeV) ,
(B) $\Xi^- + {}^{12}\text{C} \rightarrow {}^9_{\Lambda}\text{Be} + {}^4_{\Lambda}\text{H}^*$ ($B_{\Xi^-} = -0.23 \pm 0.17$ MeV) ,

E176 events

Event II (three possibilities) [2]

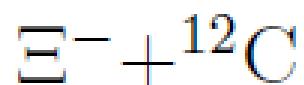
- (A) $\Xi^- + {}^{12}\text{C} \rightarrow {}^9_{\Lambda}\text{Be} + {}^4_{\Lambda}\text{H}$ ($B_{\Xi^-} = 3.89 \pm 0.14$ MeV) ,
(B) $\Xi^- + {}^{12}\text{C} \rightarrow {}^9_{\Lambda}\text{Be}^* + {}^4_{\Lambda}\text{H}$ ($B_{\Xi^-} = 0.82 \pm 0.14$ MeV) ,
(C) $\Xi^- + {}^{12}\text{C} \rightarrow {}^9_{\Lambda}\text{Be} + {}^4_{\Lambda}\text{H}^*$ ($B_{\Xi^-} = 2.84 \pm 0.15$ MeV) ,
(D) $\Xi^- + {}^{12}\text{C} \rightarrow {}^9_{\Lambda}\text{Be}^* + {}^4_{\Lambda}\text{H}^*$ ($B_{\Xi^-} = -0.19 \pm 0.15$ MeV) ,

木曾イベント

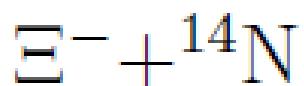


- (A) ${}^{10}_{\Lambda}\text{Be}$ in ground state ($B_{\Xi^-} = 3.82 \pm 0.18$ MeV) ,
(B) ${}^{10}_{\Lambda}\text{Be}$ in excitation of 2.68MeV ($B_{\Xi^-} = 1.14 \pm 0.18$ MeV)

G-matrix folding model



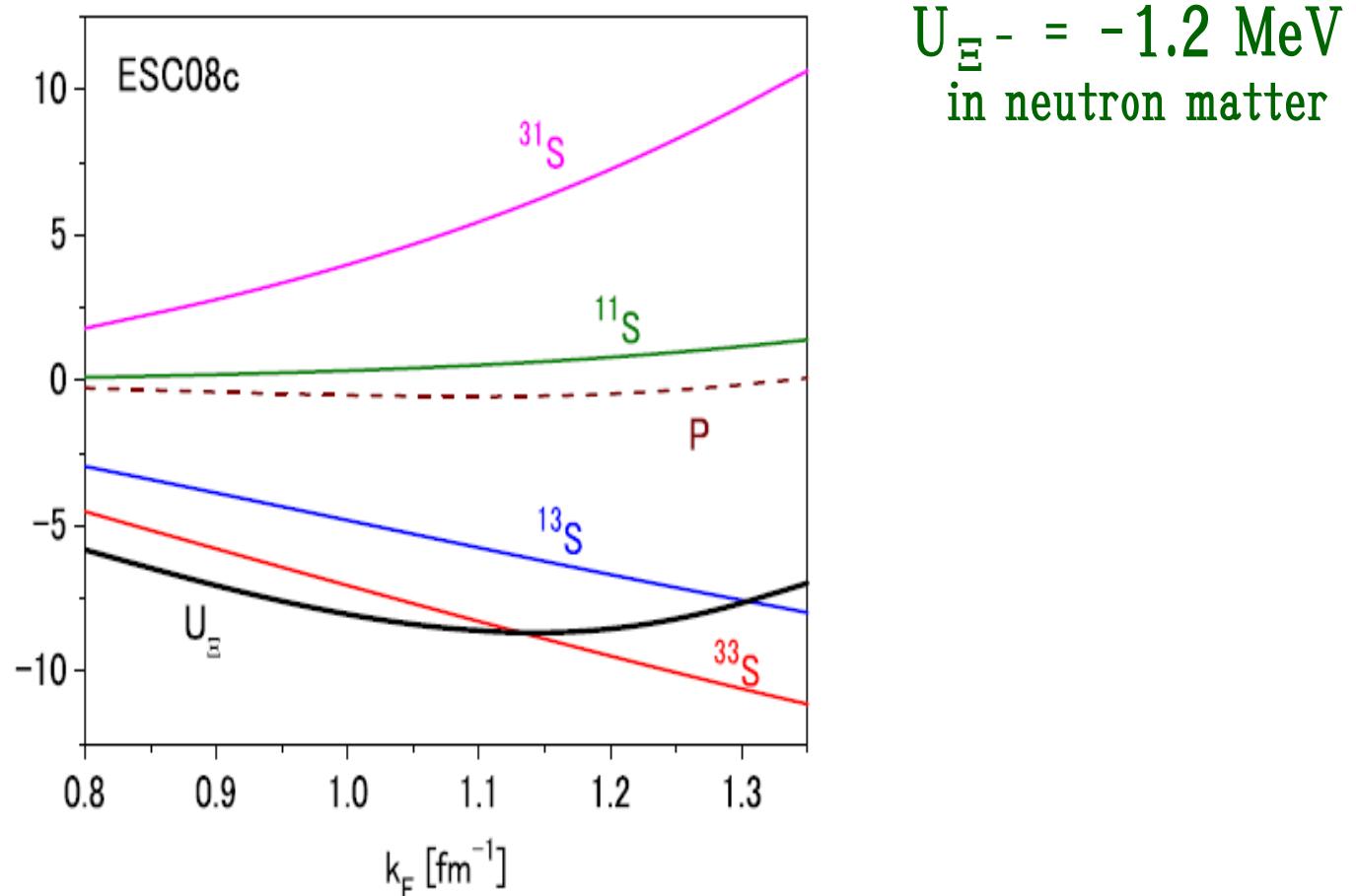
		ESC08c	Ehime	exp
1S	B_{Ξ^-}	3.83	5.10	
	Γ_{Ξ^-}	1.49	0.21	
	$\sqrt{\langle r^2 \rangle}$	3.34	3.18	
	\bar{k}_F	1.16	1.22	
2P	B_{Ξ^-}	0.68	0.82	0.82 ± 0.17
	Γ_{Ξ^-}	0.44	0.13	
	$\sqrt{\langle r^2 \rangle}$	7.54	6.92	
	\bar{k}_F	0.84	0.75	



		ESC08c	Ehime	exp
1S	B_{Ξ^-}	4.82	5.45	
	Γ_{Ξ^-}	1.87	0.25	
	$\sqrt{\langle r^2 \rangle}$	3.18	3.18	
	\bar{k}_F	1.19	1.25	
2P	B_{Ξ^-}	1.22	1.17	1.14 ± 0.18
	Γ_{Ξ^-}	0.77	0.17	
	$\sqrt{\langle r^2 \rangle}$	5.66	6.17	
	\bar{k}_F	0.93	0.80	

Table 1: $U_{\Xi}(\rho_0)$ and partial wave contributions for ESC08c calculated with the CON choice. Γ_{Ξ}^c denotes ΞN - $\Lambda\Lambda$ conversion width. all entries are in MeV.

T	1S_0	3S_1	1P_1	3P_0	3P_1	3P_2	U_{Ξ}	Γ_{Ξ}^c
0	1.4	-8.0	-0.3	1.8	1.4	-2.1		
1	10.7	-11.1	1.1	0.7	-2.6	-0.0	-7.0	4.5



Hyperon-mixed Neutron-Star matter with universal TBR (MPP)

EoS of $n + p + \Lambda + \Sigma + e^+ \mu^-$ system

ESC08c(YN) + MPP(YNN) +TBA(YNN)

Hyperon-mixed neutron matter

Starting from single particle potentials calculated with the G-matrix theory:

$$U_B(k) = \sum_{B'} U_B^{(B')}(k) \quad \text{with } B, B' = n, p, \Lambda, \Sigma^-$$

$U_B^{(B')}$ means a single particle potential of B particle in B' matter

$$\varepsilon = \varepsilon_{mass} + \varepsilon_{kin} + \varepsilon_{pot}$$

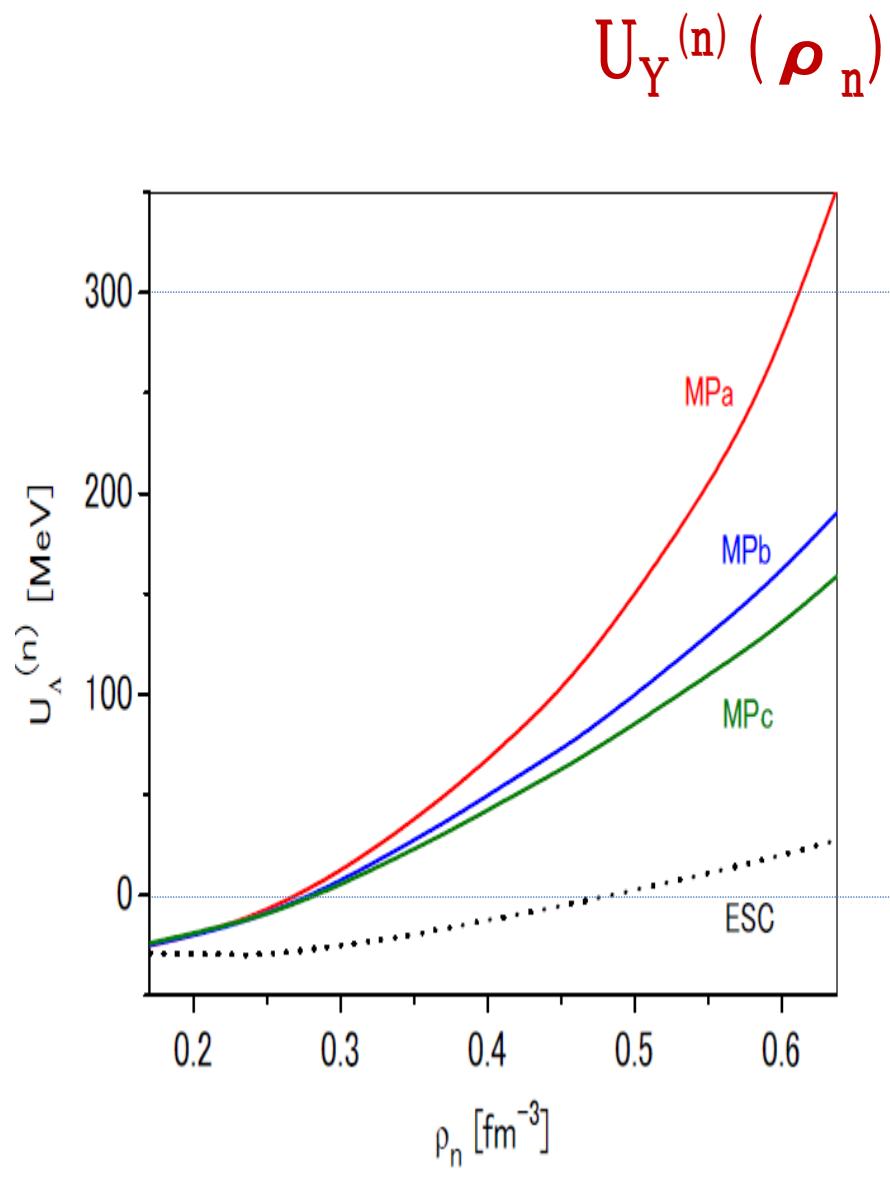
$$= 2 \sum_B \int_0^{k_F^B} \frac{d^3 k}{(2\pi)^3} \left[M_B - M_n + \frac{\hbar^2 k^2}{2M_B} + \frac{1}{2} U_B(k) \right]$$

$$\varepsilon_{mass} = \sum_B (M_B - M_n) \rho_B$$

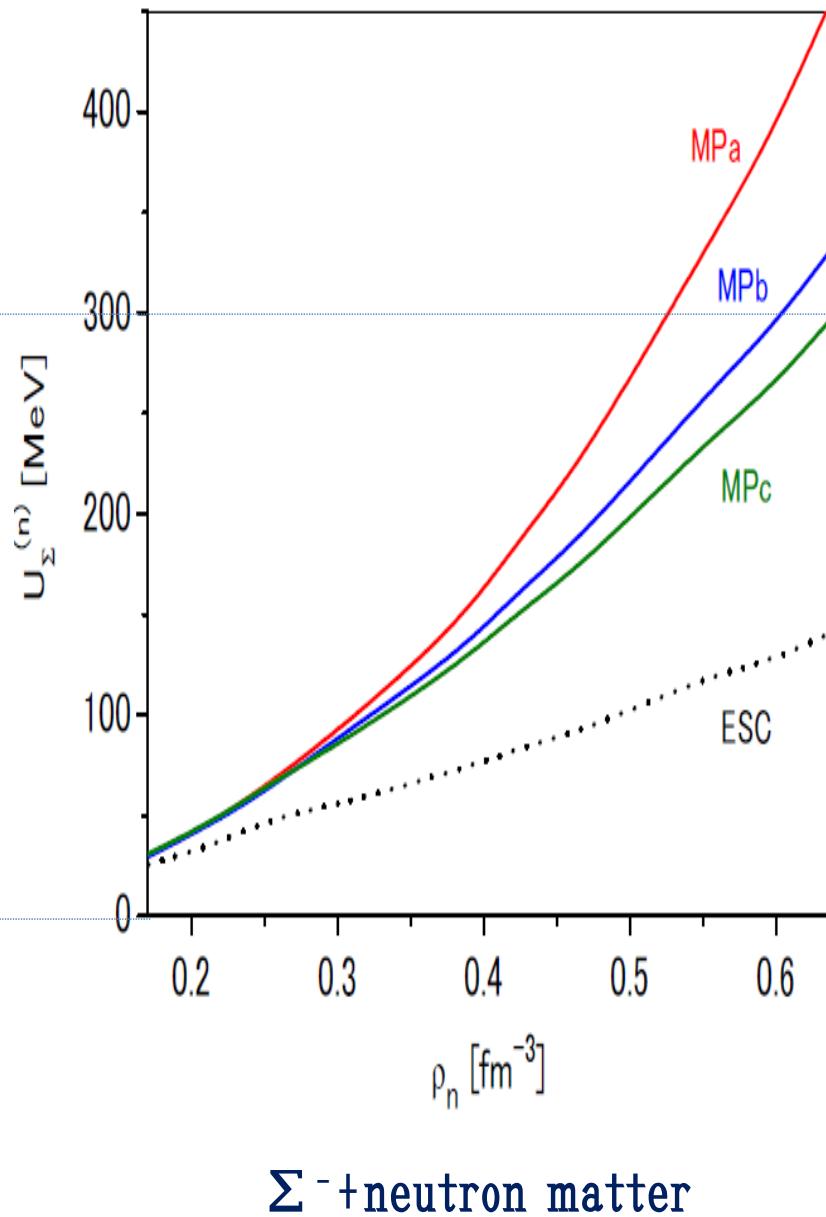
$$\varepsilon_{kin} = \sum_B \frac{3}{5} \frac{\hbar^2 (k_F^B)^2}{2M_B} \rho_B = \sum_B \frac{3}{5} \frac{\hbar^2}{2M_B} (3\pi^2)^{2/3} (\rho_B)^{5/3}$$

$$\varepsilon_{pot} = 2 \sum_B \int_0^{k_F^B} \frac{d^3 k}{(2\pi)^3} \frac{1}{2} U_B(k) = \frac{1}{2} \sum_B \int_0^{k_F^B} \frac{k^2 dk}{\pi^2} U_B(k)$$

Chemical potential : $\mu_B = \frac{\partial \varepsilon}{\partial \rho_B}$



$\Lambda + \text{neutron matter}$



Chemical potential : $\mu_B = \frac{\partial \varepsilon}{\partial \rho_B}$

Chemical equilibrium conditions:

$$\mu_n = \mu_p + \mu_e$$

$$\mu_e = \mu_\mu$$

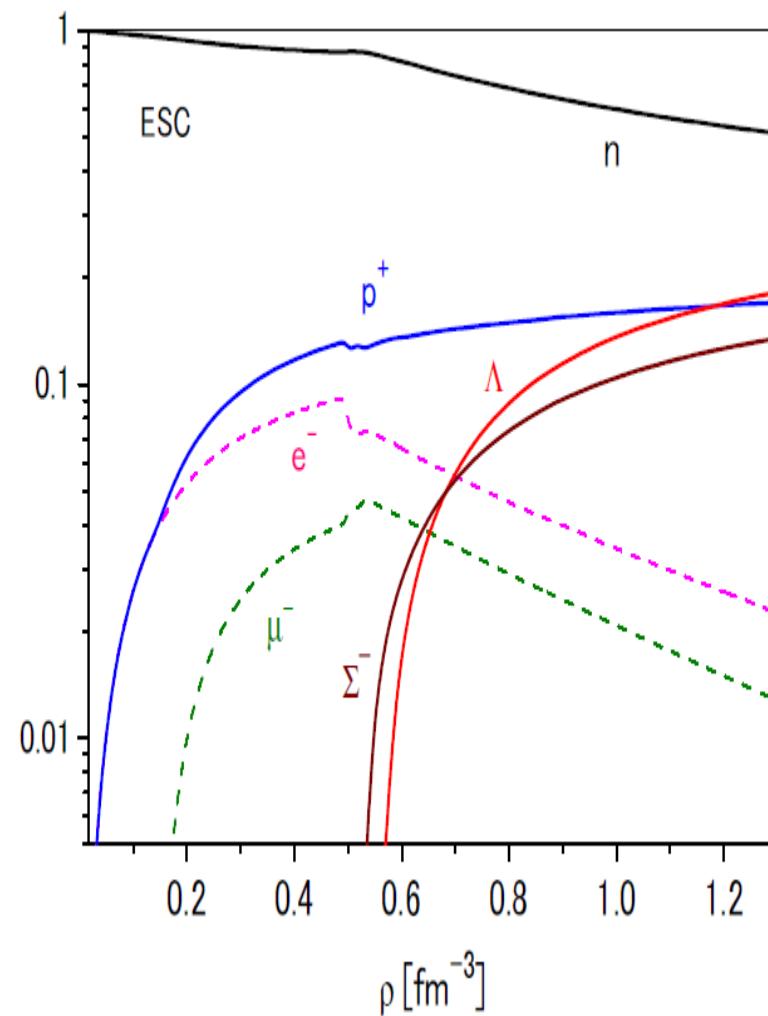
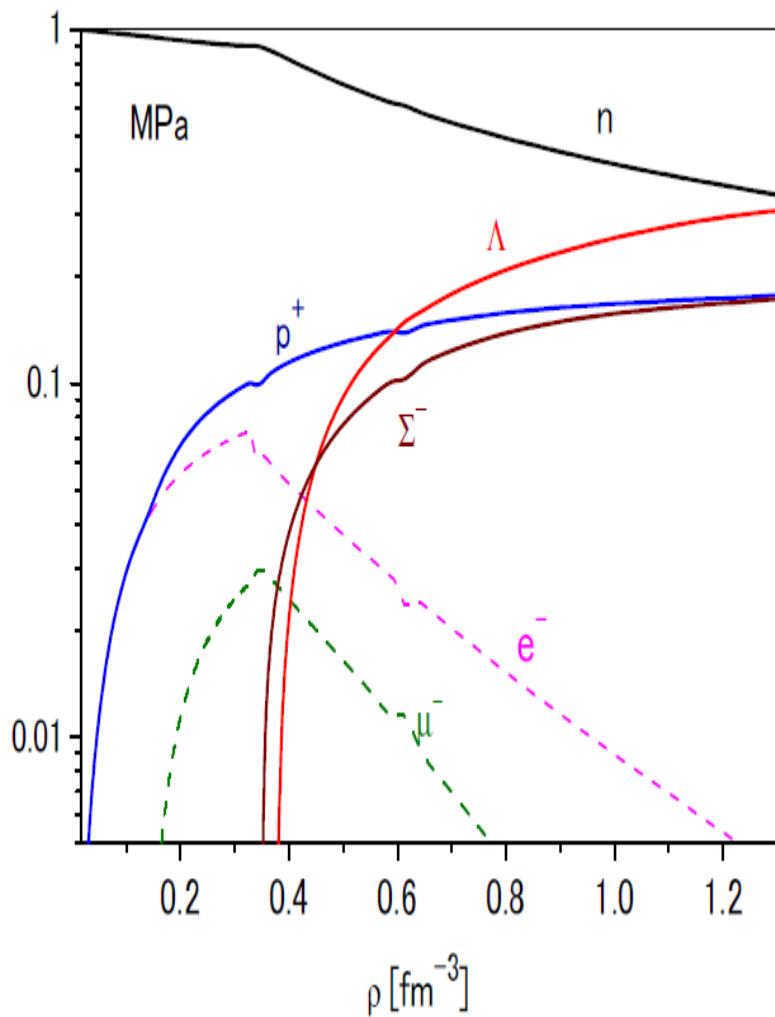
$$\mu_{\Sigma^-} = \mu_n + \mu_e$$

$$\mu_\Lambda = \mu_n$$

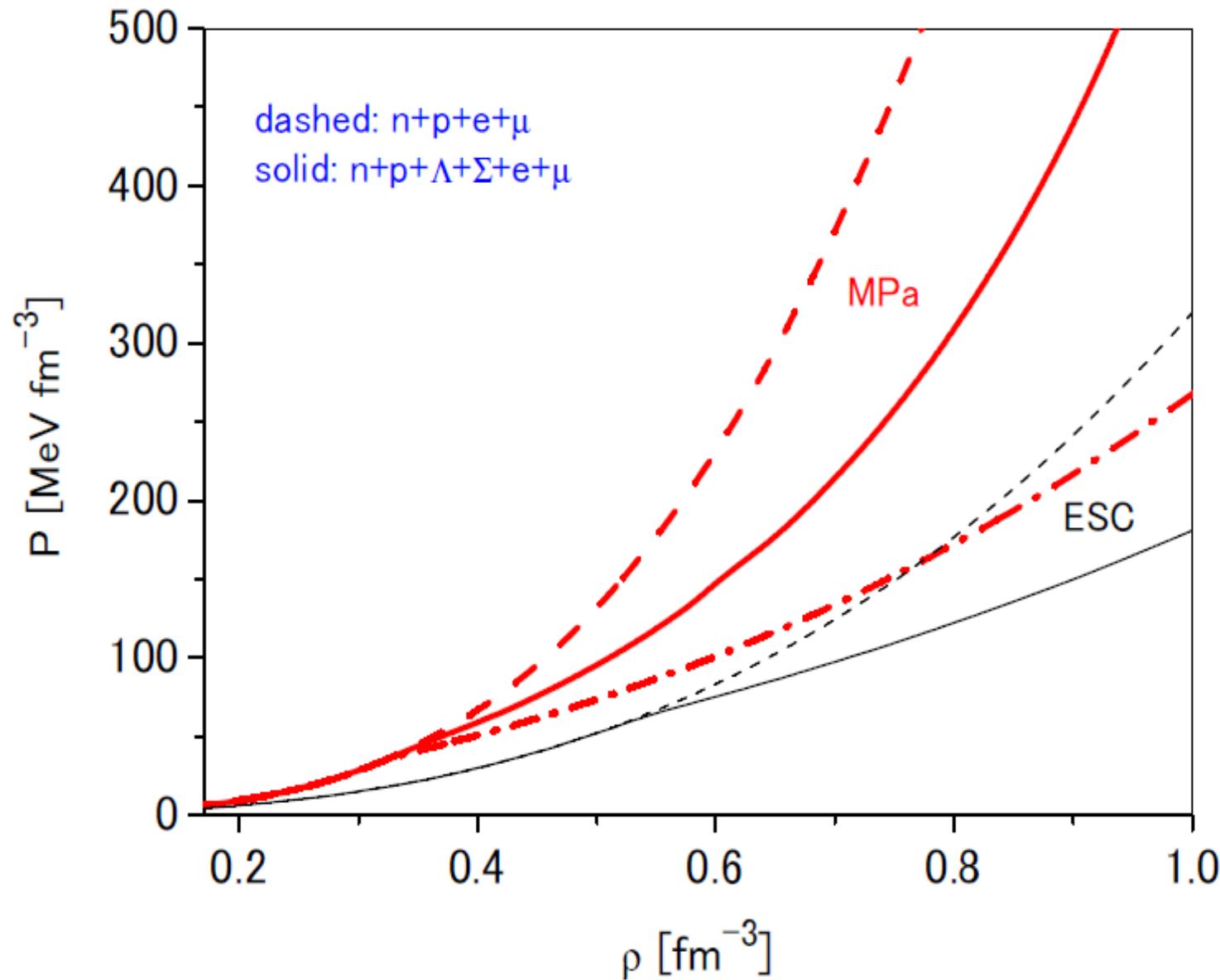
Baryon-number conservation : $y_n + y_p + y_\Lambda + y_{\Sigma^-} = 1$

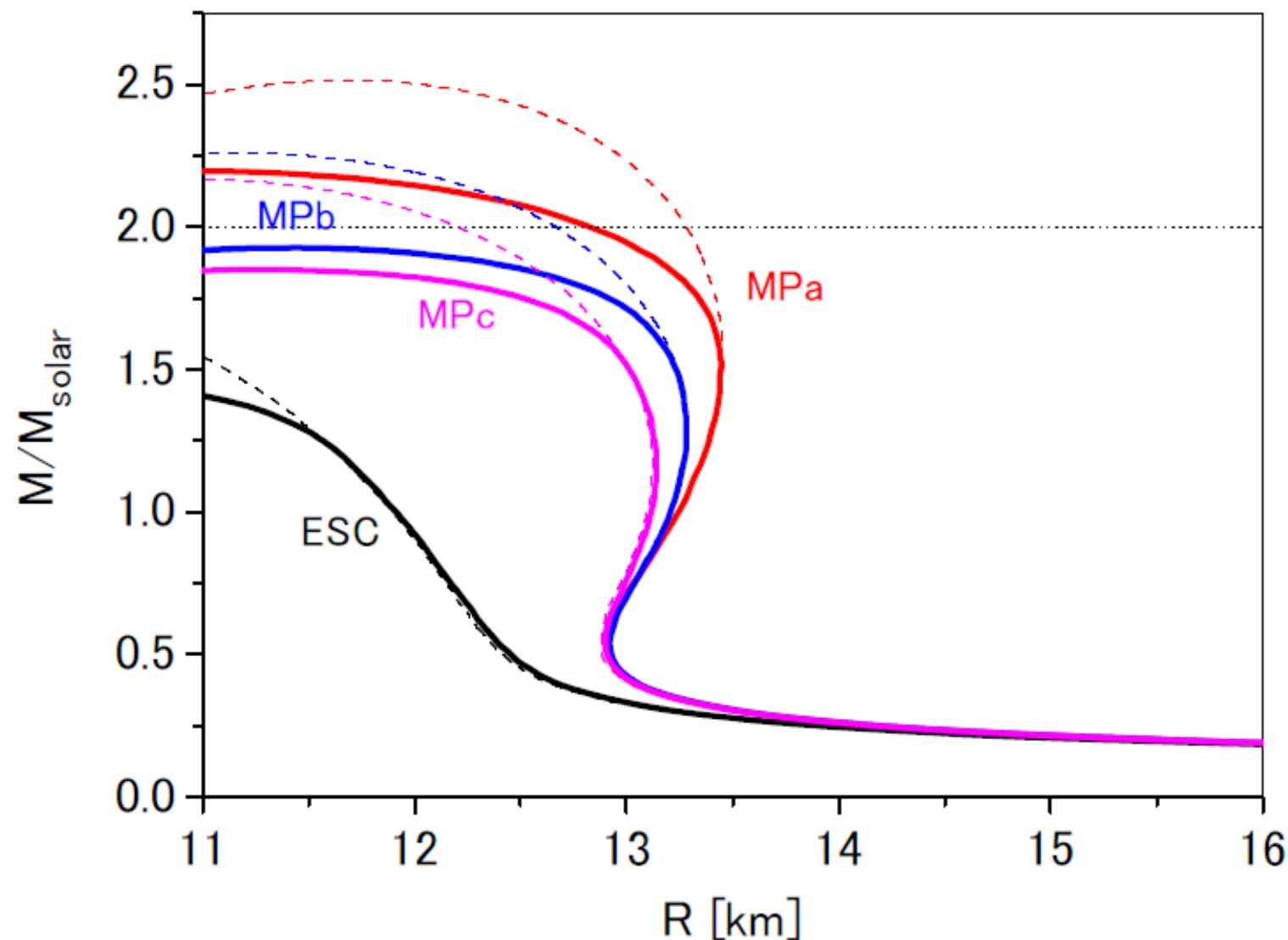
Charge neutrality : $y_p = y_{\Sigma^-} + y_e + y_\mu$

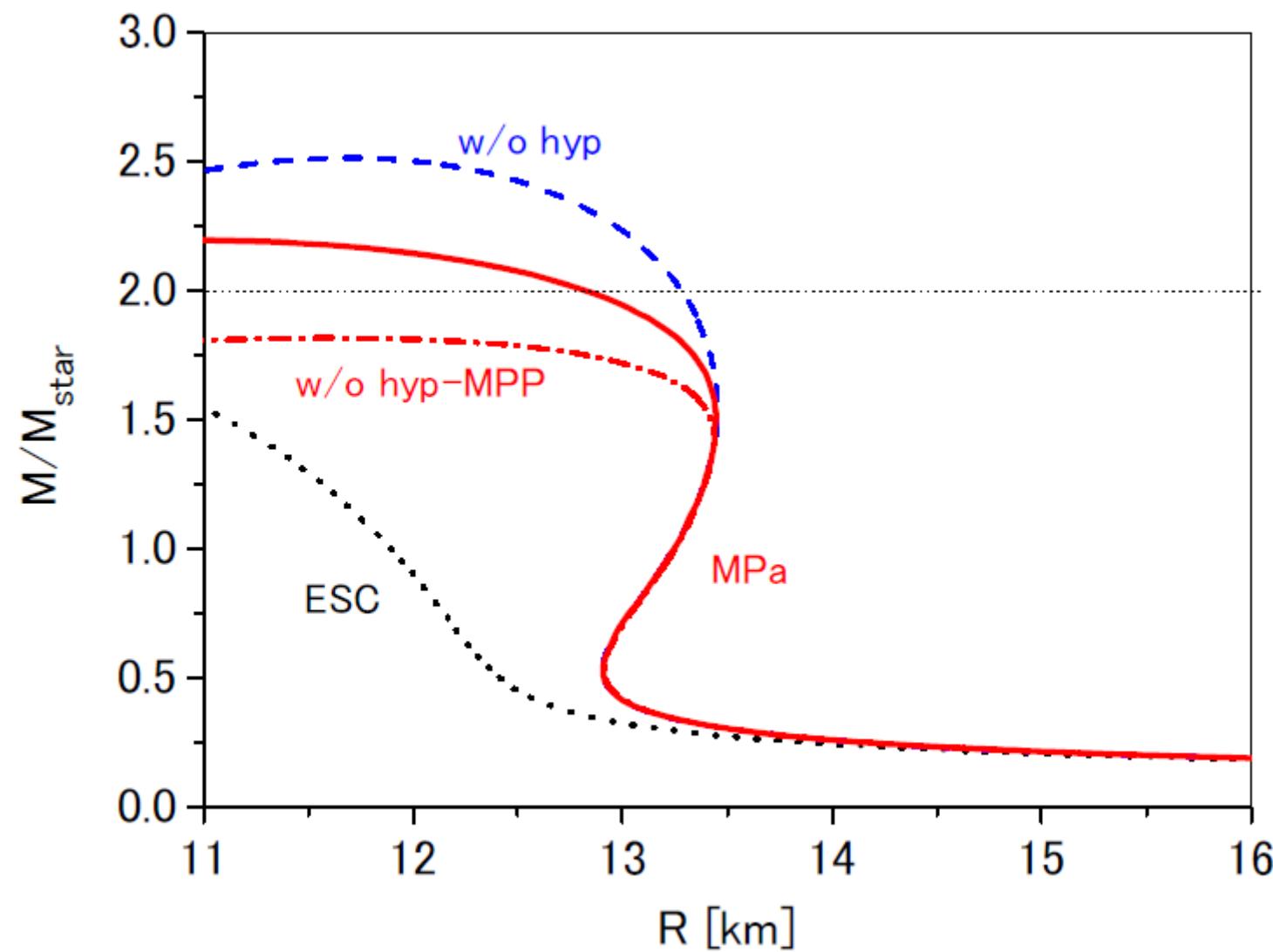
β -stable $n + p + \Lambda + \Sigma^-$ matter

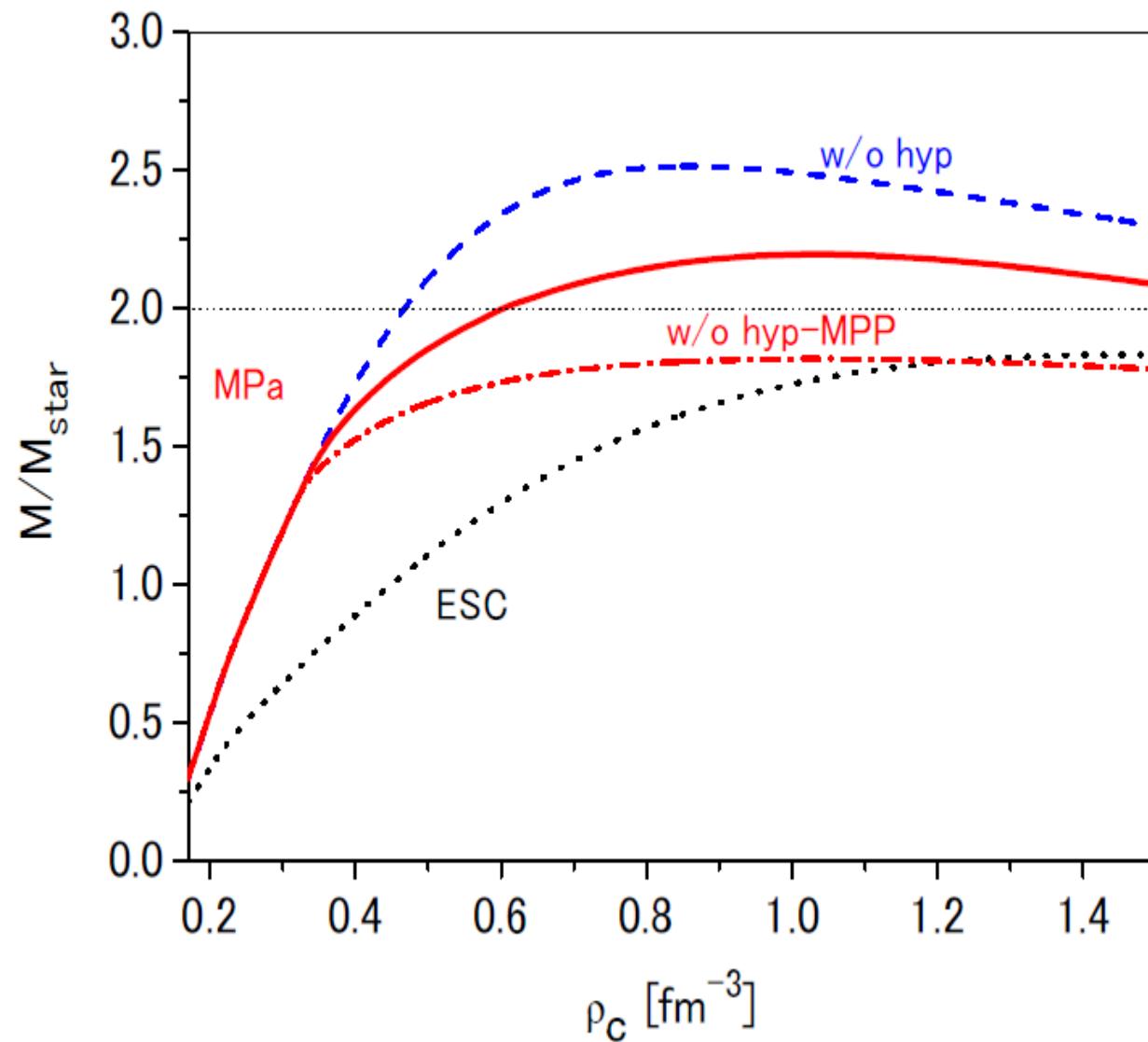


EOS









Conclusion

ESC08c+MPP+TBA model

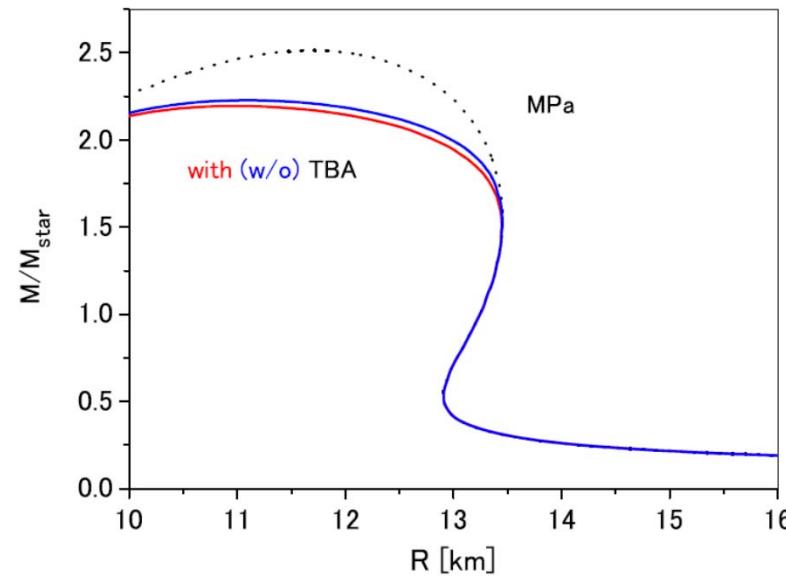
- * MPP strength determined by analysis for $^{16}\text{O} + ^{16}\text{O}$ scattering
- * TNA adjusted phenomenologically to reproduce
 $E/A(\rho_0) = -15.8 \text{ MeV}$ with $\rho_0 = 0.16 \text{ fm}^{-3}$
- * Consistent with hypernuclear data
- * No ad hoc parameter to stiffen EOS
BB interactions based on on-Earth experiments

MPa set including 3- and 4-body repulsions leads to massive neutron stars with $2M_\odot$ in spite of significant softening of EOS by hyperon mixing

MPb/c including 3-body repulsion leads to comparable to or slightly smaller values than $2M_\odot$.

Hyperon Puzzleは解けるか？

B_Λ で決まるのは(MPP+TBA)
中性子星のMR relationに実際に効くのはMPP



MPP(hyperon sector)のterrestrial experiment困難?
LQCDか？