



新学術領域研究

「実験と観測で解き明かす中性子星の核物質」



新学術セミナー

2012年11月24日

KEK東海キャンパス，東海

核物質中の Σ ハイペロン

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J-PARC Branch, KEK Theory Center

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 - 核物質中の Σ ハイペロンの役割
 - 中性子過剰 Λ ハイパー核の生成
4. まとめ

■ Keywords

Hyperon mixing + DCX

1. はじめに

ストレンジネス核物理

➤ ストレンジネスは原子核深部を探るプローブ

– ハイペロンはパウリ排他律を受けない

➤ Impurity Physics

– “糊”としての役割

– 原子核構造の変化

■ Keywords

Hyperon mixing

➤ Baryon-Baryon Interaction

– YN, YY Interaction based on $SU_f(3)$

– 核力の統一的理解・斥力芯の起源

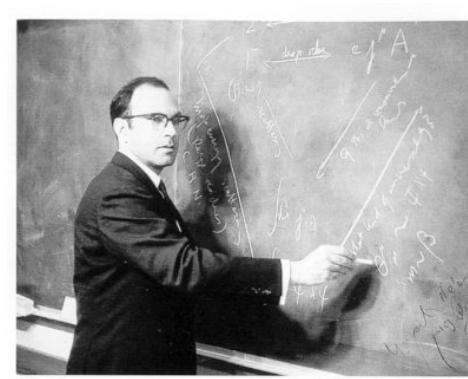
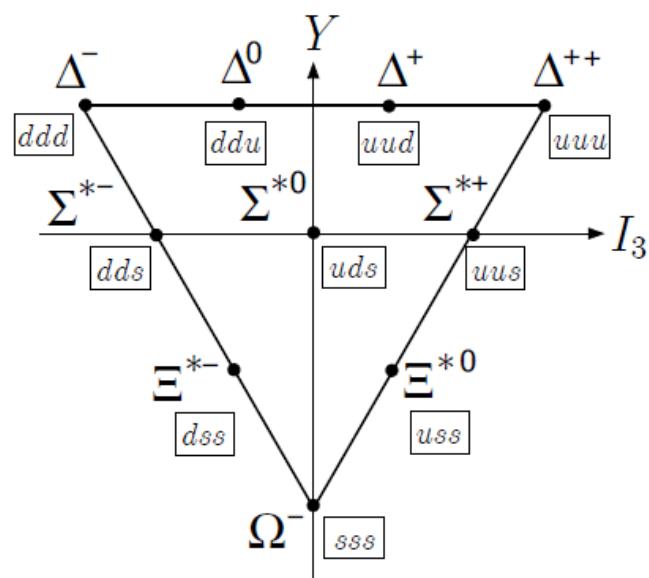
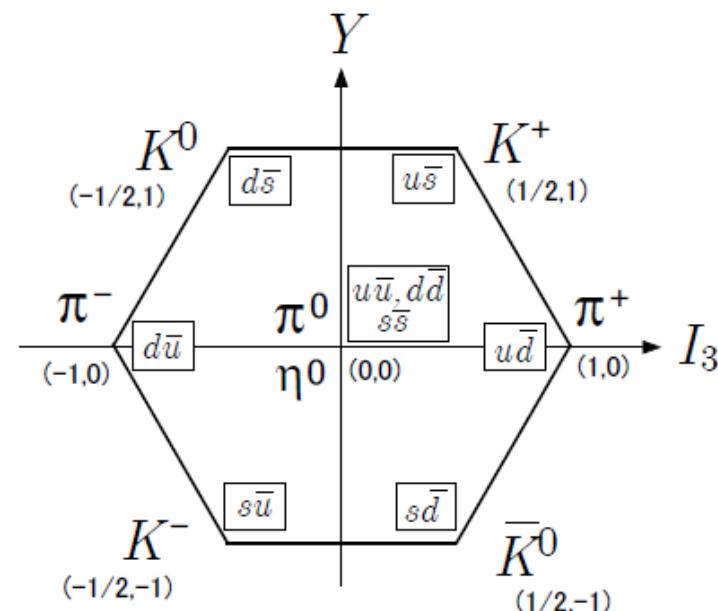
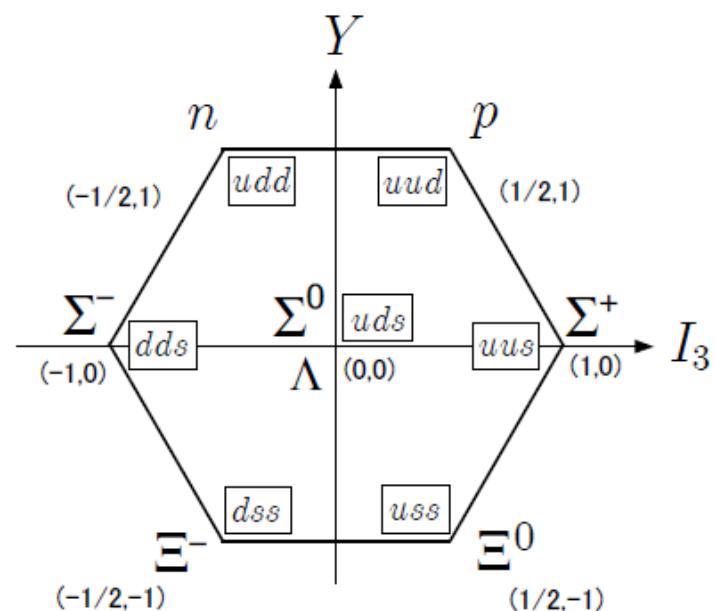
➤ “Exotic” Nuclear Physics

– ストレンジネスが拓く新しい原子核の面白さ

➤ Neutron Starの構造と進化

– 高密度核物質, EOS, 最大質量, 冷却, ...

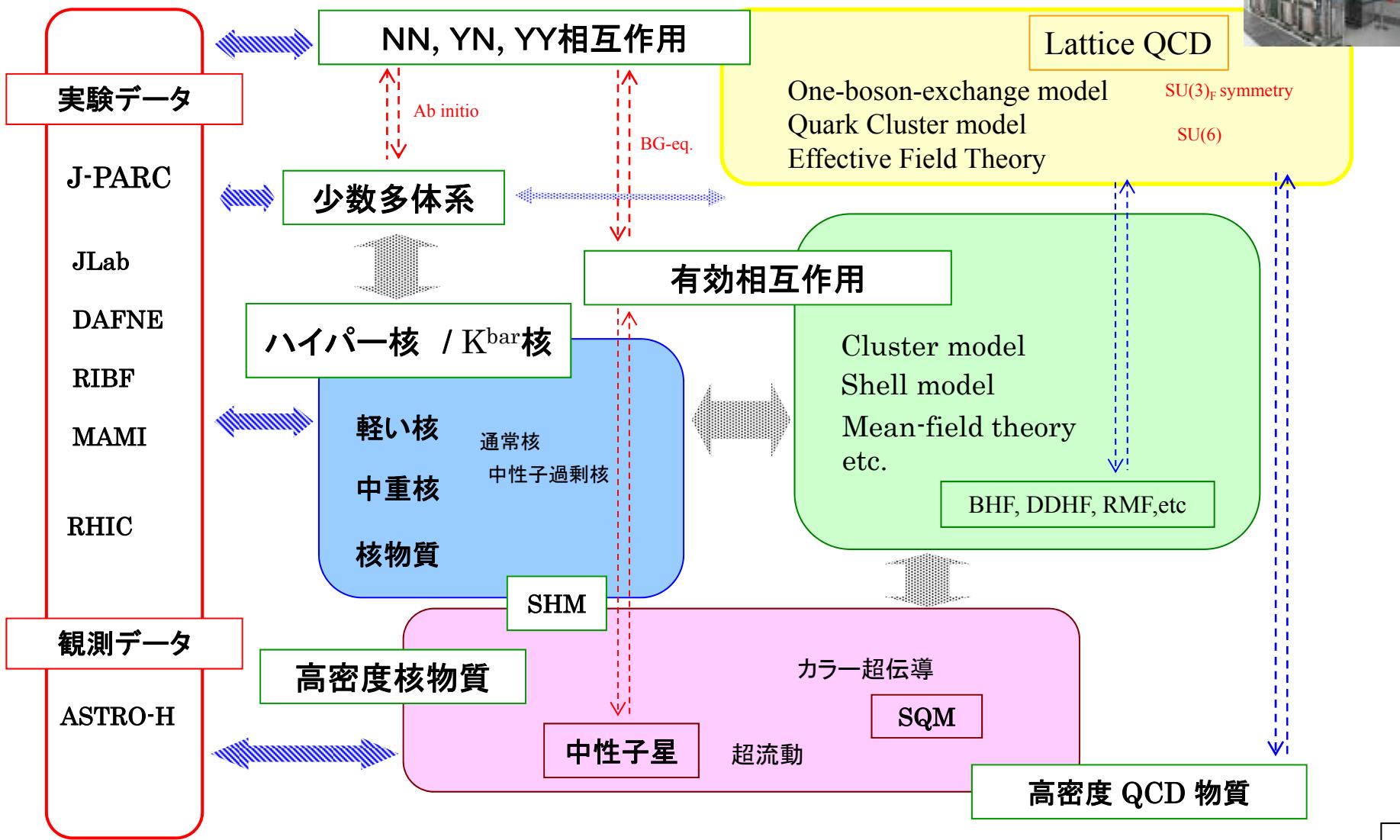
← Serious Problems from hyperon-mixing (Takatsuka)



ストレンジネス核物理の展開

by E.Hiyama

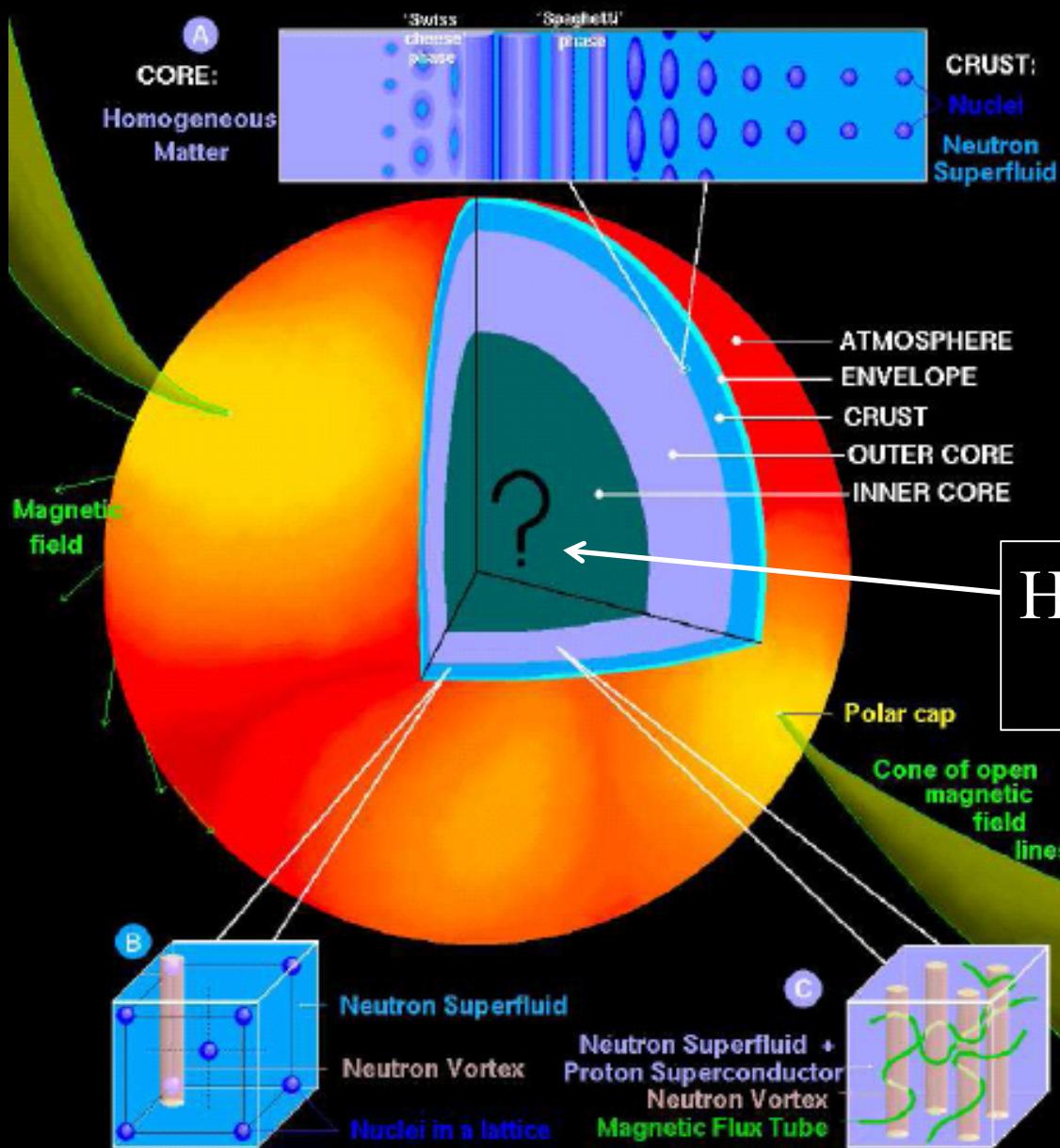
“QCD,核力から核構造へ”と“核構造からQCD,核力へ”



中性子星物質とハイペロン

by J.M. Lattimer, M. Prakash,

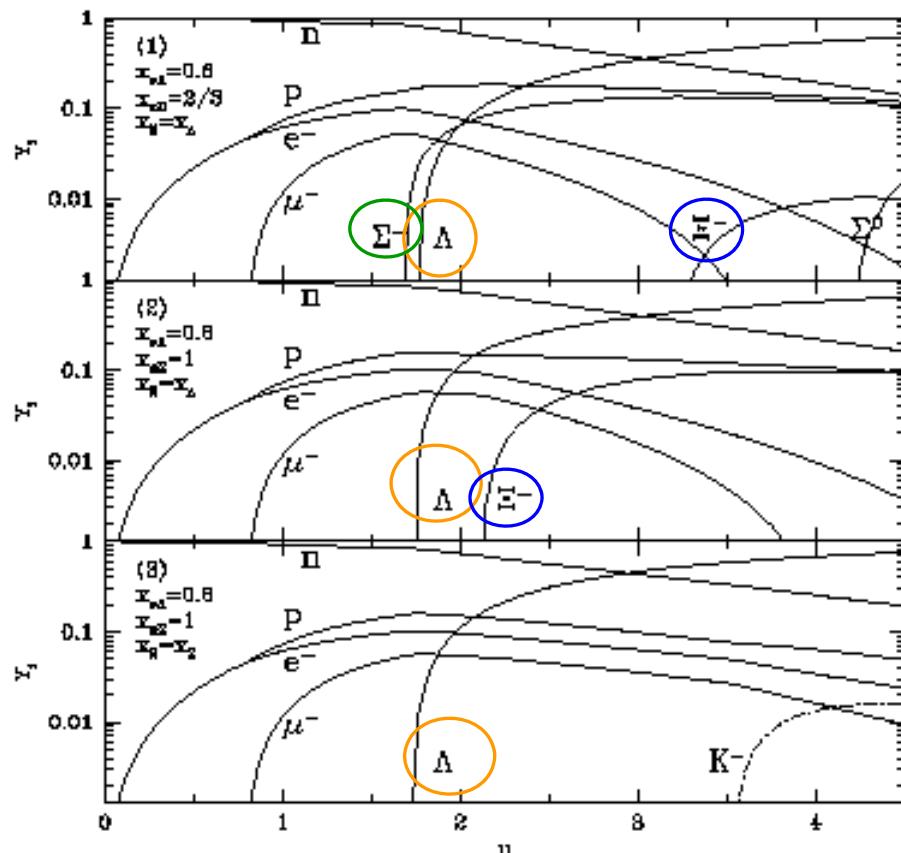
A NEUTRON STAR: SURFACE and INTERIOR



Neutron star core

= “An interesting neutron-rich hypernuclear system”

Coupling constant ratio; $x_{iY} = g_{iY}/g_{iN}$ ($i=\sigma,\omega,\rho$)



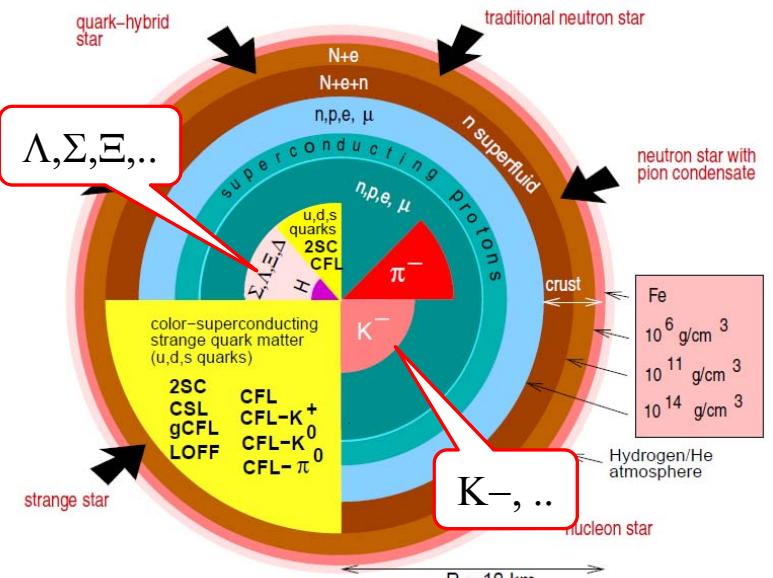
[R. Knorren, M. Prakash, P.J.Ellis, PRC52(1995)3470]

Hyperon-mixing

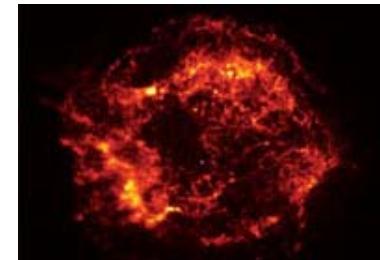
$$U_\Sigma < 0 \\ U_\Xi < 0$$

$$U_\Sigma > 0 \\ U_\Xi < 0$$

$$U_\Sigma > 0 \\ U_\Xi > 0$$

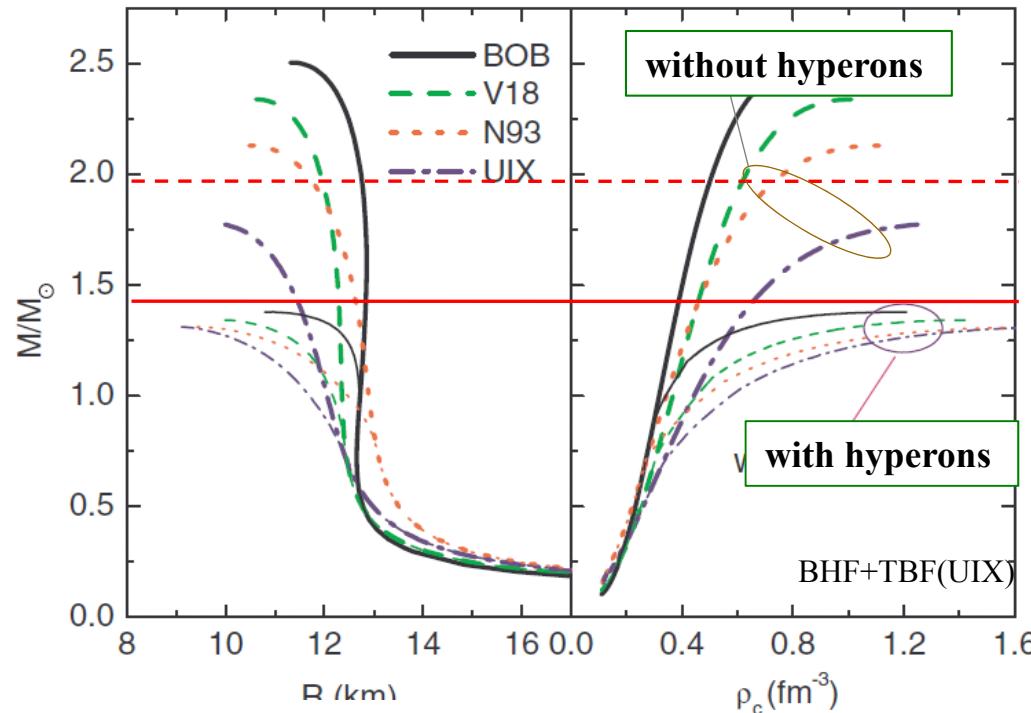


[F. Weber, PPNP 54(2005)193]



Cassiopeia A nebula
NASA/CXC/SAO.

Hyperons and massive neutron stars



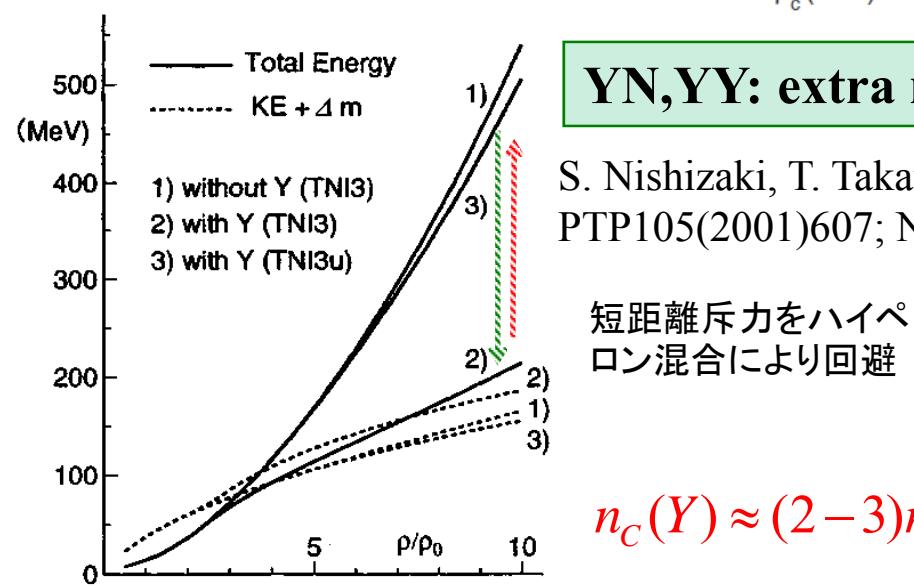
Z.H.Li, H.-J.Schulze,
PRC 78 (2008) 028801

$1.97 M_{\text{sun}}$ ← PSR J1614-2230

$1.44 M_{\text{sun}}$ ← P. B. Demorest et al.,
Nature 467(2010)1081

Maximum Mass/Radius

Softening on the EOS

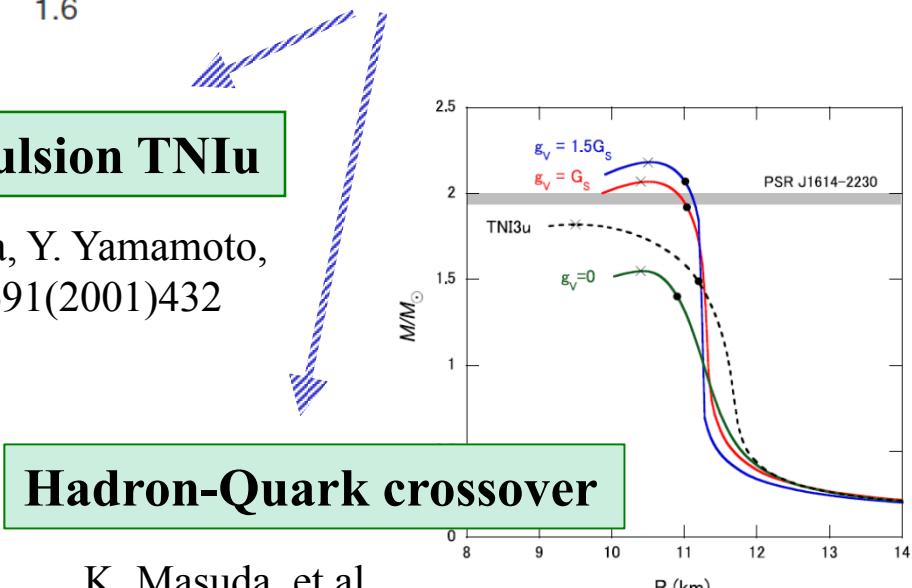


YN,YY: extra repulsion TN1u

S. Nishizaki, T. Takatsuka, Y. Yamamoto,
PTP105(2001)607; NPA691(2001)432

短距離斥力をハイペ
ロン混合により回避

$$n_C(Y) \approx (2-3)n_0$$

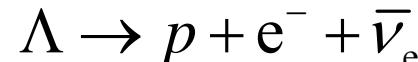


Hadron-Quark crossover

K. Masuda, et al.,
arXiv:1205.3621v2 [nucl-th]

Thermal evolution of neutron stars

Rapid neutrino emission
via weak processes
(Direct/Modified Urca)



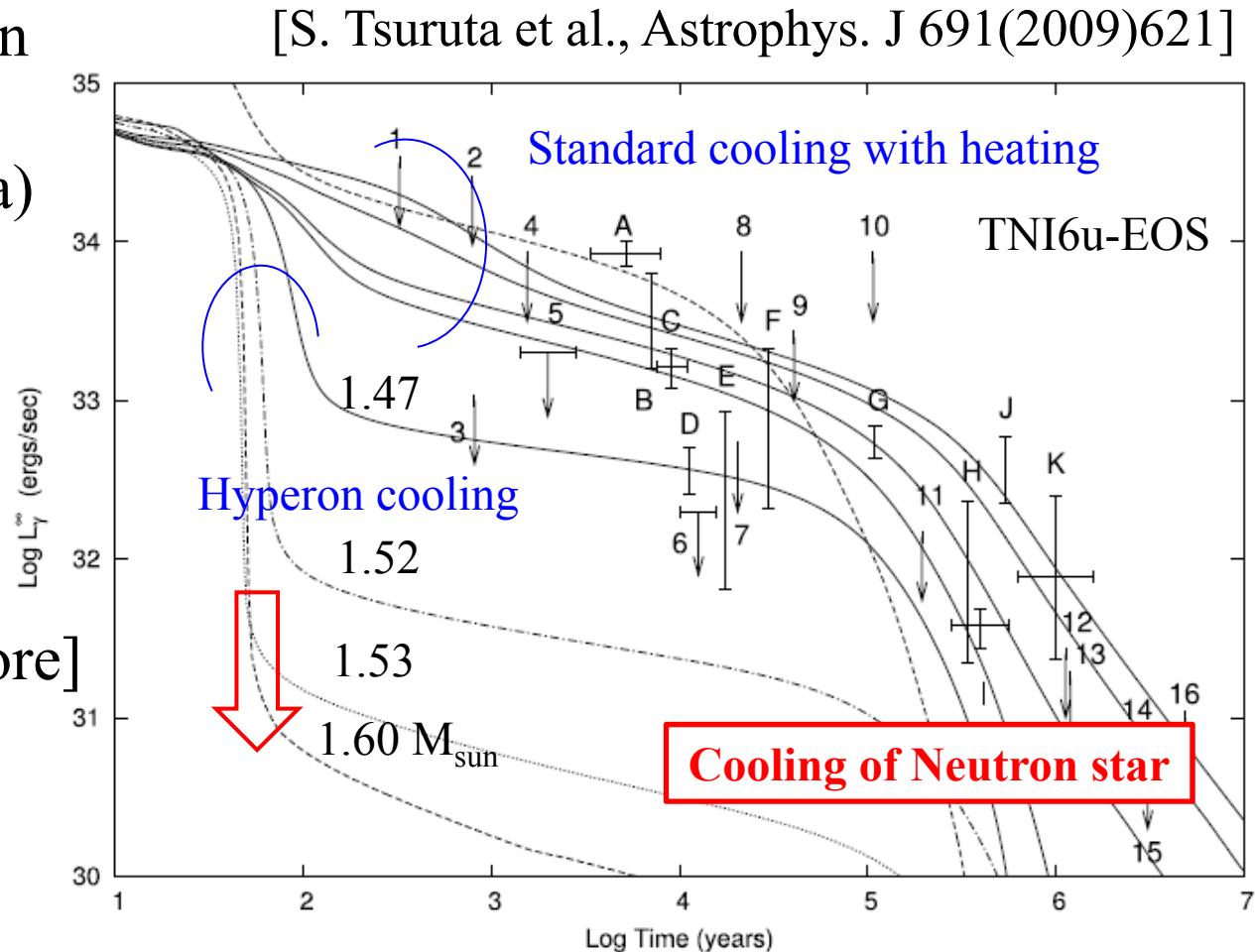
- Cooper pair
 1S_0 [inner crust]
 $^3P_2 - ^3F_2(n), ^1S_0(p)$ [core]
→ Standard cooling

- YY pairing
→ Hyperon cooling
Cooling relaxation?

- Hyperon superfluidity v.s. YY interactions
Nagara event $\Delta B_{\Lambda\Lambda} \sim 0.67$ MeV → no $\Lambda\Lambda$ superfluidity ?



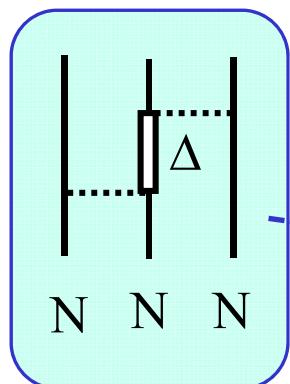
very sensitive to properties of YN, YY interactions



Dynamics in Strangeness Nuclear Systems

Fujita-Miyazawa

3BF



~ 300 MeV

Nuclei

$S = 0$

NN —

$N\Sigma$ —

NA —
 ~ 72 MeV

$\Lambda N-\Sigma N$ coupling

$S = -1$

$S = -2$

Hypernuclei

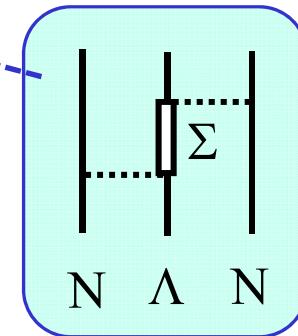
$\Sigma\Sigma$ —

$\Lambda\Sigma$ —

$N\Xi$ —
 $\Lambda\Lambda$ —
 ~ 28 MeV



$\Xi N-\Lambda\Lambda$ coupling
very large ?



Strong ΛNN 3BF ?

- Various effects on the hyperon mixing
- Related to the 3BF in nuclei

ハイペロン-核子間相互作用

■ One-Boson-Exchange model

➤ Nijmegen potential

NHC-D/F → NSC89 → NSC97e,f → ESC04a-d →

ESC06 → ESC08a-c [Th.A. Rijken, M. M. Nagels, Y. Yamamoto, PTPS185(2010)14]

➤ Funabashi-Gifu potential

[I. Arisaka et al., PTP104(2000)995]

■ Quark Cluster model

➤ Kyoto-Niigata potential

RGM-F → FSS → fss2 [Y. Fujiwara et al, PRC54(1996) 2180; PPNP58 (2007)439]

■ Chiral LO Effective Field Theory

➤ Julich potential

[H. Polinder, et al., NPA779 (2006) 244; PLB653 (2007) 29]

■ Lattice QCD

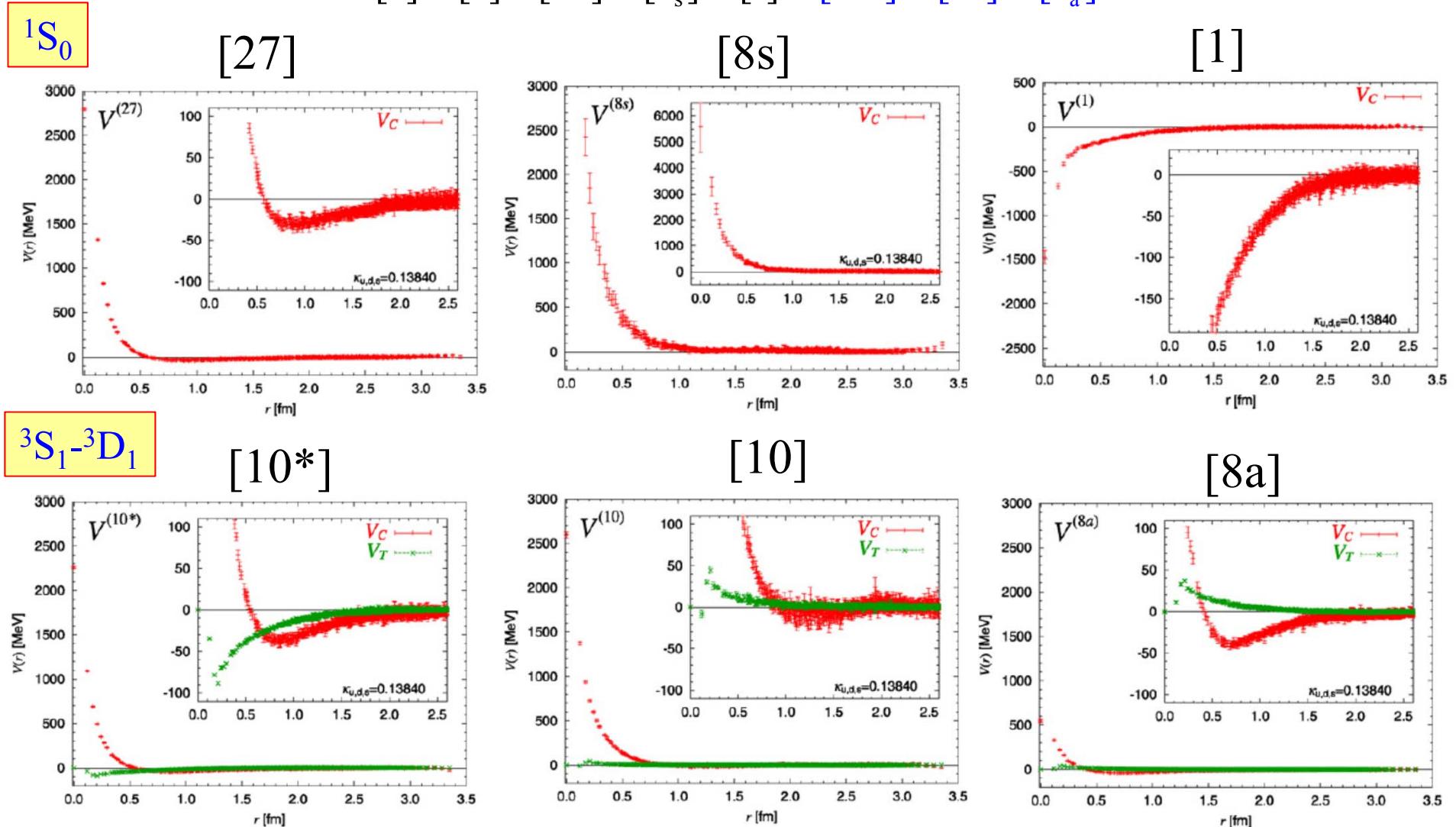
➤ HAL QCD Collaboration

[H. Nemura, et al., PLB 673 (2009) 136; T. Inoue, et al., PTP124 (2010) 591;
PRL106 (2011) 162002]

Baryon-Baryon force in SU(3) basis from lattice QCD

T. Inoue et al., HAL QCD Collaboration, NPA881 (2012) 28.

$$[8] \otimes [8] = [27] \oplus [8_s] \oplus [1] \oplus [10^*] \oplus [10] \oplus [8_a]$$



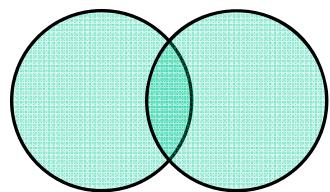
- at the $SU(3)_F$ limit corresponding to $M\pi = MK = 837$ MeV.
- possibility of a bound H-dibaryon in the limit.

Short-range repulsive core in baryon-baryon interaction

Spin-flavor SU(6) symmetry

Quark Cluster Model

Quark-exchange
(anti-symmetrized)



M.Oka,K.Shimizu,K.Yazaki, PLB130(1983)365; NPA464(1987)700

symmetric

antisymmetric

$$[3] \otimes [3] = [6] \oplus [42] \oplus [51] \oplus [33]$$

orbital x flavor-spin x color singlet

$\downarrow L=0$

Pauli forbidden state

S = 0 state

[51]

[33]

1

$\Lambda\Lambda$ - $\Xi\bar{N}$ - $\Sigma\Sigma$ (I=0), H-dibaryon

8_S

1

ΣN (I=1/2, 1S_0) *Pauli forbidden*

27

4/9

5/9

NN(1S_0)

S = 1 state

[51]

[33]

8_A

5/9

4/9

E40@J-PARC: $\Sigma^+ p$ Scattering

10

8/9

1/9

ΣN (I=3/2, 3S_1)

almost Pauli forbidden

10*

4/9

5/9

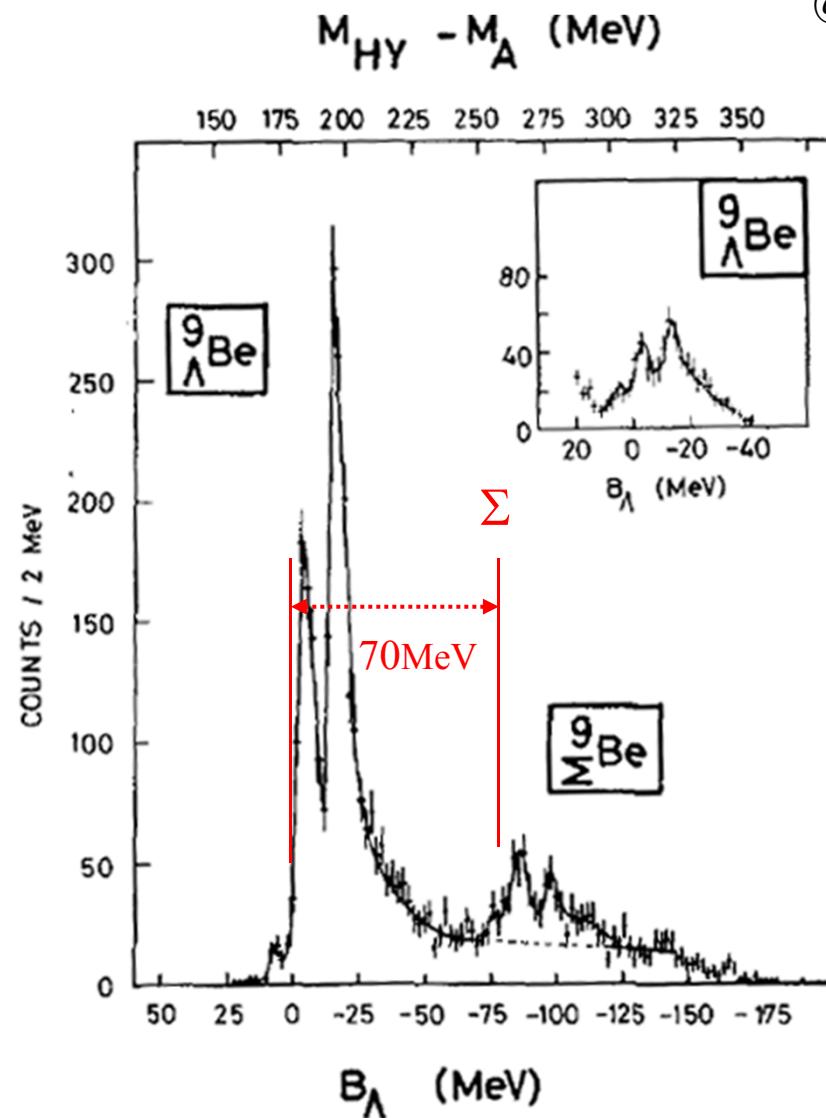
NN(3S_1), ΛN - ΣN (I=1/2, 3S_1)

➤ SU(6)sp symm. → Strongly spin-isospin dependence

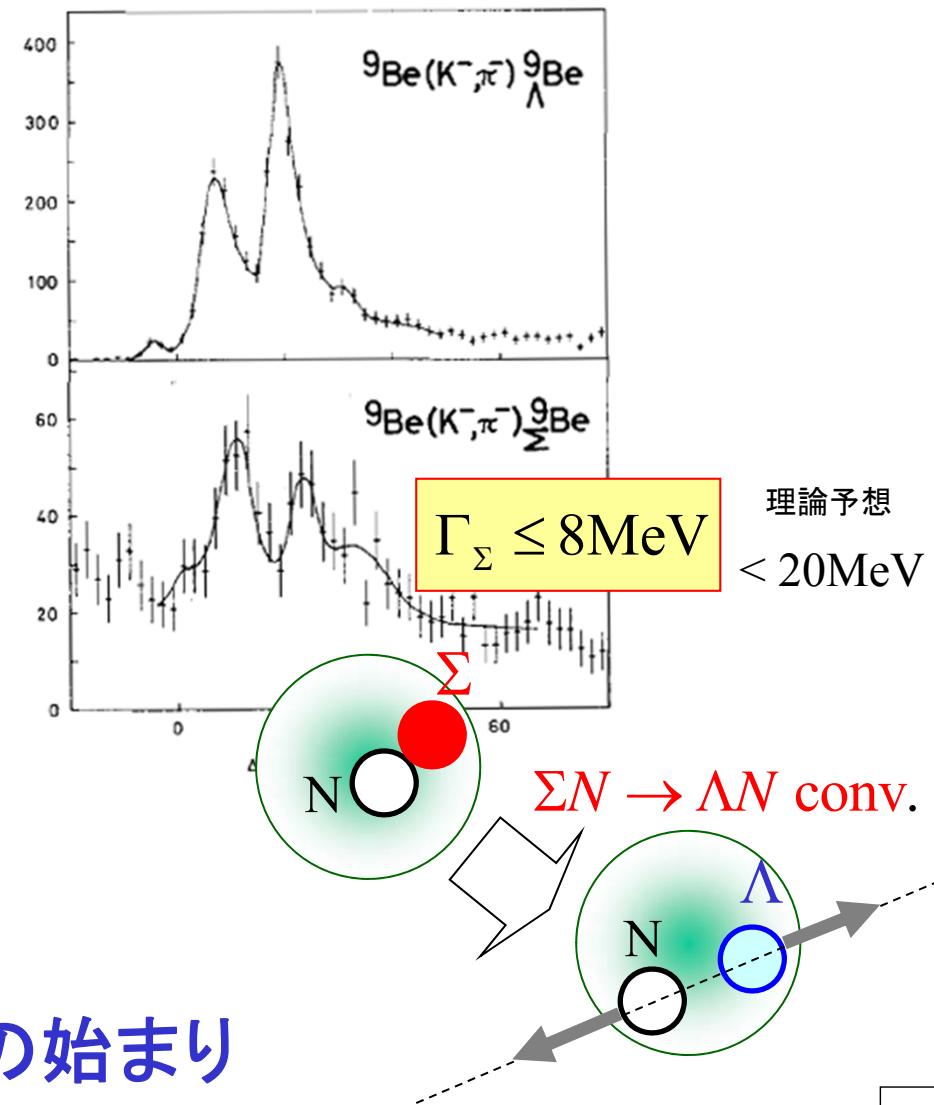
2. Σ ハイパー核

Searching for Sigma-Hypernuclei (1980-)

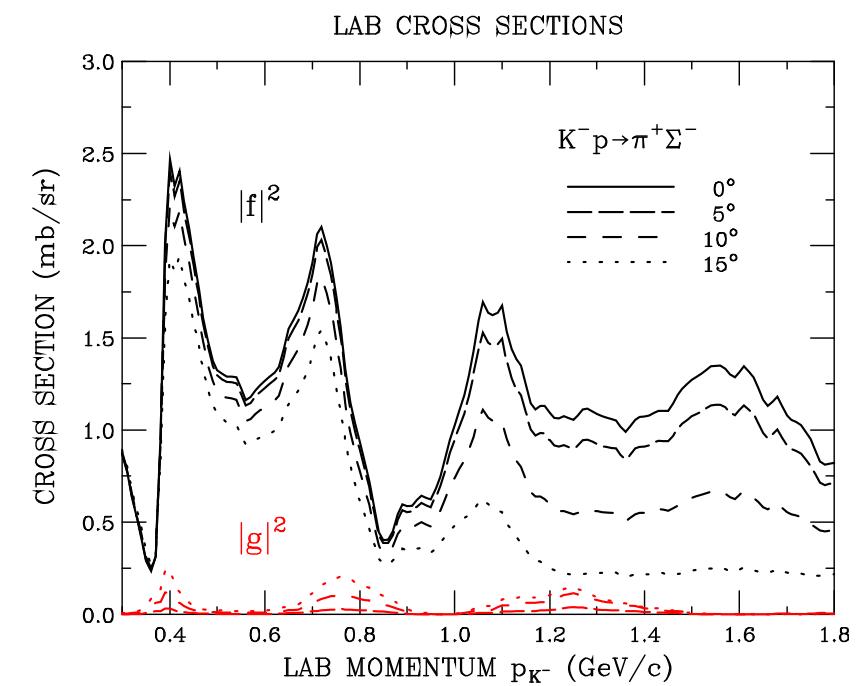
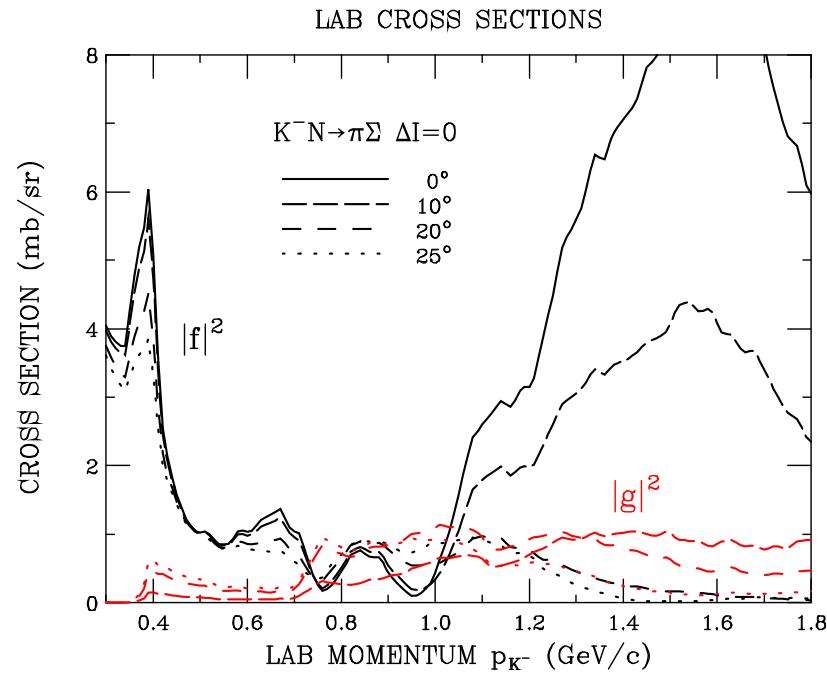
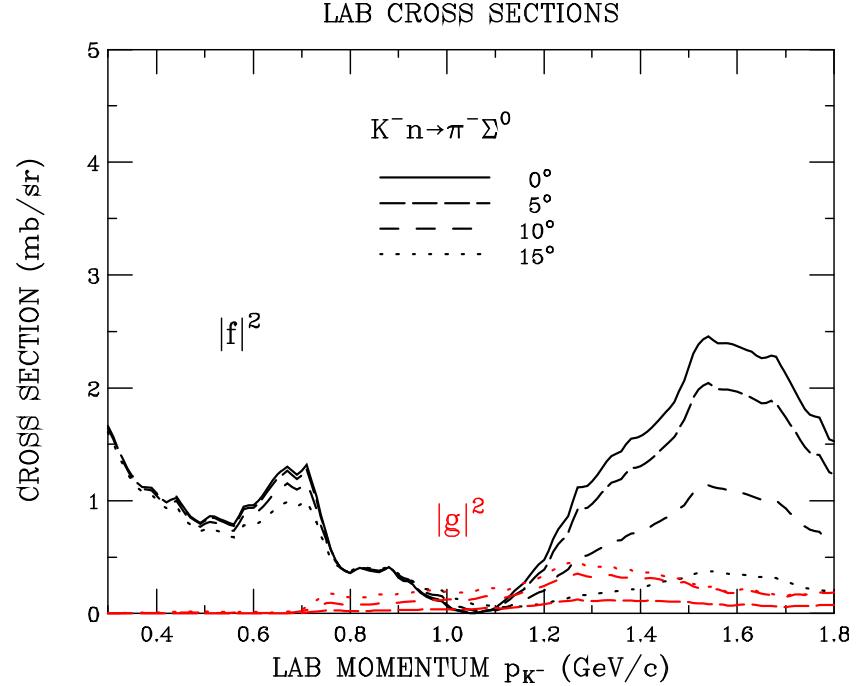
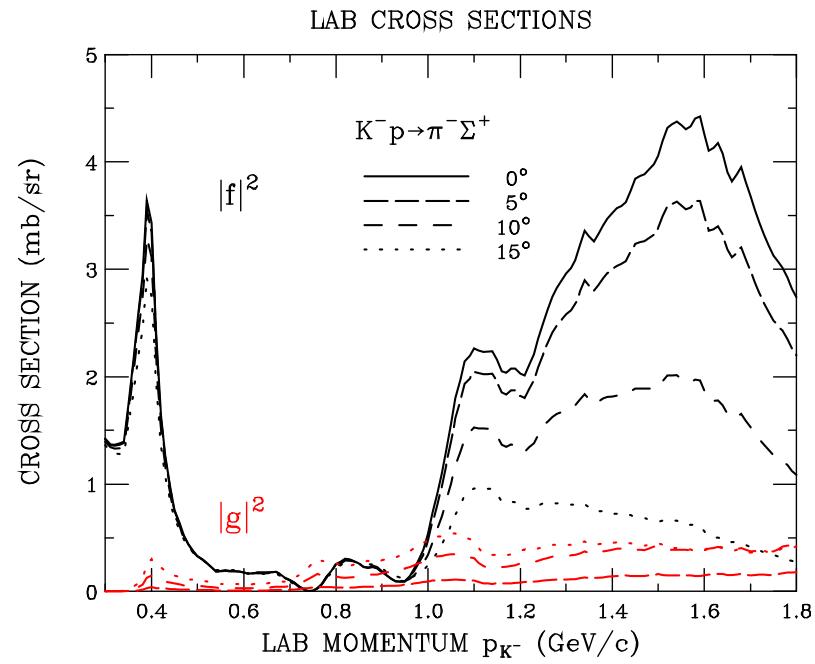
@CERN-PS, 720 MeV/c (0deg.)



R.Bertini al., PB90(1980)375

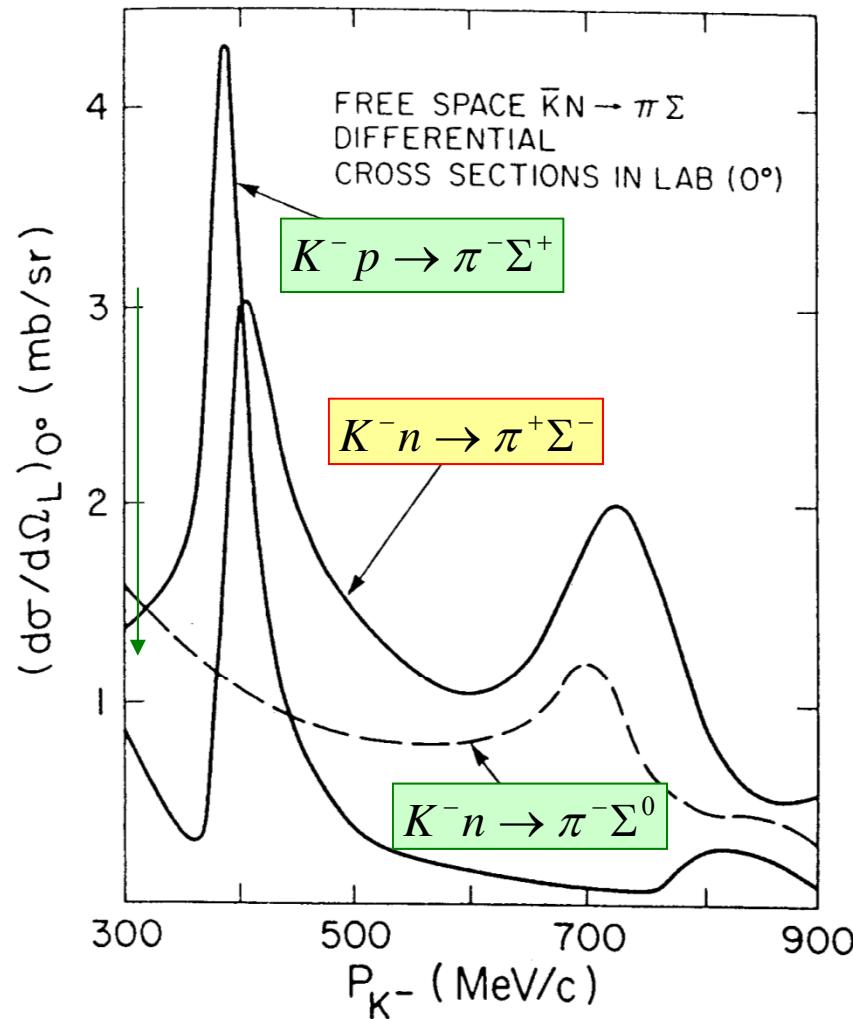


“狭い幅の状態”的問題の始まり

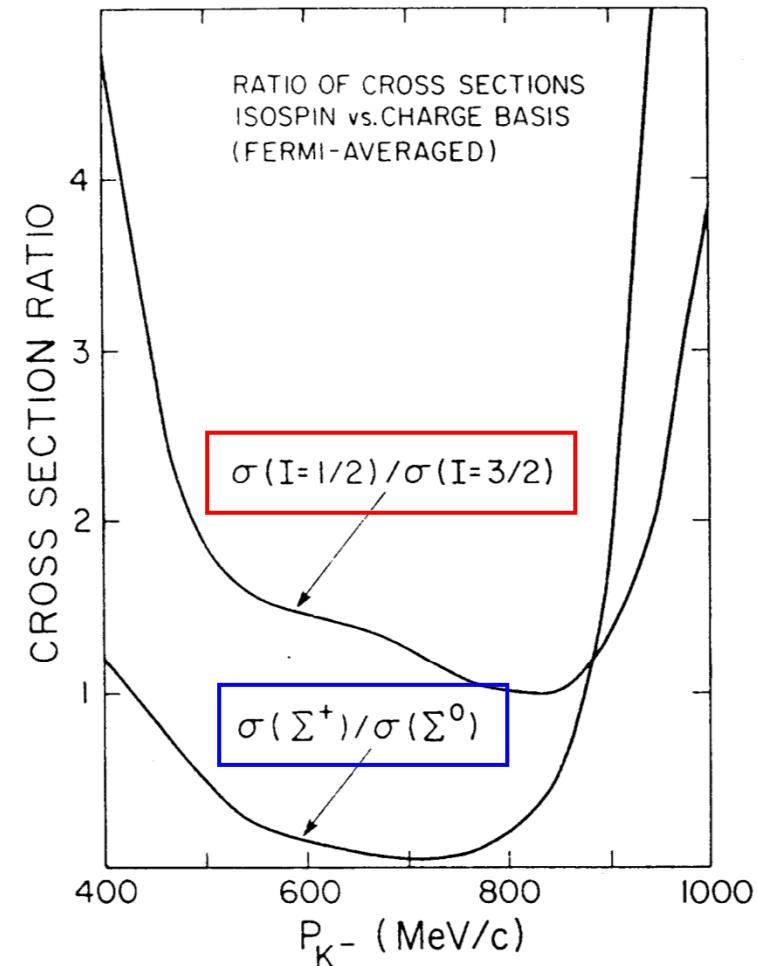


Elementary (K^- , π^\pm) reactions

$$\left[\frac{d\sigma}{d\Omega_L} \right]_{\text{elem}}$$

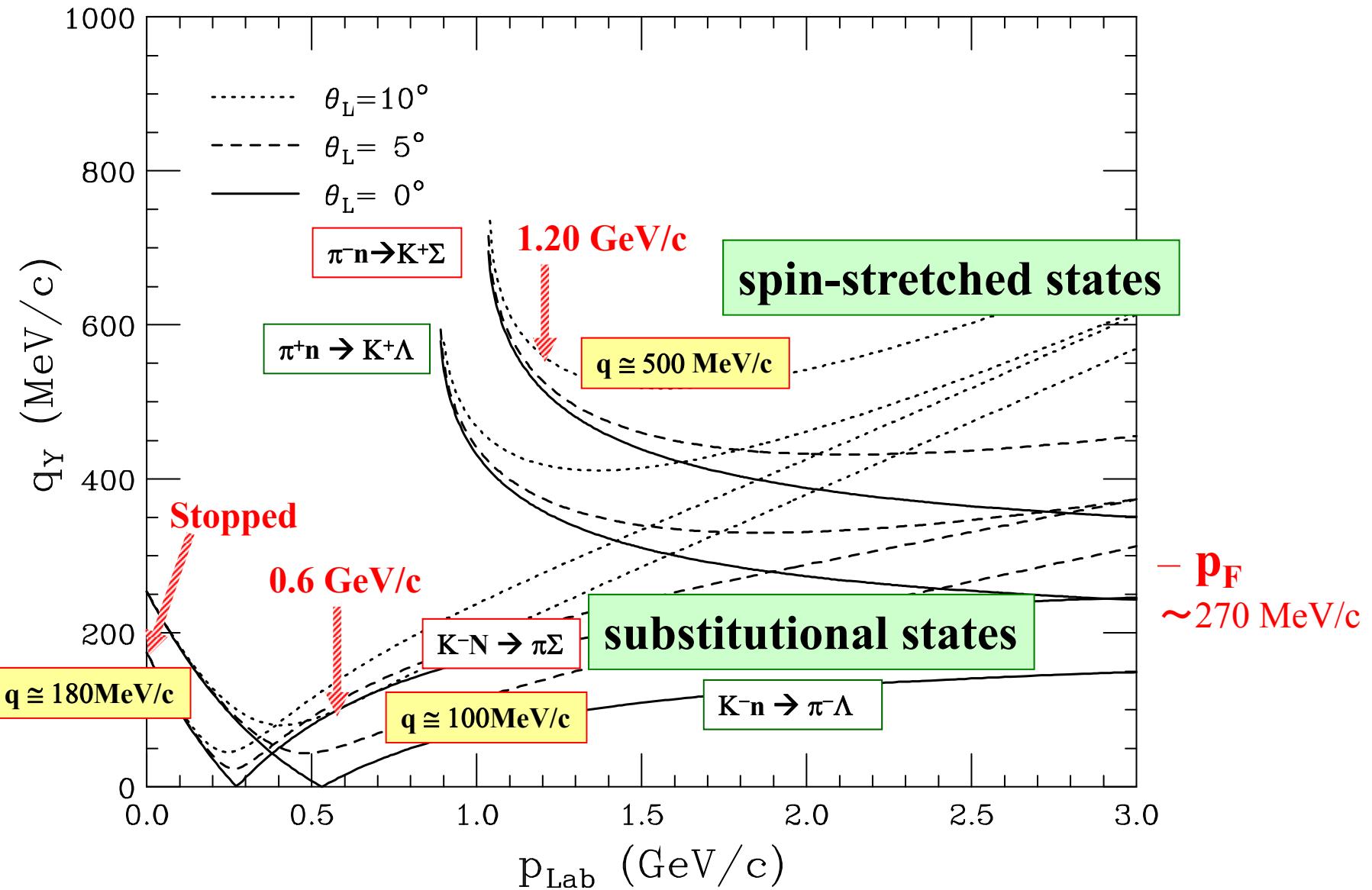


G.P.Gopal et al., NPB119(1977)362.



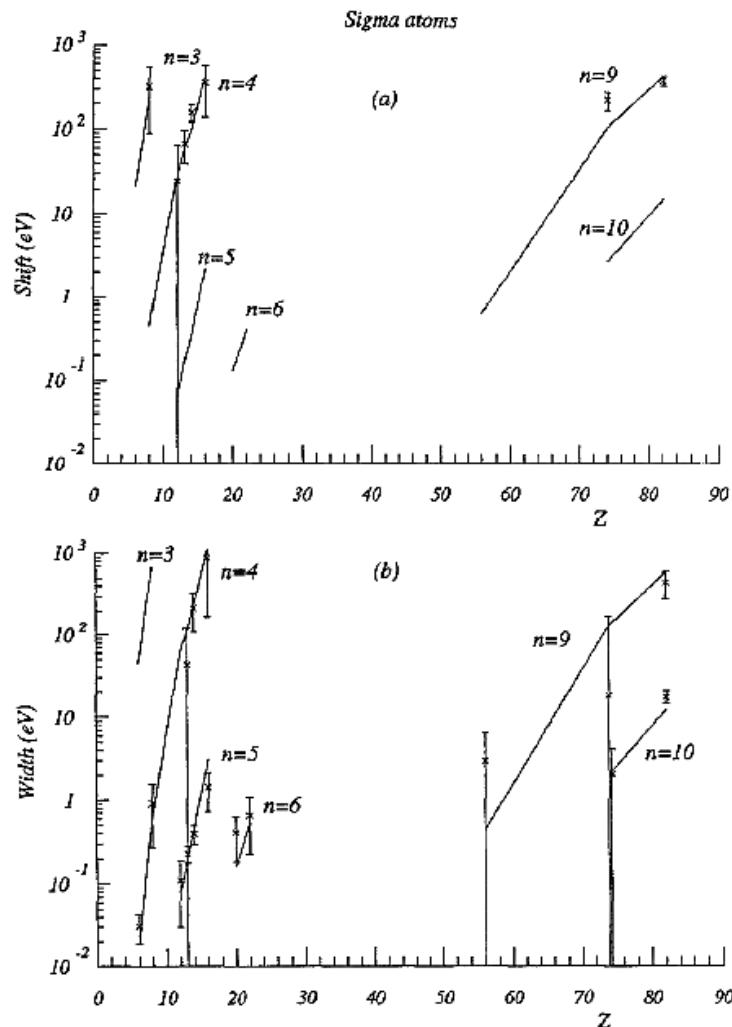
C.B.Dover, D.J.Millener and A.Gal, Phys. Rep.184(1989)1.

Momentum transfer to Λ , Σ -hyperons



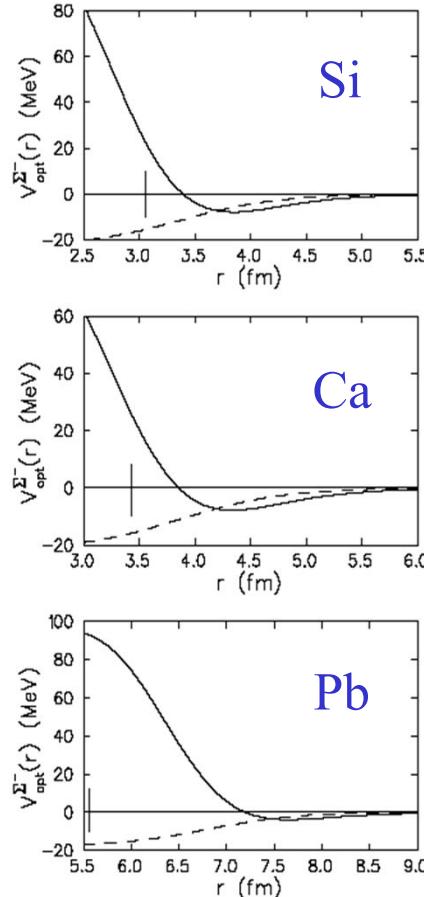
Σ^- 原子のx線データと Σ^- -原子核間ポテンシャル

C.J.Batty et al., Phys.Rep.287(1997)385



RMF

J. Mares et al., NPA594(1995)311



LDA+YNG-F

J. Dabrowski, Acta Phys. Pol. B31(2001)2179

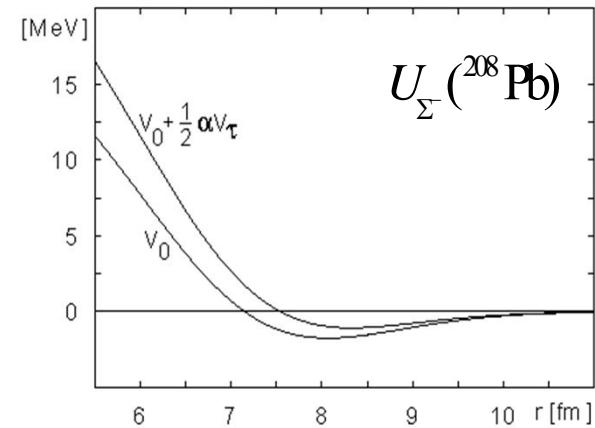


Fig. 2. Potential V_{Σ^-} in ^{208}Pb .



- Repulsive core + attractive tail
- Laneポテンシャルは斥力的
- NHC-Fが良い？

Only 23 measurements !!

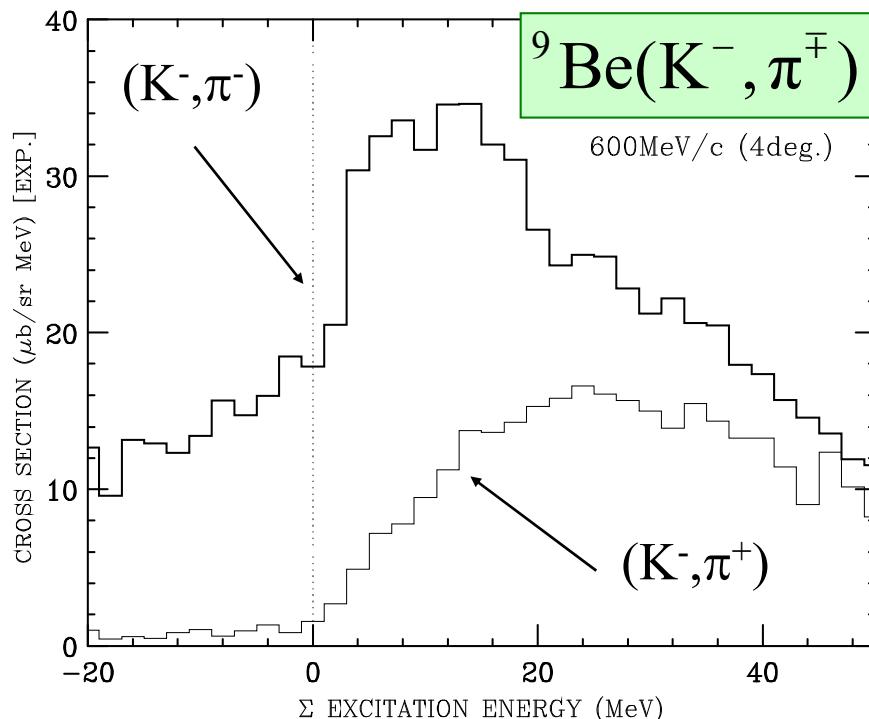
NSC97a-f のLane項は引力で不適！

J. Dabrowski, PRC61(1999)025802

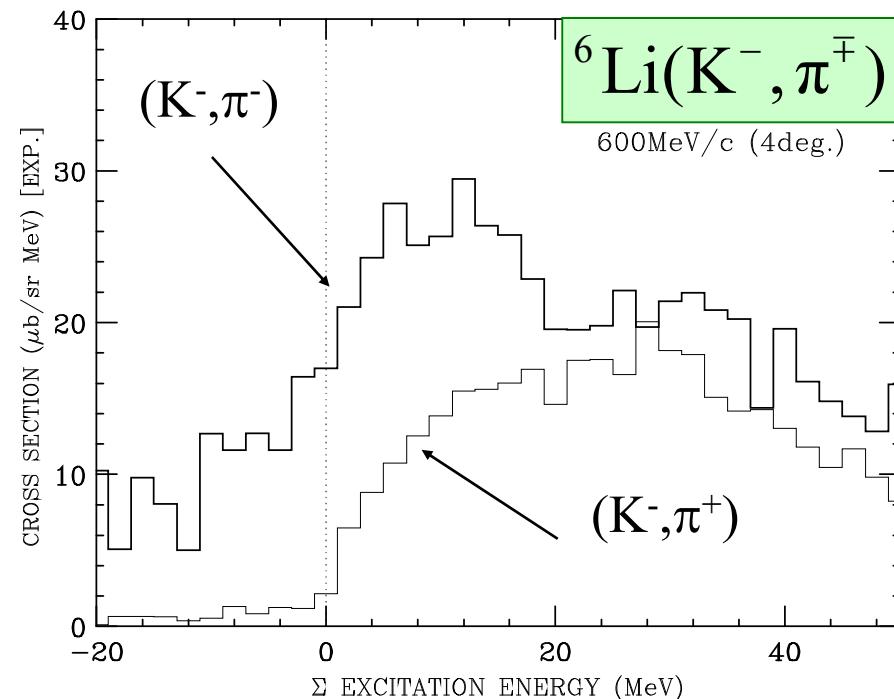
(K^-, π^\pm) Experiments at BNL-AGS 600MeV/c (4deg.)

“狭い幅の状態の問題”的終焉 (-1999)

高統計のデータ



S.Bart et al., PRL83(1999)5238



- There is no Σ bound state on both ${}^6\text{Li}$ and ${}^9\text{Be}$.
- The π^- and π^+ spectra are very different each other.

→ Strong isospin dependence of the Σ -nucleus potentials

シグマハイパー核の諸問題(1980s-)

- シグマハイパー核は存在するのか？

狭い幅の状態の問題は?

CERN, BNL, KEK

$\Sigma N(T=1/2, {}^3S_1)$ の束縛状態は？

ANL, BNL

A=4の束縛状態の存否は?

KEK, BNL

- Σ ポテンシャルは引力か斥力か？

シグマ原子のX線データ v.s.

(π^-, K^+) 反応によるシグマ生成スペクトル

KEK

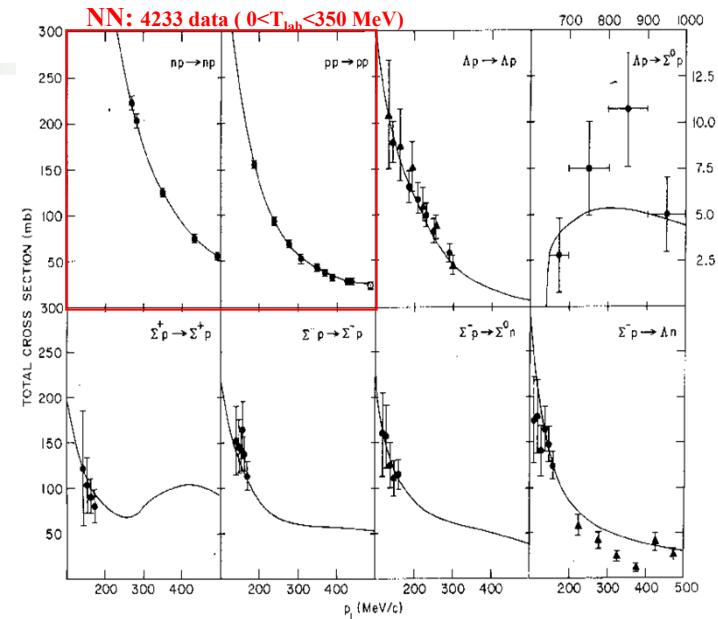
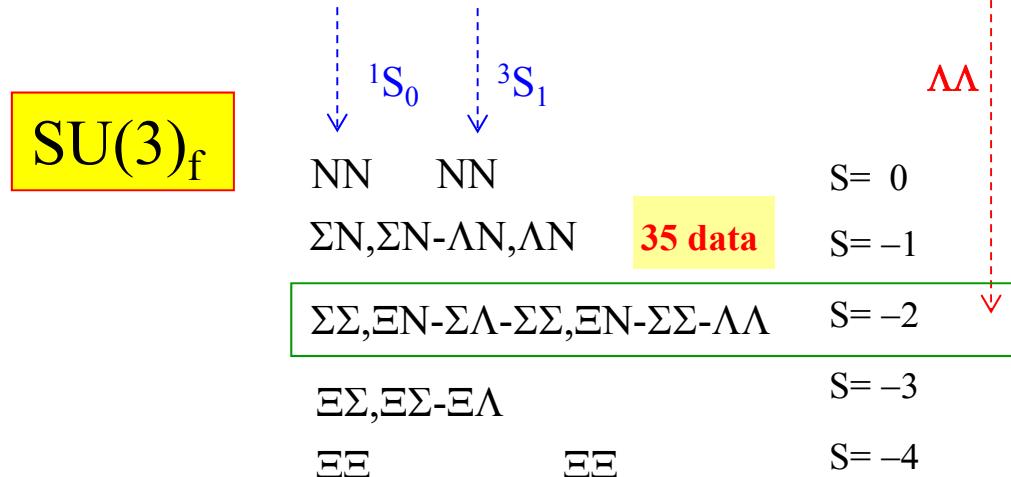
- ラムダ核における Σ 混合の割合は？

- アイソスピンは良い量子数か？

- スピン-軌道力の大きさは？

NN, YN interactions

$$\{8\} \otimes \{8\} = \{27\} \oplus \{10^*\} \oplus \{10\} \oplus \{8\}_s \oplus \{8\}_a \oplus \{1\}$$



C.B. Dover and H. Feshbach, Ann. Phys. 198(1990)321

Nijmegen soft-core potential

NHC-D \rightarrow NSC89 \rightarrow NSC97 \rightarrow ESC04a-d
NHC-F a-f ESC08

Th.A. Rijken, V.G.J. Stoks, Y. Yamamoto, PRC59(1999)21

V.G.J. Stoks, Th.A. Rijken, PRC59(1999)3009

Th.A. Rijken, Y. Yamamoto, PRC73(2006)044008

One-Boson-Exchange model

Funabashi-Gifu potential

I. Arisaka, K. Nakagawa, S. Shinmura, M. Wada, PTP104(2000)995; FBS.Suppl.12(2000)395

Kyoto-Niigata potential

RGM-F \rightarrow FSS \rightarrow fss2

Quark Cluster model

T. Fujita, Y. Fujiwara, C. Nakamoto, Y. Suzuki, et al., FBS.Suppl.12(2000)399; PRC64(2001)054001

$K^-d \rightarrow \pi^-\Lambda p$ Reactions (1960s-1970s)

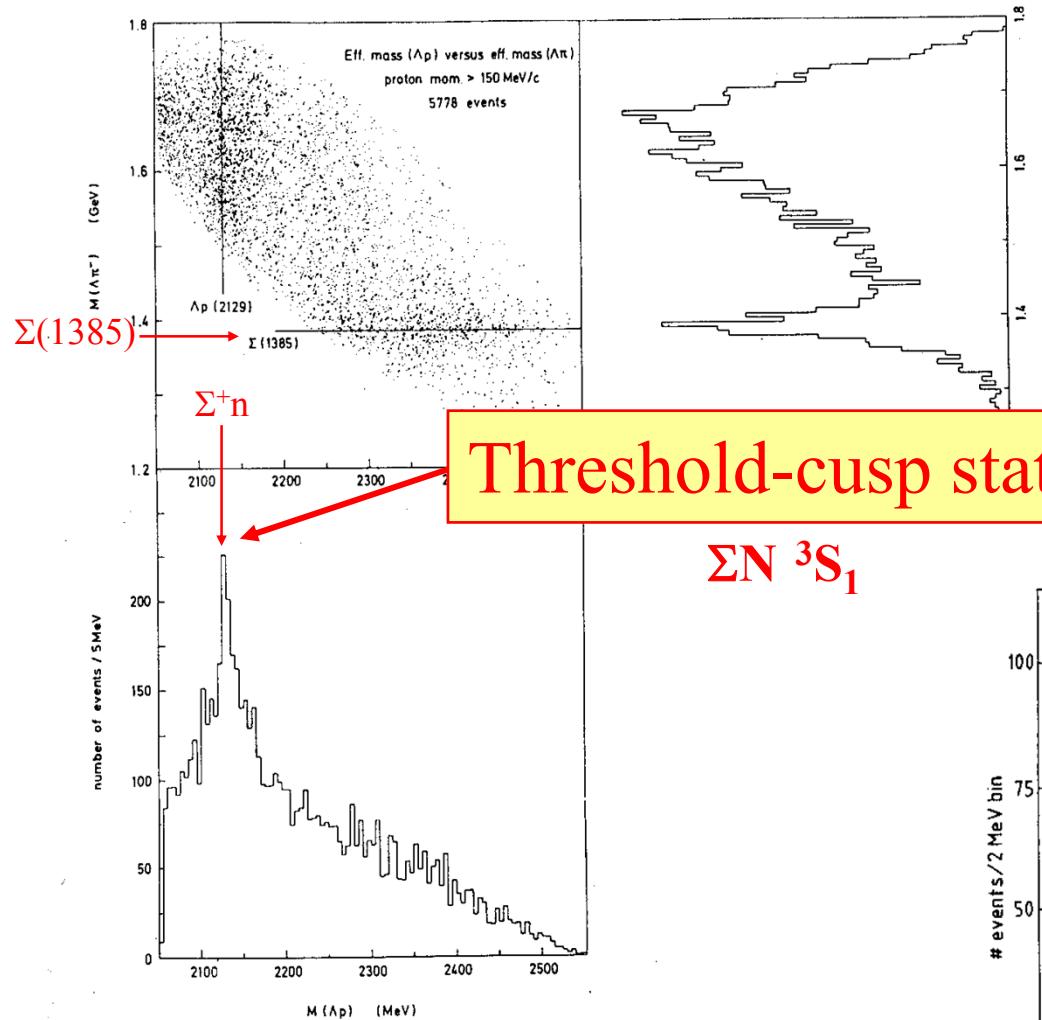
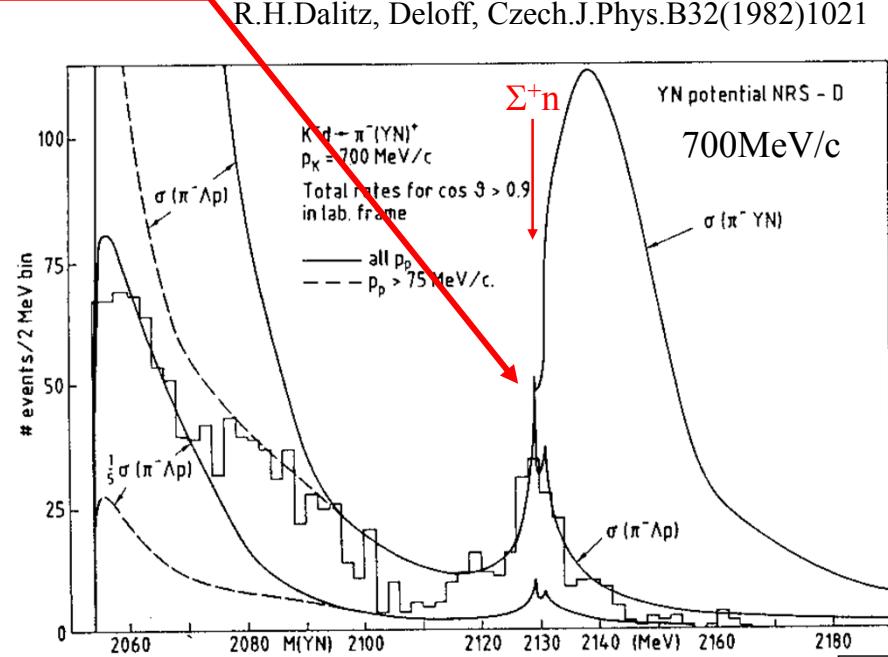


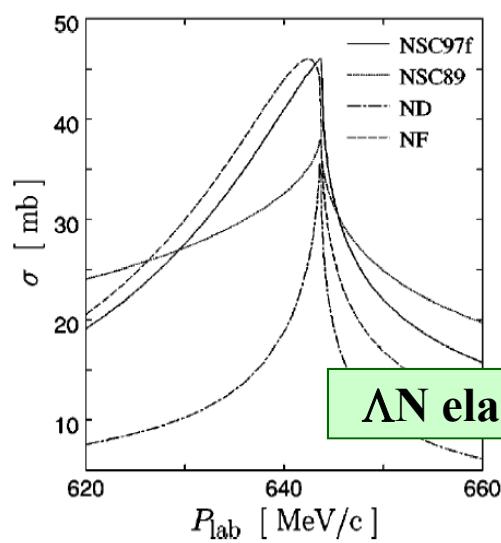
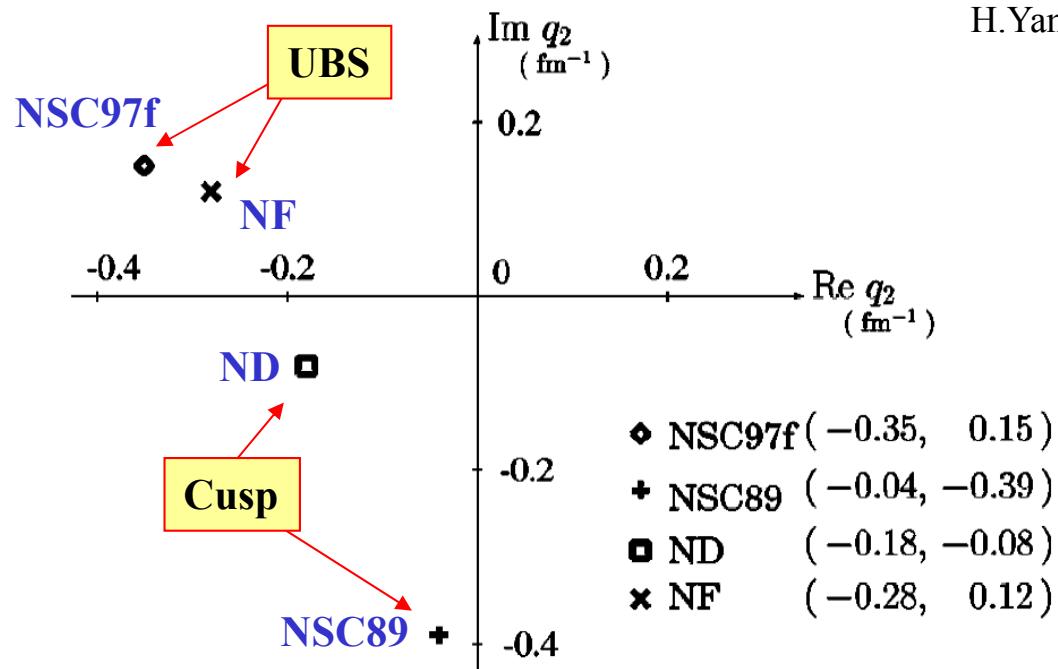
Fig. 1. Scatter diagram of the effective (Λp) mass *versus* the effective ($\Lambda\pi^-$) mass in the $K^-d \rightarrow \Lambda p\pi^-$.

T.H.Tan, PRL23(1969)395.
O.Braun et al., NPB124(1977)45.
D.Eastwood et al., PRD3(1971)2603.

- $S = -1$ dibaryon search
- YN interaction study
- (K^-, π) reaction study



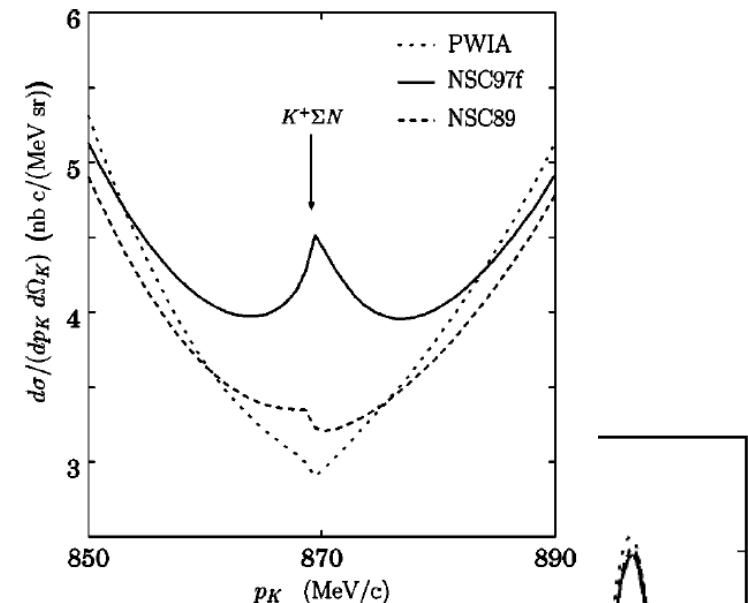
$d(\gamma, K^+)$ spectrum near the ΣN threshold



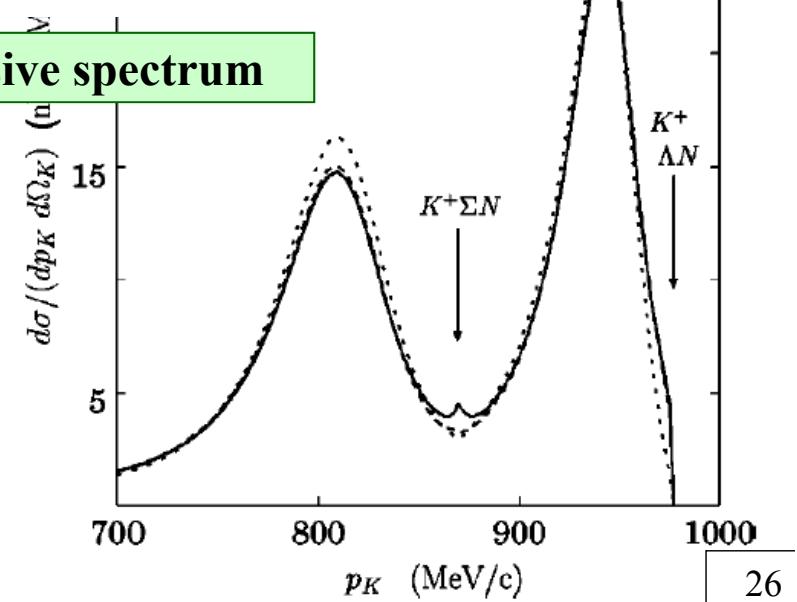
K. Miyagawa, H. Yamamura,
PRC60(1999)024003

ΛN elastic cross section

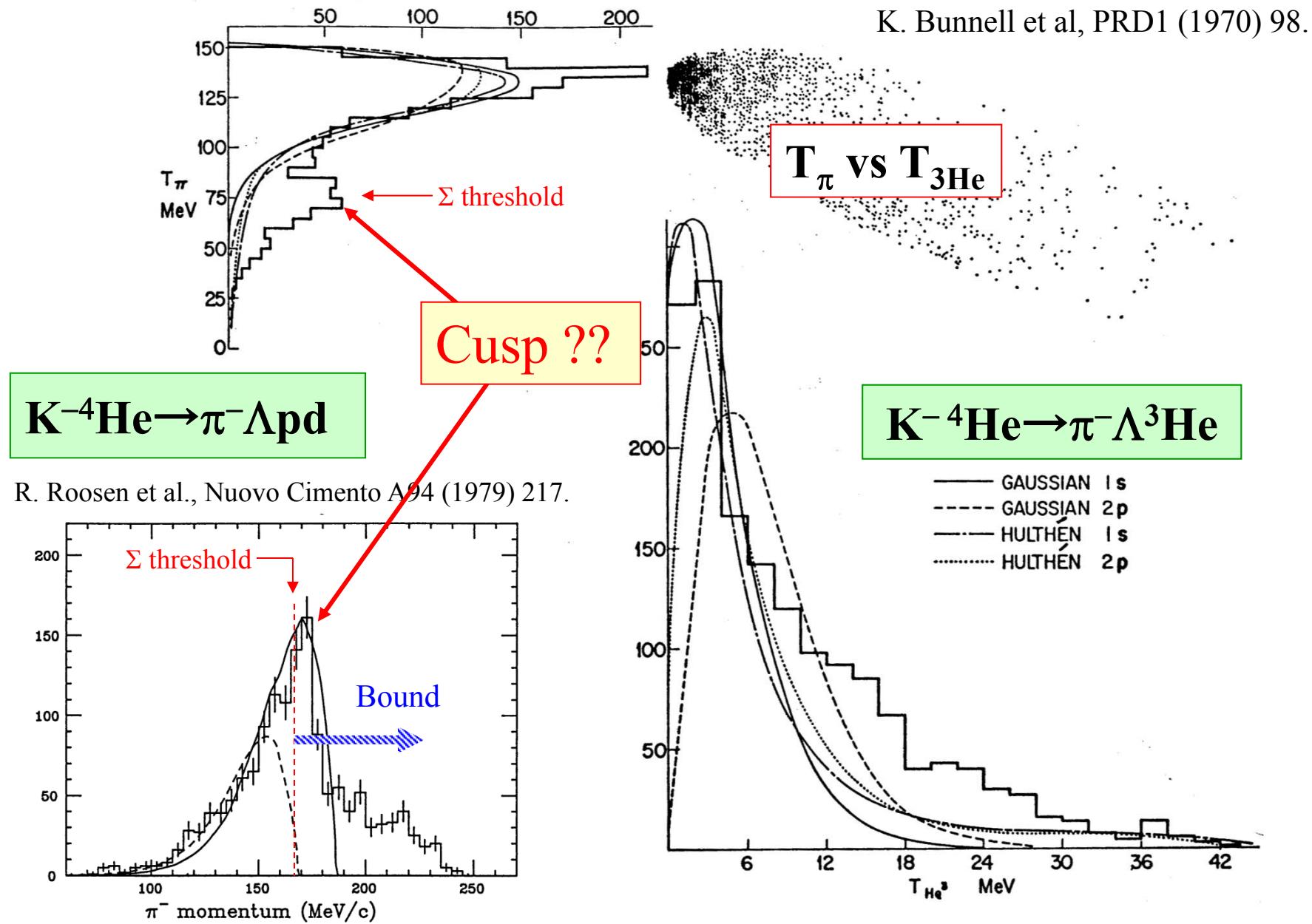
H.Yamamura, K. Miyagawa, et al., PRC61(1999)014001



$d(\gamma, K^+)$ inclusive spectrum



HeBC Study of K⁻He Interactions (1960s-1970s)



Σ ハイパー核の束縛状態の探索

•理論的予測 (1987-)

T.Harada, S.Shinmura, **Y.Akaishi**, H.Tanaka, NPA507(1990)715

•HeBC exp. at ANL (1970s)

• $^4\text{He}(\text{stopped K}^-, \text{p})$ exp. at KEK (1989)

• $^4\text{He}(\text{K}^-, \text{p})$ exp. at BNL (1992,1995)

•理論的解析 (-2000)

T.Harada, PRL80 (1998) 1605; NPA672 (2000) 181

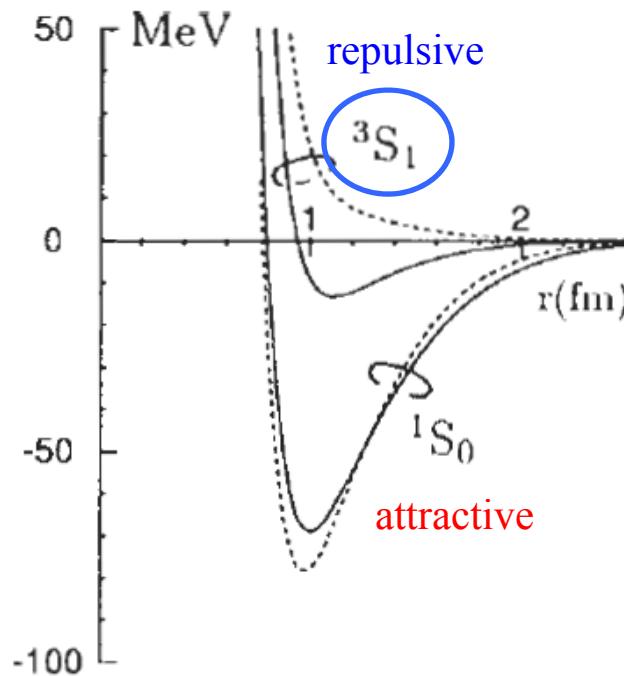
Two-body ΣN potentials in free space

Sigma-nucleon absorptive potential (SAP)

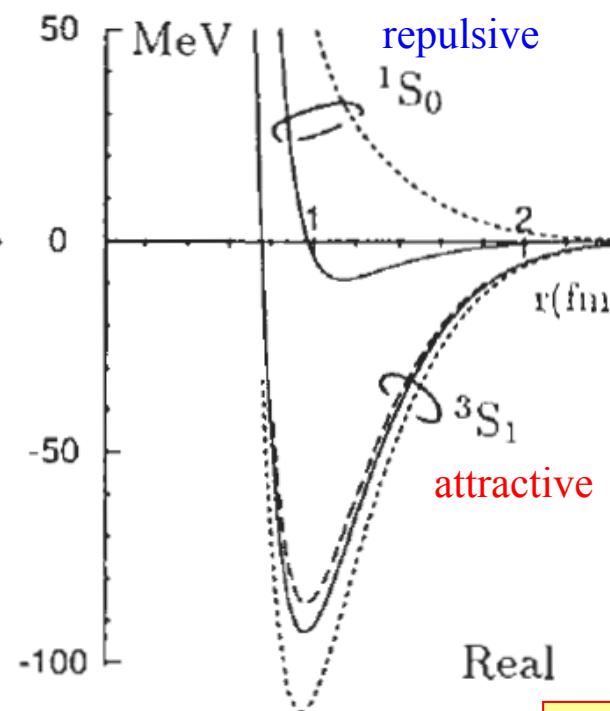
T.Harada, S.Shinmura, Y.Akaishi, H.Tanaka, NPA507(1990)715.

簡単であるが
特長を捉えや
すい

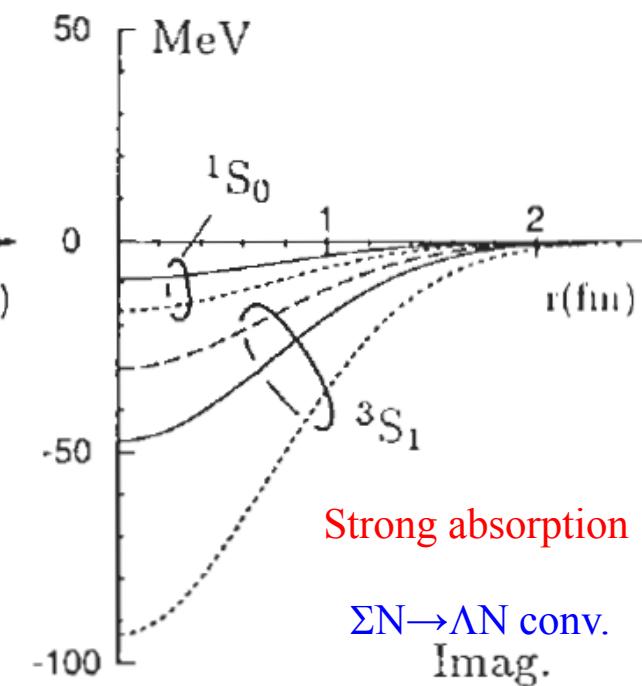
S-matrix equivalent to Nijmegen model-D (model-F)



$T=3/2$



$T=1/2$



$\Sigma N \rightarrow \Lambda N$ conv.
Imag.

Strong spin-isospin dependence

ハイペロン-原子核間ポテンシャルの導出

$$U(\mathbf{R}) = \langle \Phi_0 | V^{\text{ex}} \hat{F}^{\text{ex}} | \Phi_0 \rangle$$

$$\square \langle \Phi_0 | V^{\text{ex}} | \Psi^{\text{ATMS}} \rangle / \langle \Phi_0 | \Psi^{\text{ATMS}} \rangle$$

KAT Theory

Kurihara, Akaishi, Tanaka, PTP71(1984)561

$$V^{\text{ex}} = \sum_{ij} V_{ij}^{\text{ex}}$$

$$\hat{F}^{\text{ex}} = 1 + \sum_{(ij)} \frac{Q}{e} V_{ij}^{\text{ex}} \hat{F}_{ij}^{\text{ex}}$$

多重散乱理論

$$\hat{F}^{\text{ex}} = 1 + \sum_{(ij)} \frac{Q}{e} g_{ij} \hat{F}_{ij}^{\text{ex}} \quad Q = 1 - |\Phi_0\rangle \langle \Phi_0|$$

$$\hat{F}_{ij}^{\text{ex}} = 1 + \sum_{(kl)} \frac{Q}{e} g_{kl} \hat{F}_{kl}^{\text{ex}} \quad e = E - H^{\text{in}} - T_R$$

$$g_{ij} = V_{ij}^{\text{ex}} + V_{ij}^{\text{ex}} \frac{Q}{e} g_{ij}$$

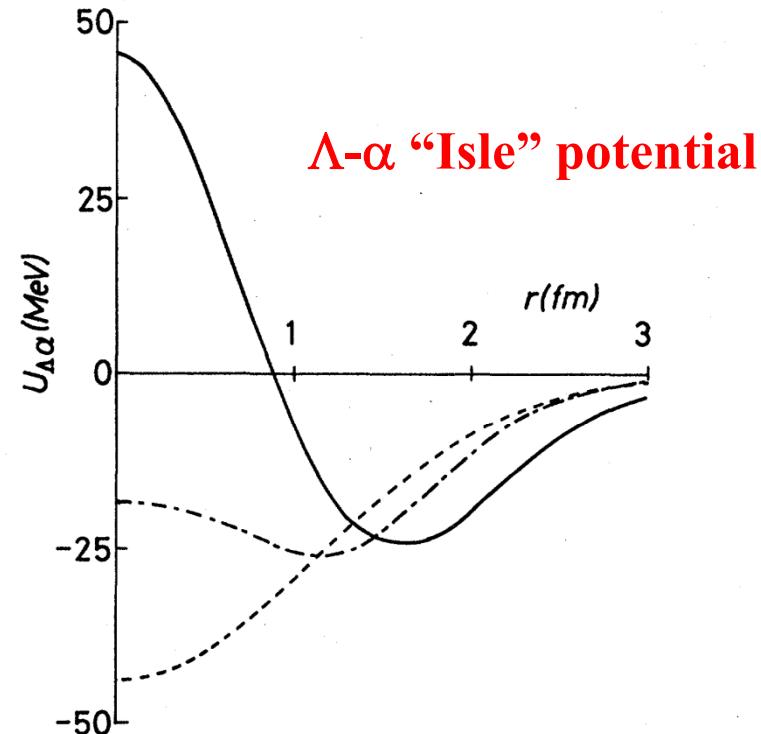


FIG. 1. Λ - α potentials. The solid, dashed, and dashed-dotted lines denote the isle, SG, and Maeda-Schmid (MS) (Ref. 7) potentials, respectively.

STRUCTURE OF THE $\frac{1}{2}^+ \text{He}$ HYPERNUCLEAR BOUND STATE

Toru HARADA, Shoji SHINMURA¹, Yoshinori AKAISHI and Hajime TANAKA²

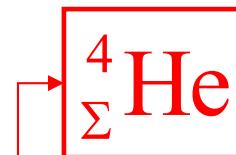
¹ Department of Physics, Hokkaido University, Sapporo 060, Japan

² Department of Applied Mathematics, Gifu University, Gifu 501-11, Japan

² Sapporo Gakuin University, Ebetsu 067, Japan

Received 20 April 1989

(Revised 18 September 1989)



1989
理論的予測

Abstract: The structure of $\frac{1}{2}^+ \text{He}$ is theoretically investigated on the basis of realistic ΣN interaction. The bound state has spin-parity $J^\pi = 0^+$ and isospin $T \sim \frac{1}{2}$ (99%), binding energy $B_{\Sigma^+} = 3.7\text{-}4.6 \text{ MeV}$ and a narrow $\Sigma N \rightarrow \Lambda N$ conversion width of $\Gamma = 4.5\text{-}7.9 \text{ MeV}$, which are in agreement with experimental data obtained at KEK. The existence of the Σ bound state with such a narrow width is explained from characteristic properties of the nucleus- Σ potential derived from the microscopic four-body calculation.

NN pot.: C3G

Tamagaki

ATMS

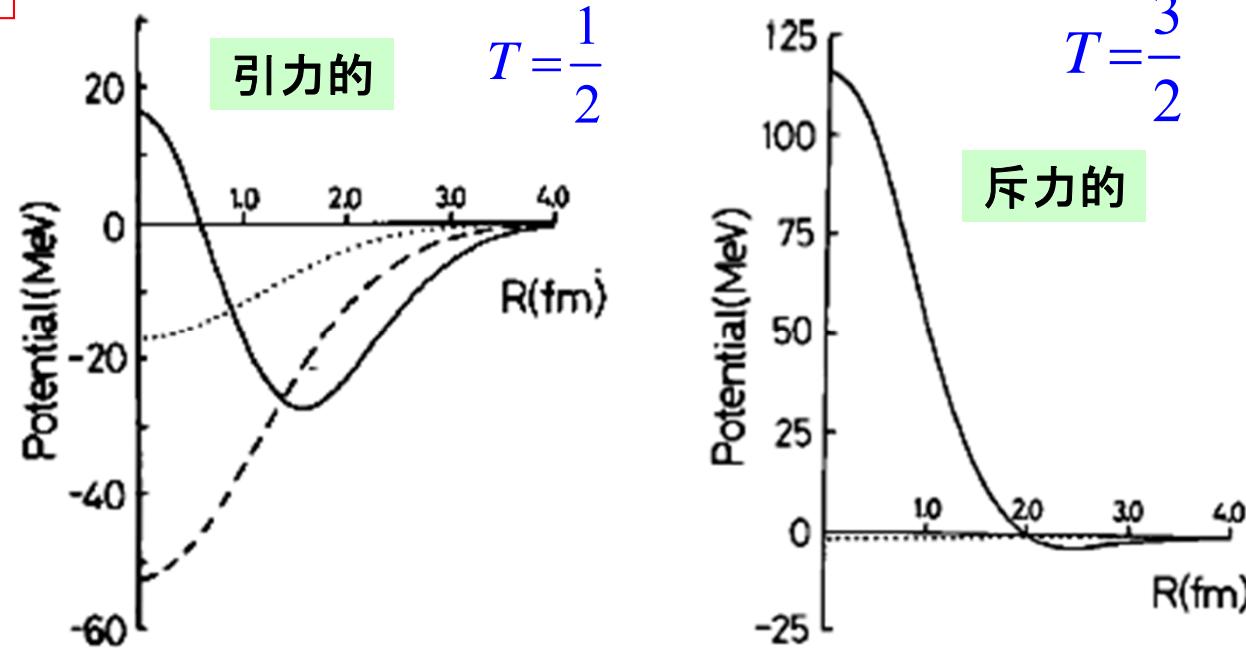
KAT Theory

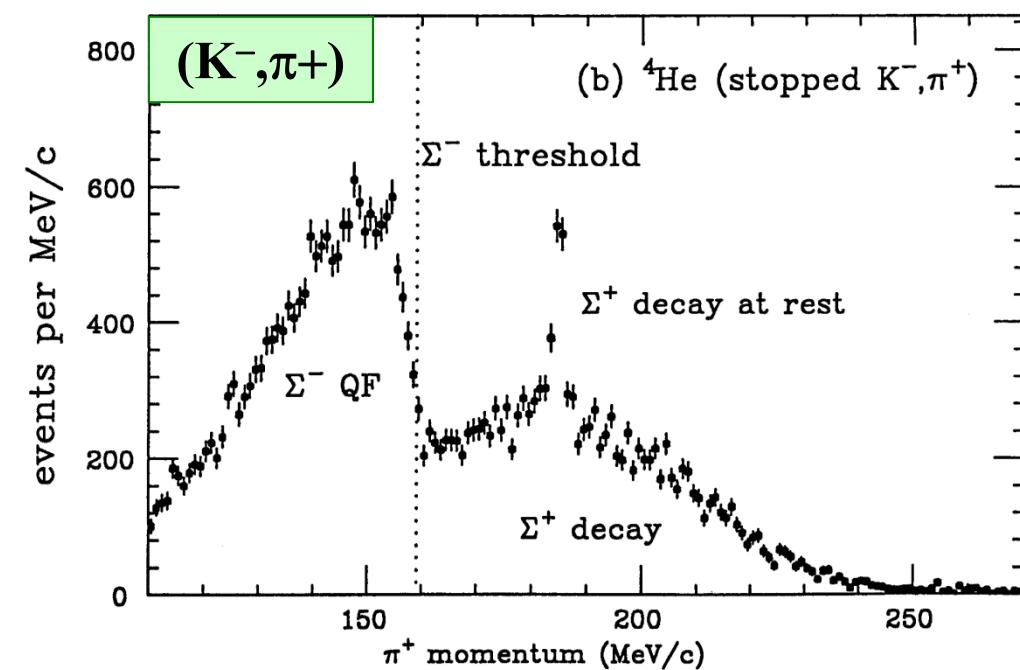
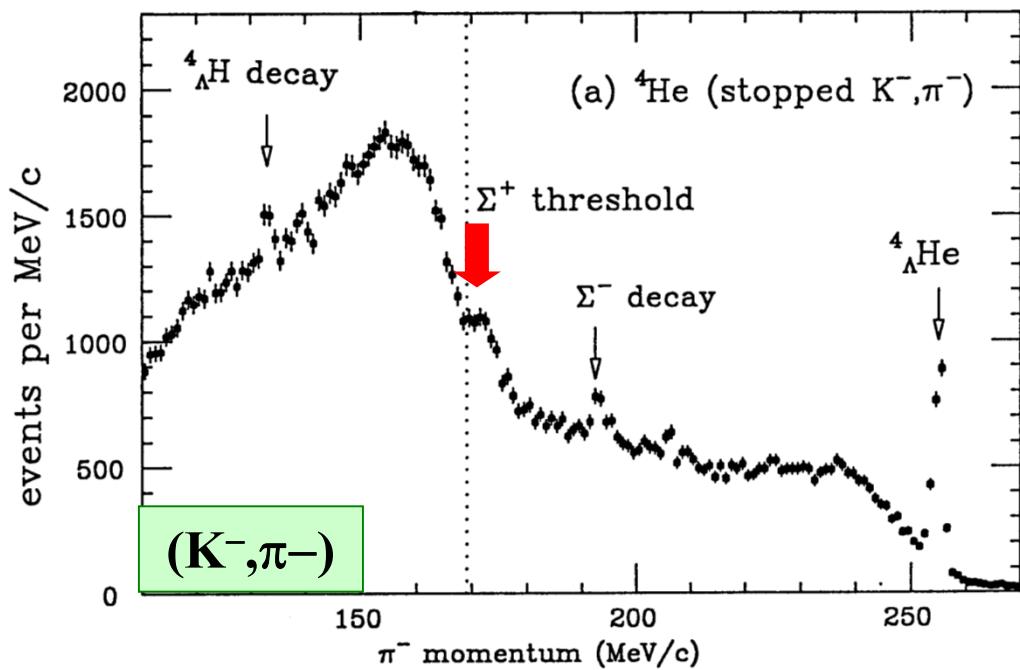
Kurihara

ΣN pot: ASP

Shinmura

“研究室の伝統と
先輩方に感謝！”





First Observation of a Bound Σ Hypernuclear State

KEK-E167 (1989)

R.S.Hayano, T.Ishikawa, M.Iwasaki,
H.Outa, E.Takeda, H.Tamura,
A.Sakaguchi, M.Aoki T.Yamazaki,
Phys.Lett. B231(1989)355.

$${}^4\Sigma\text{He} \quad B_{\Sigma^+} = 3.2 \pm 0.3^{+0.1}_{-1.1} \text{ MeV}$$

$$\Gamma = 4.6 \pm 0.5^{+1.6}_{-1.3} \text{ MeV}$$

Strong Lane term

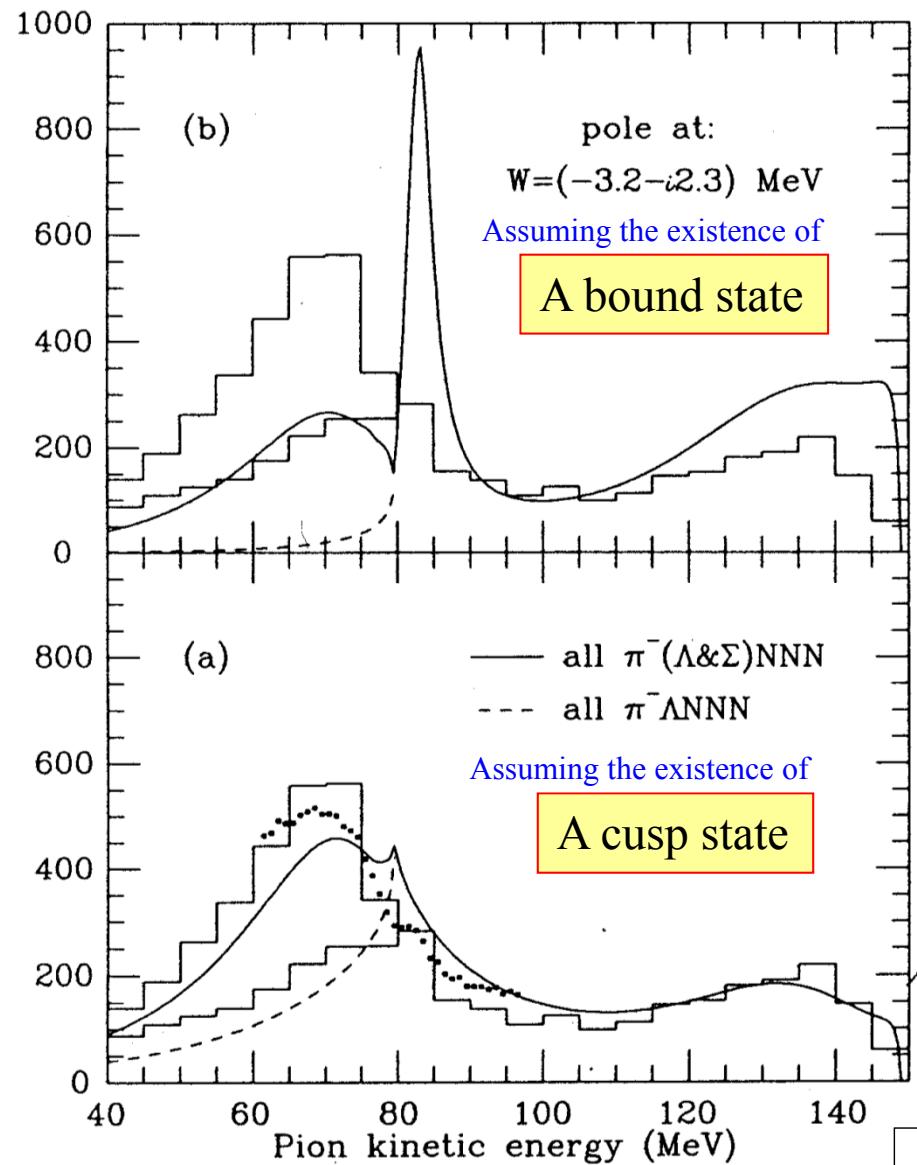
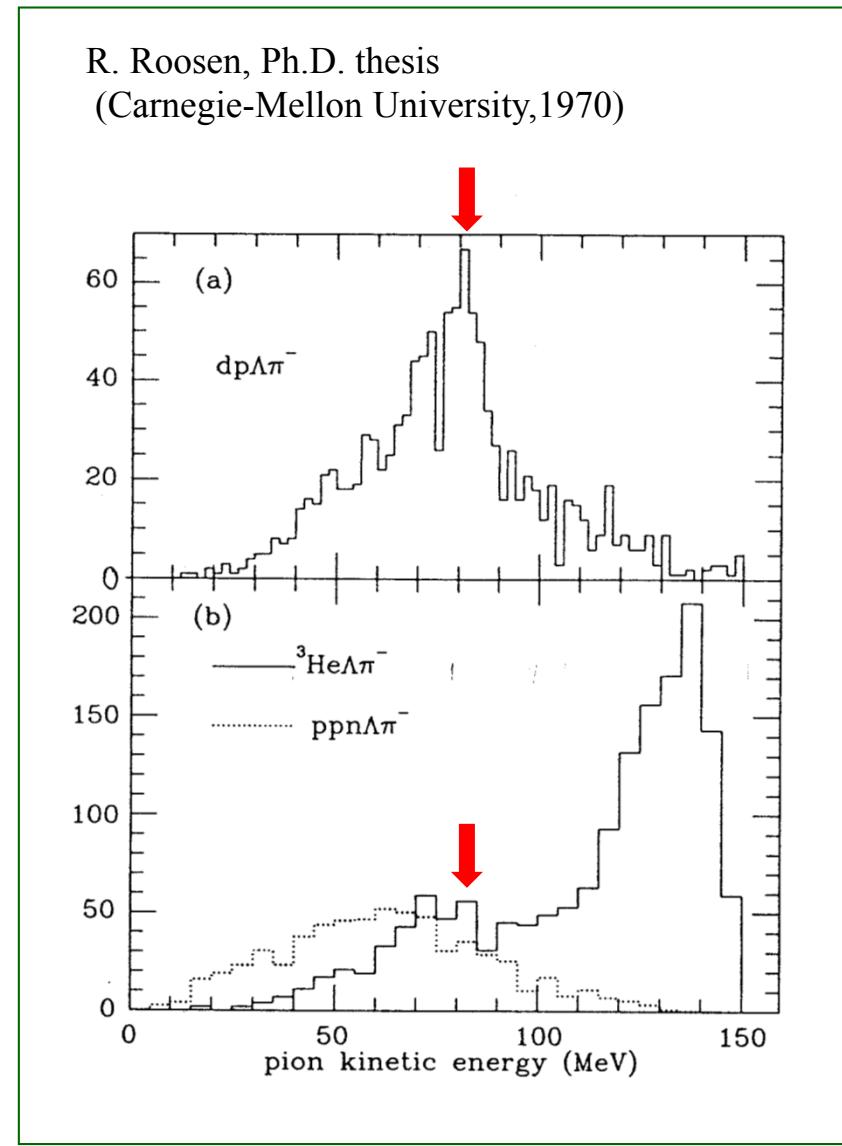
$$U_\Sigma = U_0 + U_\tau (\vec{T} \cdot \vec{t})$$

$$U_0 - U_\tau \quad \text{attractive} \quad U_0 + U_\tau / 2 \quad \text{repulsive}$$

T.Harada, S.Shinmura,Y.Akaishi,
H.Tanaka, NPA507(1990)715.

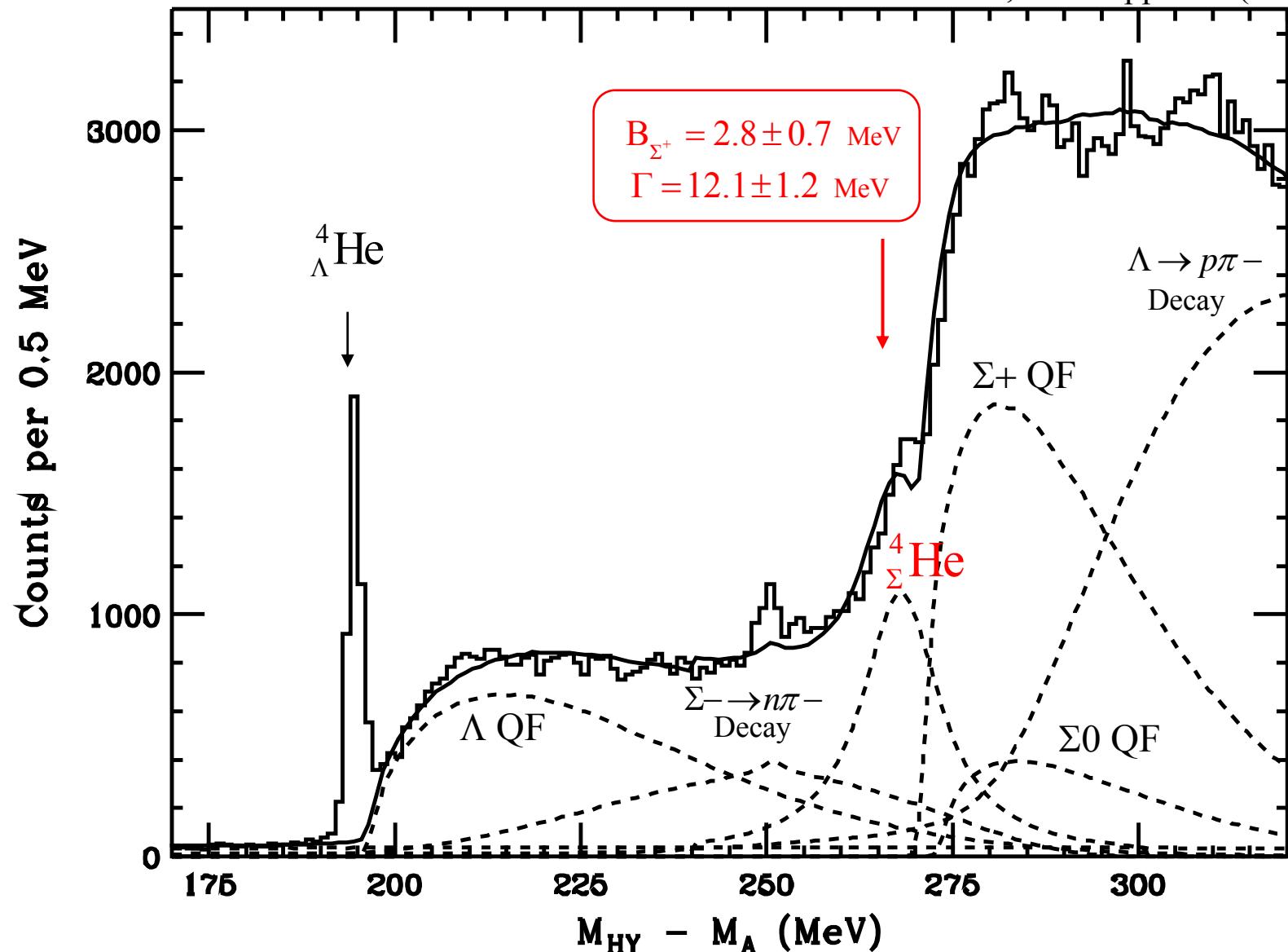
“IS THERE A BOUND $^4\Sigma$ He ?” (1990)

R.H.Dalitz, D.H. Davis and A.Deloff, PLB236(1990)76



Subtraction of hyperon decay background and Λ component from the π^- spectrum

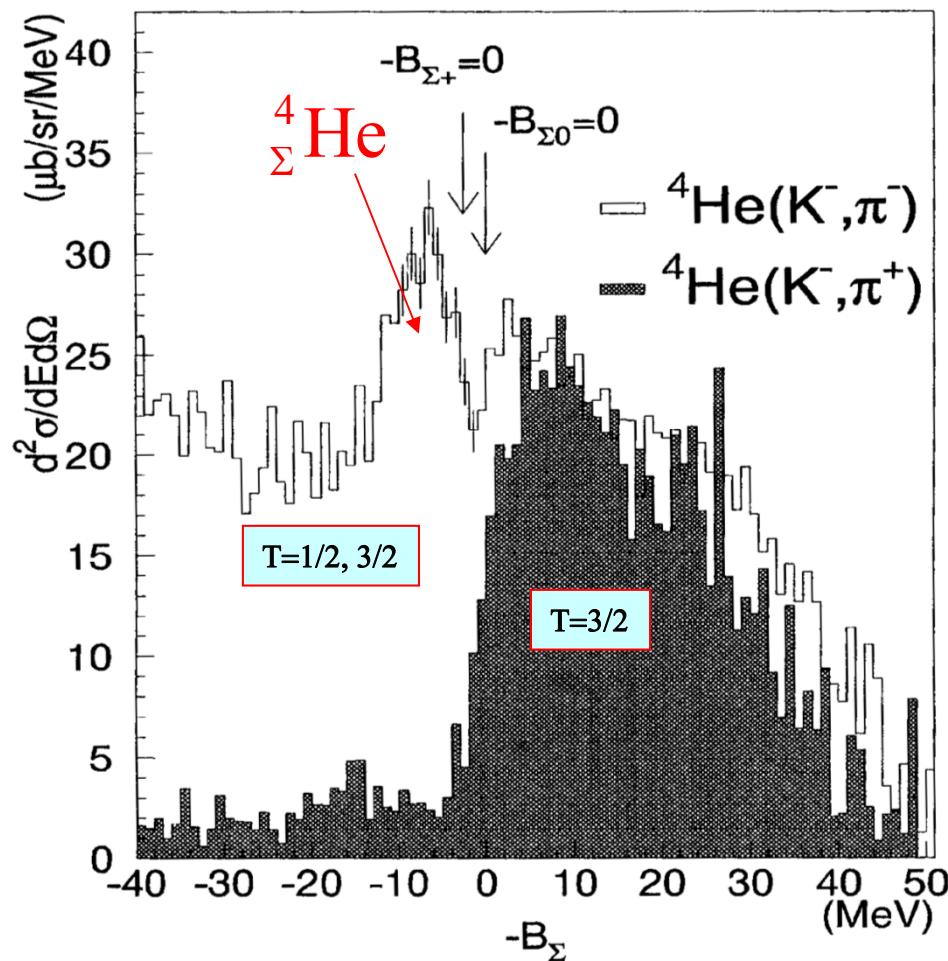
H. Outa et al., PTP.Supp. 117(1994)177.



Observation of a ${}^4\Sigma$ He Bound State

VOLUME 80, NUMBER 8

PHYSICAL RE



BNL-AGS (1995-)

T. Nagae, T. Miyachi, T. Fukuda, H. Outa,
T. Tamagawa, J. Nakano, R.S. Hayano,
H. Tamura, Y. Shimizu, K. Kubota,
R. E. Chrien, R. Sutter, A. Rusek,
W. J. Briscoe, R. Sawafta,
E.V. Hungerford, A. Empl, W. Naing,
C. Neerman, K. Johnston, M. Planinic,
Phys.Rev.Lett. **80**(1998)1605.

$$B_{\Sigma^+} = 4.4 \pm 0.3 \text{ MeV}$$

$$\Gamma = 7 \pm 0.7 \text{ MeV}$$

4.6 MeV
7.9 MeV

$$T = 1/2$$

$$J^\pi = 0^+$$

Theoretical Prediction

T. Harada, S. Shinmura,
Y. Akaishi, H. Tanaka,
NPA507(1990)715.

DWIA calculation for production cross sections

Green's function method

O. Morimatsu, K. Yazaki, NPA483(1988)493

スペクトル計算の理論的基盤
多方面でも適用され威力を発揮！

Inclusive differential cross section

$$\frac{d^2\sigma}{dE_\pi d\Omega} = \frac{k_\pi E_\pi}{(2\pi)^2 v_K} \frac{1}{[J_i]} \sum_{M_i} \sum_f |< f | \hat{O} | i >|^2 \delta(E_\pi - E_K + \omega)$$

Strength function

$$S(E) = \sum_f |< f | \hat{O} | i >|^2 \delta(E_\pi - E_K + E_f - E_i) = -\frac{1}{\pi} \text{Im} \int d\mathbf{r} d\mathbf{r}' F^\dagger(\mathbf{r}) G(E+i\varepsilon, \mathbf{r}, \mathbf{r}') F(\mathbf{r}')$$

Green's function

Coupled-channel Green's function

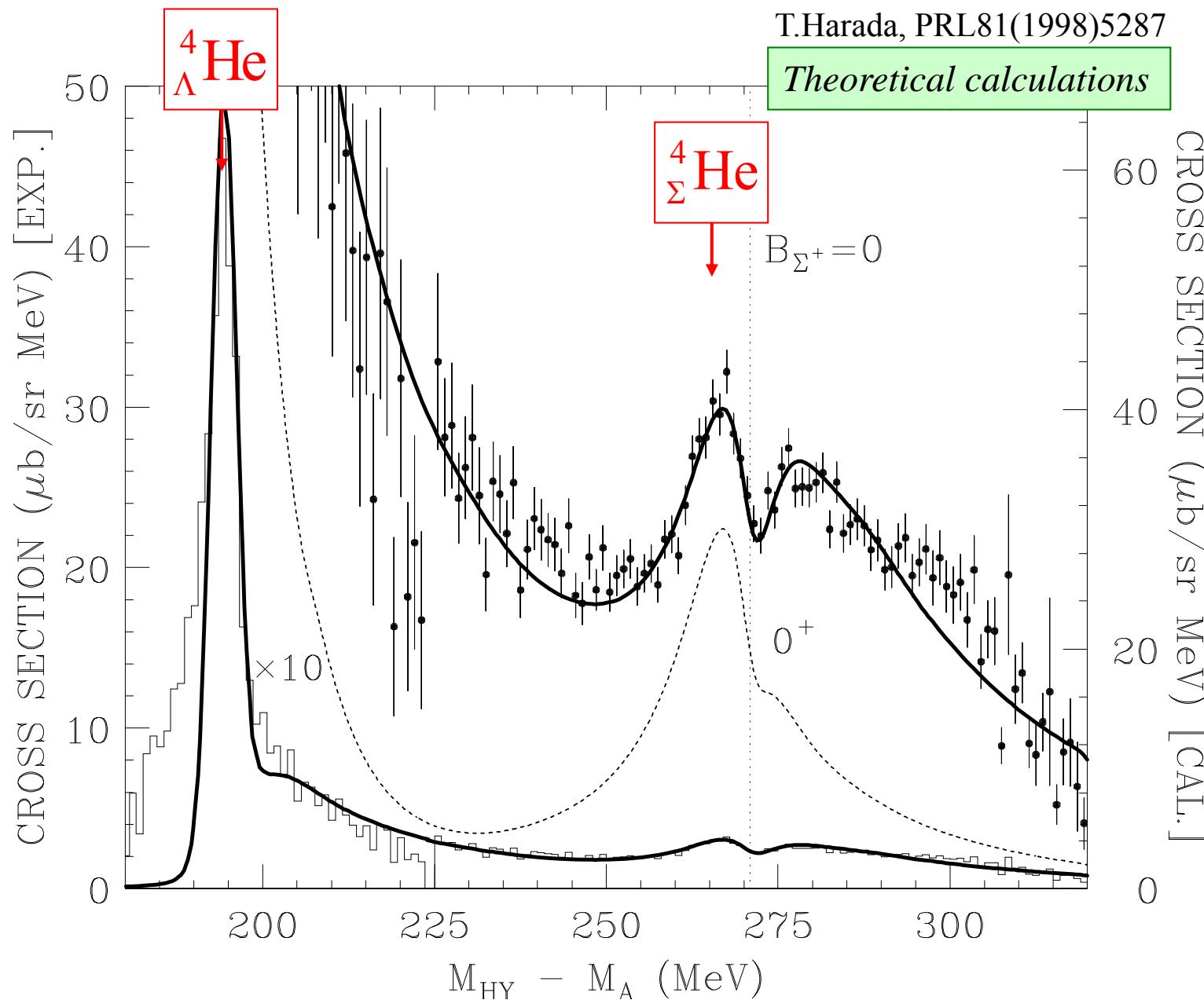
T.Harada, NPA672(2000)181

$$\hat{\mathbf{G}}(E_f) = \hat{\mathbf{G}}^{(0)}(E_f) + \hat{\mathbf{G}}^{(0)}(E_f) \hat{\mathbf{U}} \hat{\mathbf{G}}(E_f)$$

$$\hat{\mathbf{G}}^{(0)}(E_f) = \begin{bmatrix} G_\Lambda^{(0)} & & \\ & G_{\Sigma^+}^{(0)} & \\ & & G_{\Sigma^0}^{(0)} \end{bmatrix} \quad \hat{\mathbf{U}} = \begin{bmatrix} U_{\Lambda,1/2} & U_{X_1,1/2} & 0 \\ U_{X_1,1/2} & U_{\Sigma,1/2} & 0 \\ 0 & 0 & U_{\Sigma,3/2} \end{bmatrix}$$

$$\text{Im}\hat{G} = \underbrace{\hat{\Omega}^{(-)\dagger} \{ \text{Im}\hat{G}_\Lambda^{(0)} \} \hat{\Omega}^{(-)}}_{\Lambda \text{ escape}} + \underbrace{\hat{\Omega}^{(-)\dagger} \{ \text{Im}\hat{G}_{\Sigma^+}^{(0)} \} \hat{\Omega}^{(-)}}_{\Sigma^+ \text{ escape}} + \underbrace{\hat{\Omega}^{(-)\dagger} \{ \text{Im}\hat{G}_{\Sigma^0}^{(0)} \} \hat{\Omega}^{(-)}}_{\Sigma^0 \text{ escape}} + \underbrace{\hat{G}^\dagger \{ W_{Y,T} \} \hat{G}}_{\text{Spreading (3N breakup)}}$$

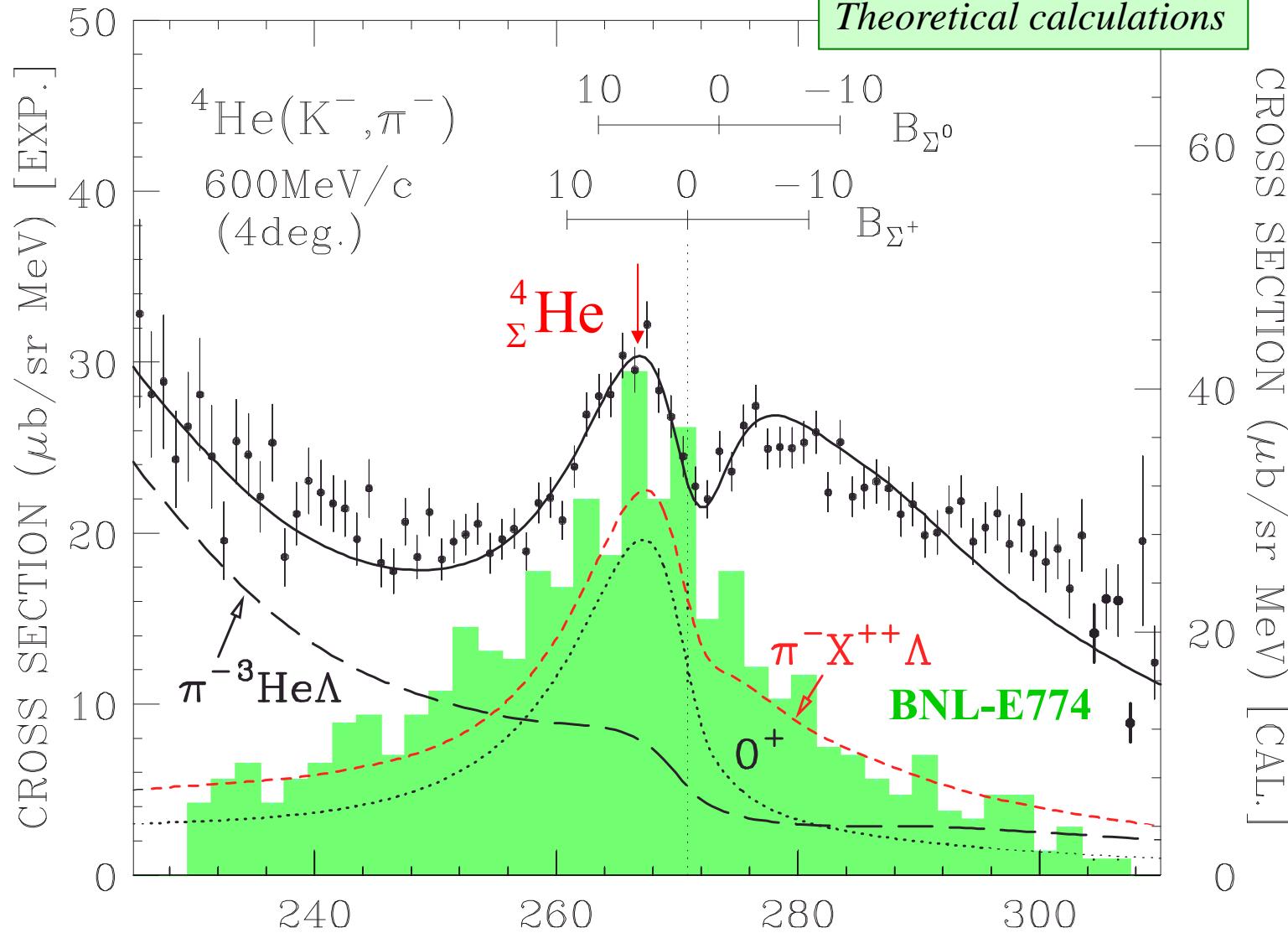
$^4\text{He}(\text{K}^-, \pi^-)$ spectrum at 600 MeV/c (BNL)



$^4\text{He}(\text{K}^-, \pi^-)$ spectrum at 600 MeV/c (BNL)

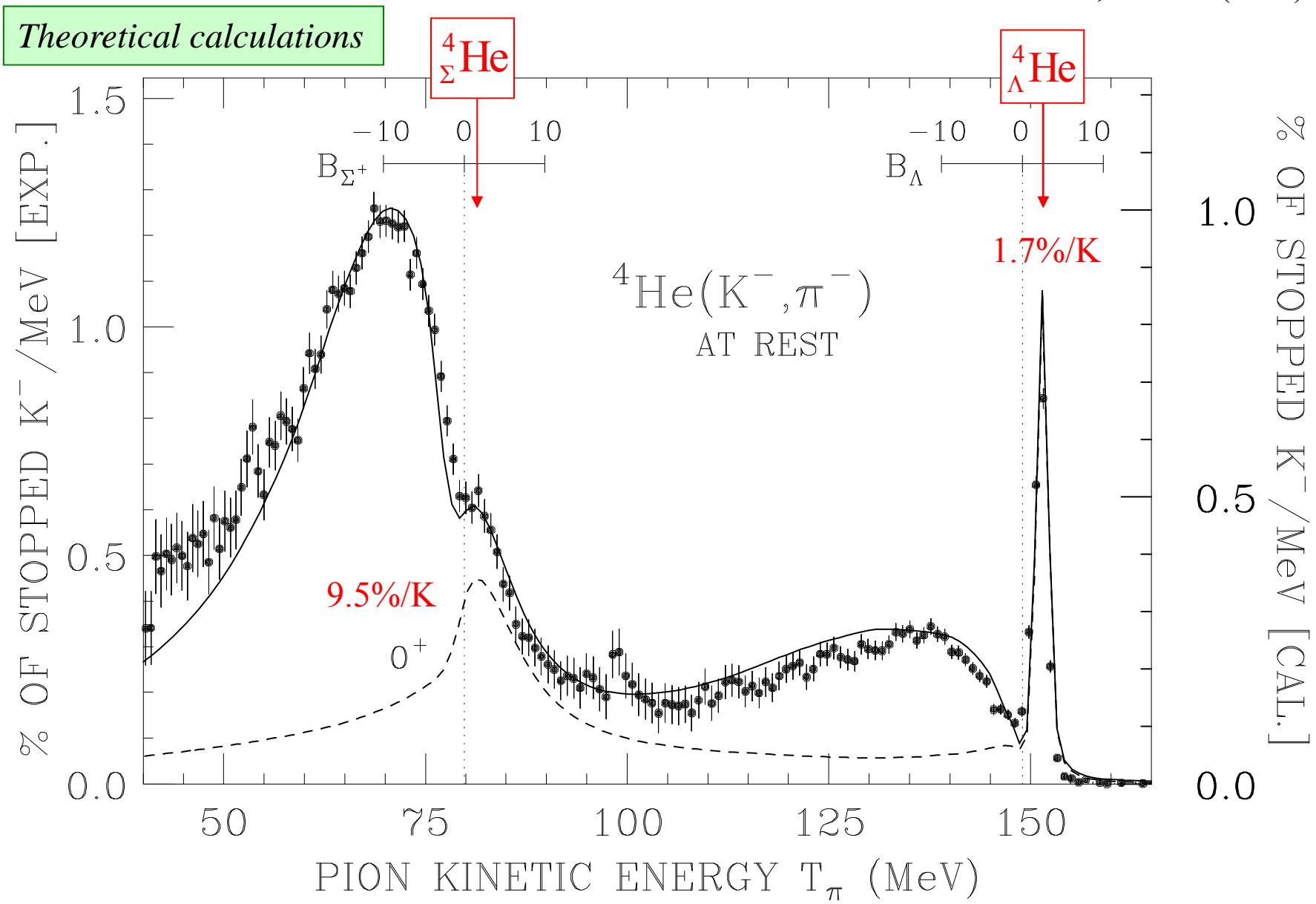
T.Harada, PRL81(1998)5287

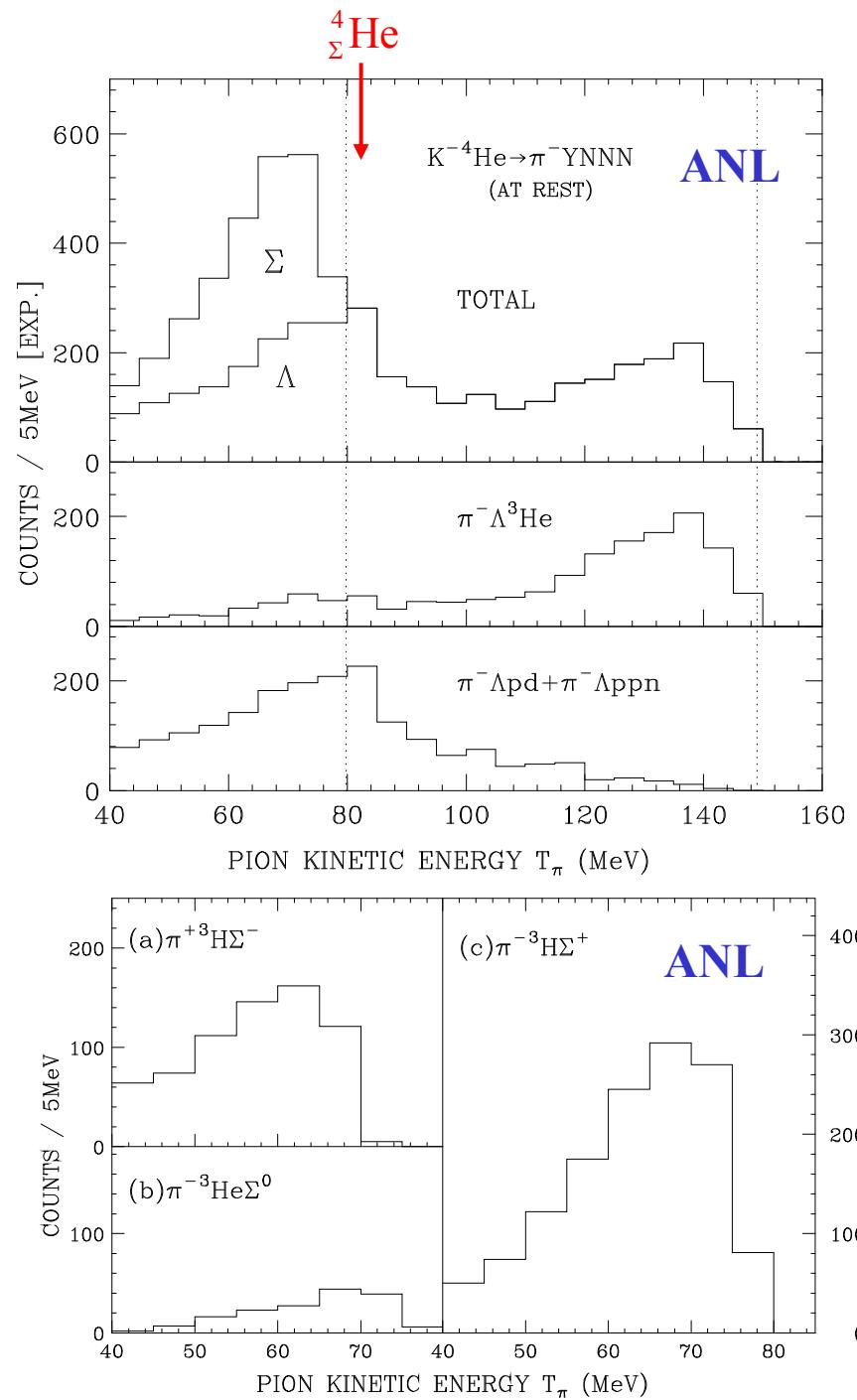
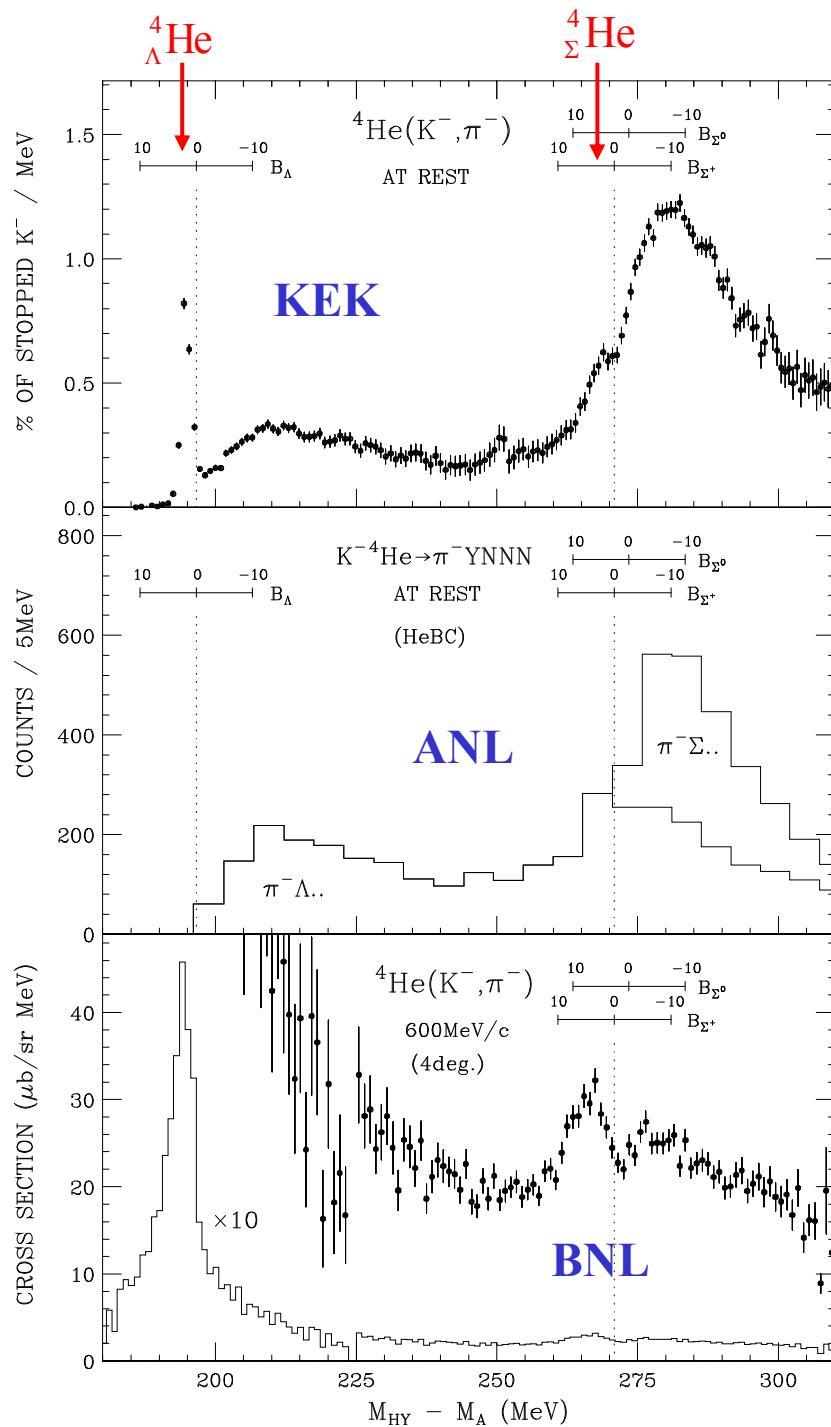
Theoretical calculations

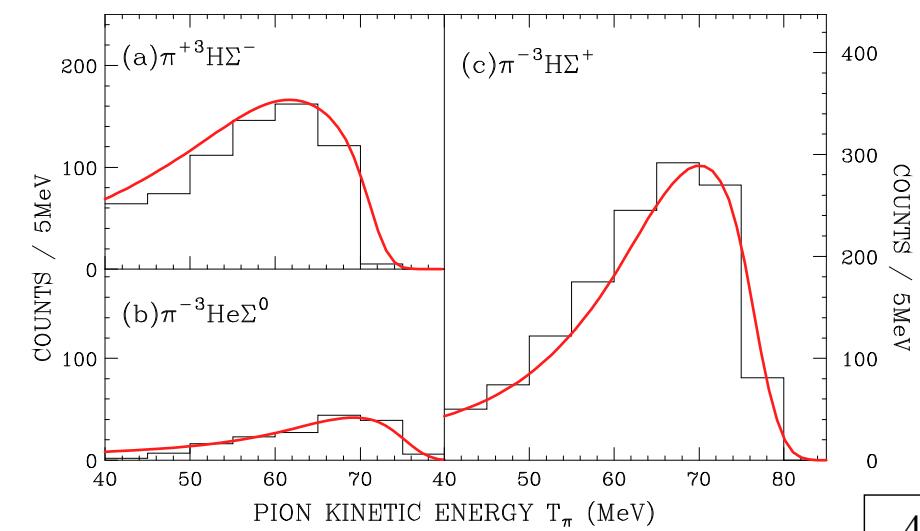
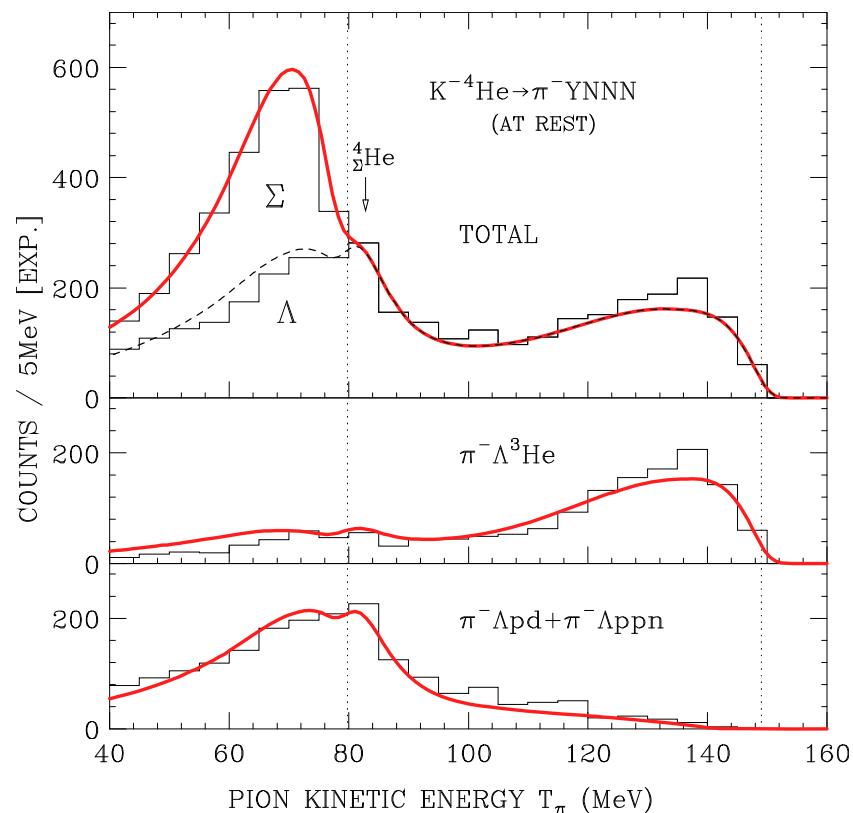
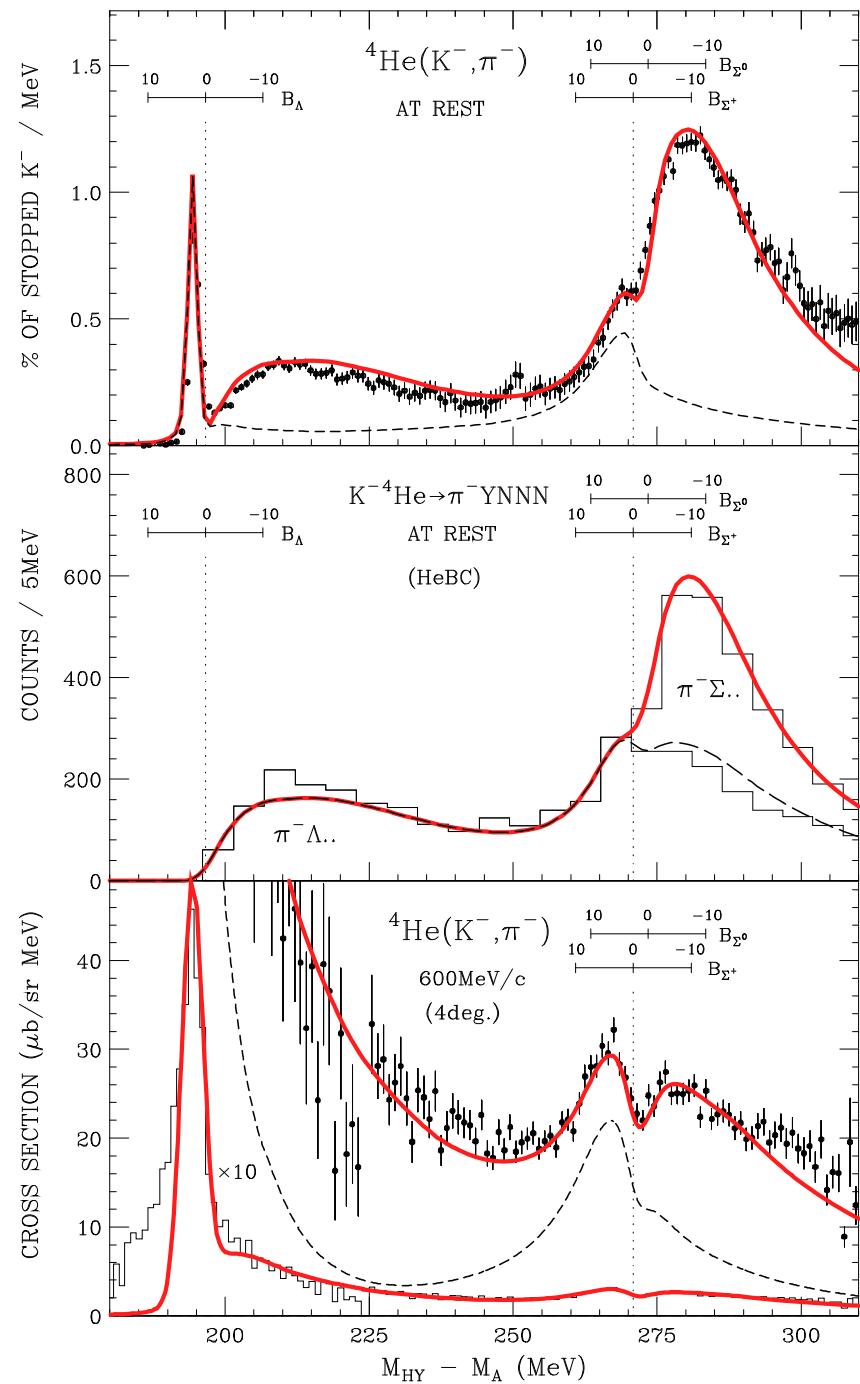


$^4\text{He}(\text{K}^-, \pi^-)$ spectrum at Rest (KEK)

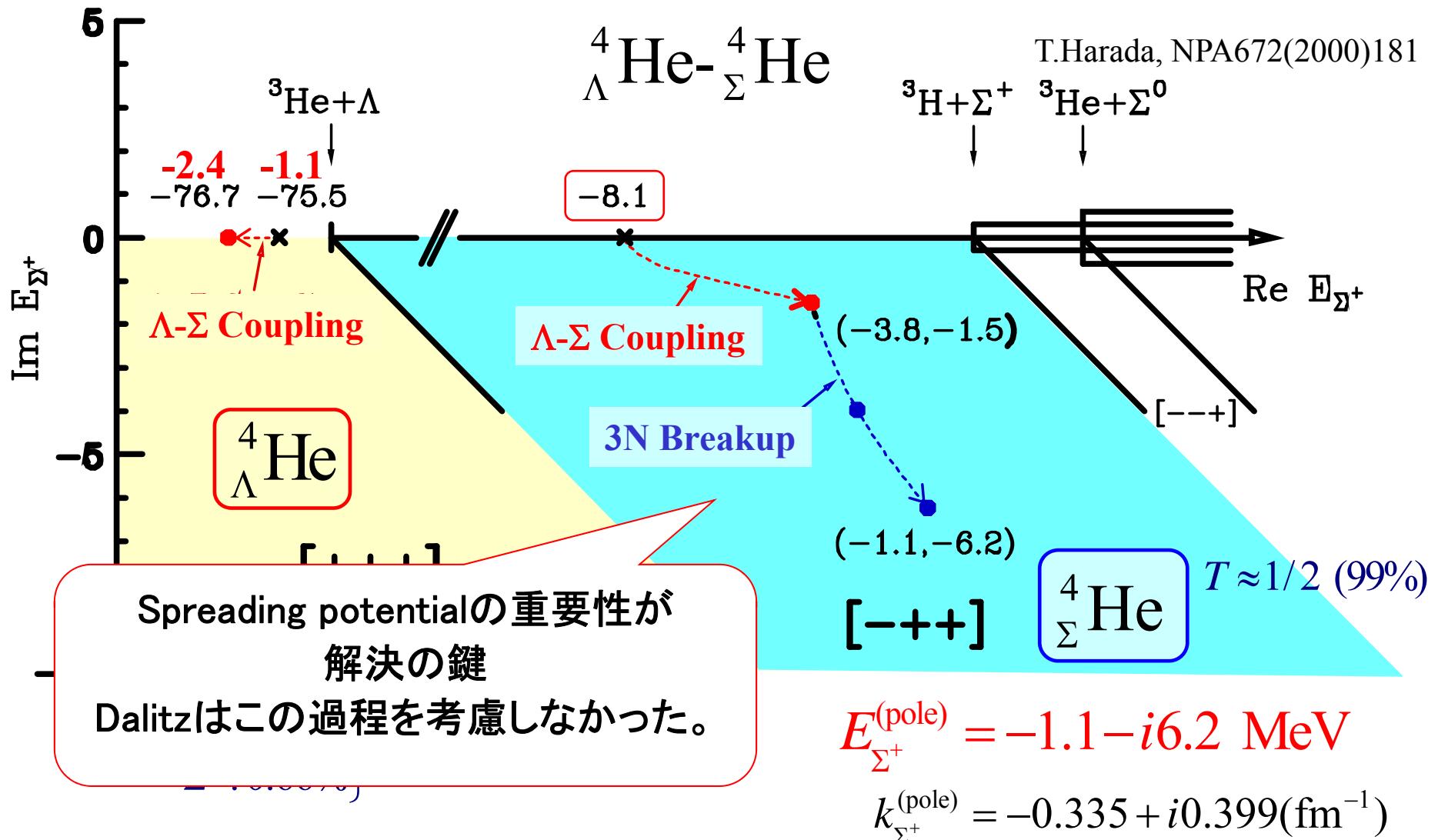
T.Harada, NPA672(2000)181



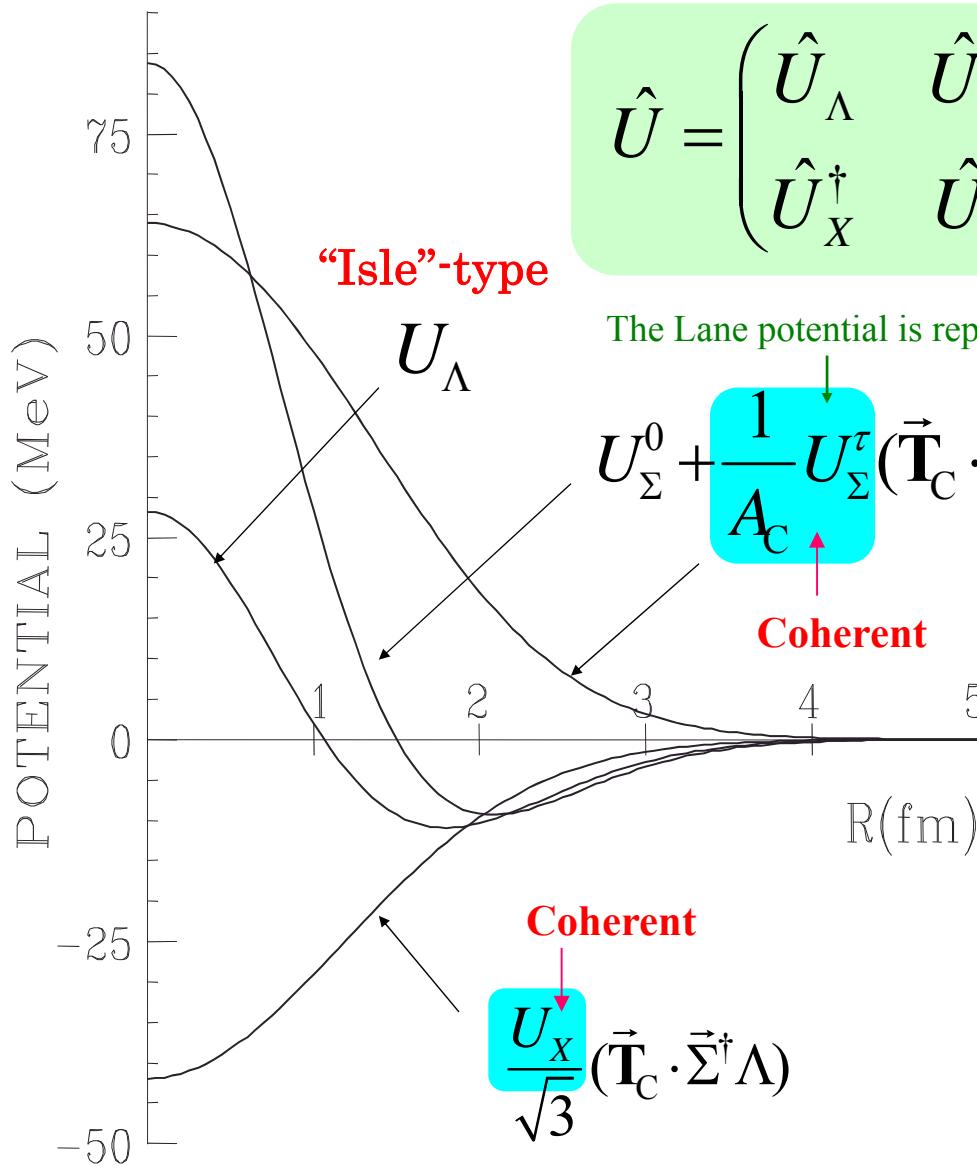




Pole positions of the $Y\text{-}3N$ hypernucleus



Properties of the 3N-Y potential

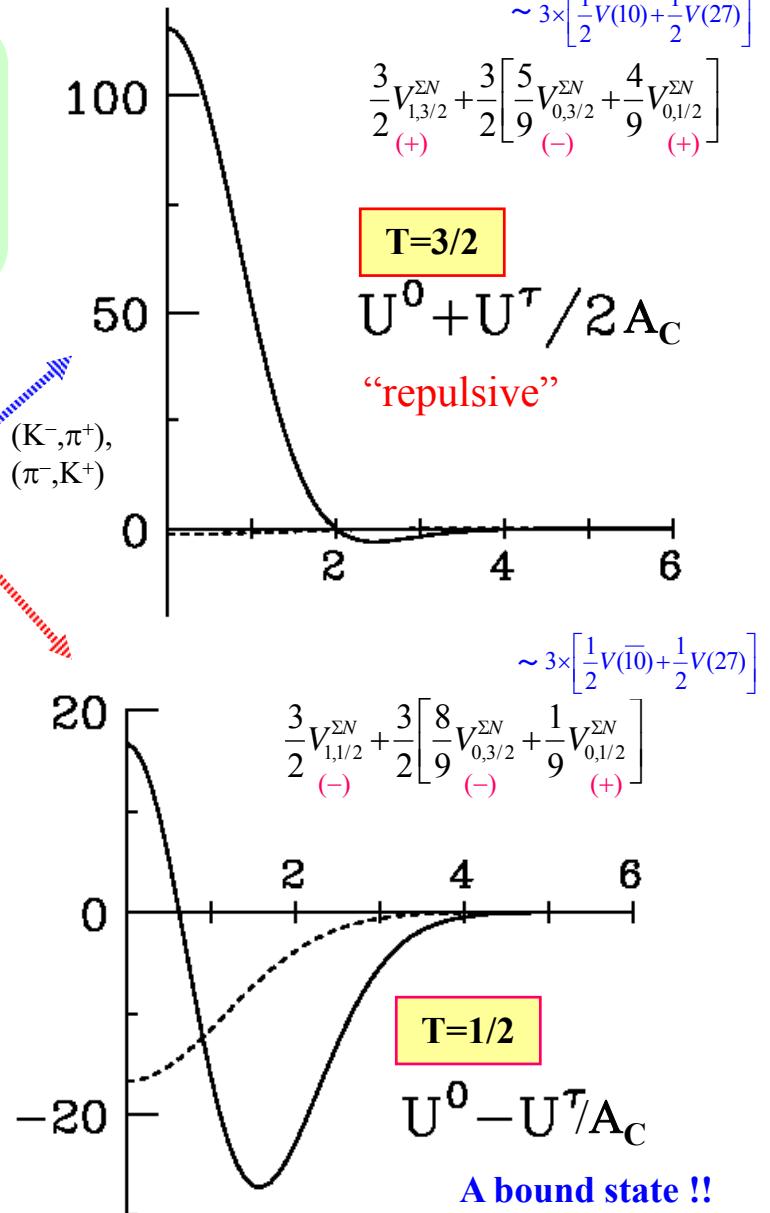


$$\hat{U} = \begin{pmatrix} \hat{U}_\Lambda & \hat{U}_X \\ \hat{U}_X^\dagger & \hat{U}_\Sigma \end{pmatrix}$$

The Lane potential is repulsive.

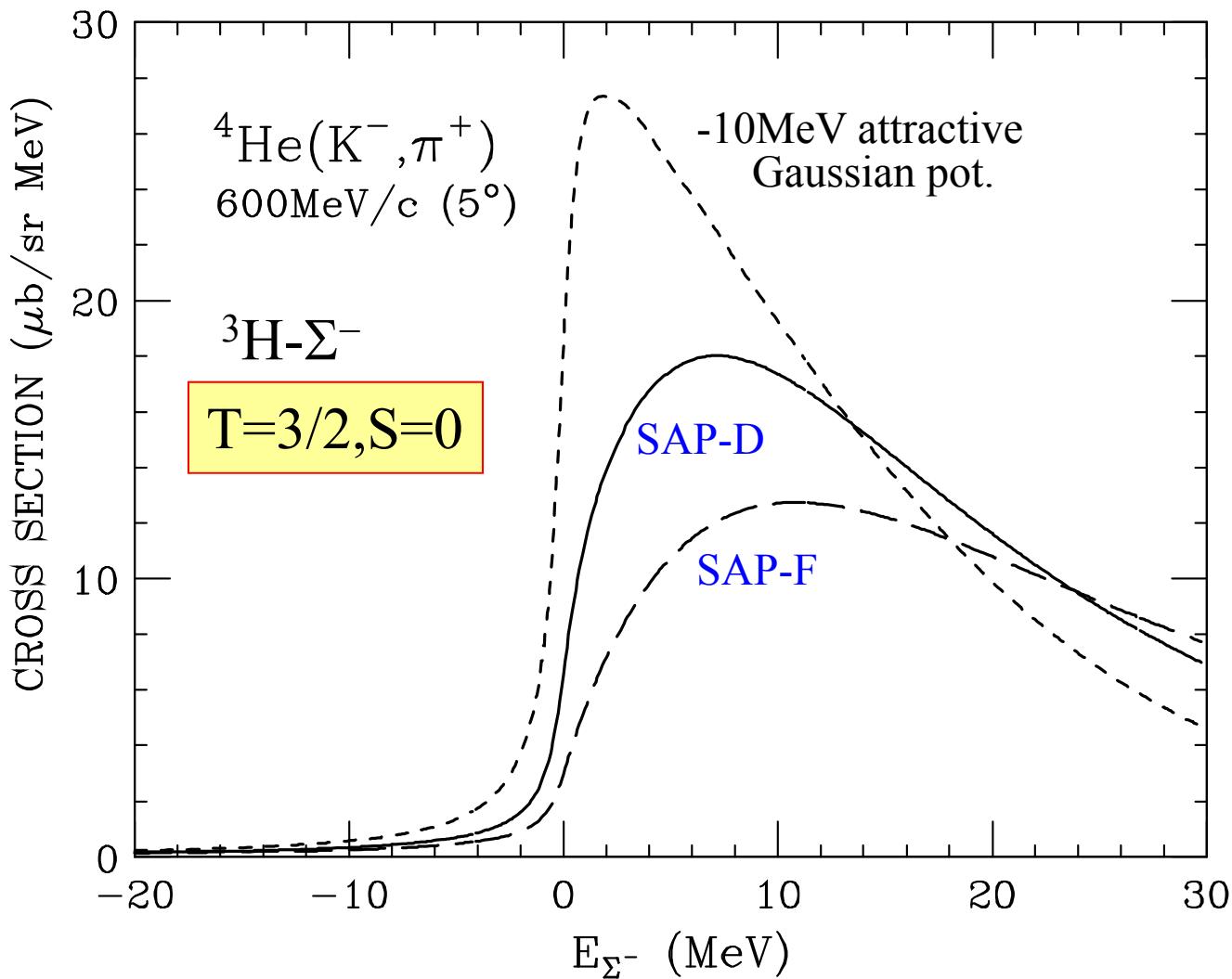
$$U_\Sigma^0 + \frac{1}{A_C} U_\Sigma^\tau (\vec{T}_C \cdot \vec{t}_\Sigma)$$

Coherent



Cf. T.Yamada, K. Ikeda, PRC46(1992)1315.

$^4\text{He}(\text{K}^-, \pi^+)$ spectrum at 600 MeV/c (5deg)



Coherent isospin and Λ - Σ Coupling in ${}^4_{\Lambda}\text{He}$ - ${}^4_{\Sigma}\text{He}$

B.F. Gibson *et al.*, PRC6 (1972) 741
 T. Harada *et al.*, NPA507(1990) 715
 Y.Akaishi *et al.*, PRL84 (2000) 3539.

$$| {}_{\Lambda,\Sigma}{}^4\text{He} \rangle = \phi_{\Lambda}(\mathbf{r}) | {}^3\text{He} \rangle + \phi_{\Sigma^+}(\mathbf{r}) | {}^3\text{H} \rangle + \phi_{\Sigma^0}(\mathbf{r}) | {}^3\text{He} \rangle$$

0^+

1^+

$$T = \frac{3}{2}$$

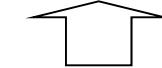
$$\frac{3}{2}g_{1,3/2}^{\Sigma N} + \frac{3}{2} \left[\frac{5}{9}g_{0,3/2}^{\Sigma N} + \frac{4}{9}g_{0,1/2}^{\Sigma N} \right]$$



$$(+) - (-) - [(-) - (+)]$$

${}^4_{\Sigma}\text{He}$

$$\frac{5}{2} \left[\frac{11}{15}g_{1,3/2}^{\Sigma N} + \frac{4}{15}g_{1,1/2}^{\Sigma N} \right] + \frac{1}{2}g_{0,3/2}^{\Sigma N}$$



$$(+) - (-) + [(-) - (+)]$$

—

$$\frac{3}{3}[g_{1,3/2}^{\Sigma N} - g_{1,1/2}^{\Sigma N}] - \frac{1}{3}[g_{0,3/2}^{\Sigma N} - g_{0,1/2}^{\Sigma N}]$$



$$\frac{3}{2}g_{1,1/2}^{\Sigma N} + \frac{3}{2} \left[\frac{8}{9}g_{0,3/2}^{\Sigma N} + \frac{1}{9}g_{0,1/2}^{\Sigma N} \right]$$

${}^4_{\Sigma}\text{He}$

$$\frac{5}{2} \left[\frac{8}{15}g_{1,3/2}^{\Sigma N} + \frac{7}{15}g_{1,1/2}^{\Sigma N} \right] + \frac{1}{2}g_{0,1/2}^{\Sigma N}$$

$$T = \frac{1}{2}$$

$$\frac{3}{2}g_{1,1/2}^{\Lambda N, \Sigma N} - \frac{1}{2}g_{0,1/2}^{\Lambda N, \Sigma N}$$

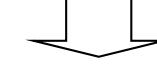


$$\frac{3}{2}g_{1,1/2}^{\Lambda N} + \frac{3}{2}g_{0,1/2}^{\Lambda N}$$

Lane term

$$\hat{U}_{\Sigma}^{\tau}$$

$$\frac{1}{3}[g_{1,3/2}^{\Sigma N} - g_{1,1/2}^{\Sigma N}] + \frac{1}{3}[g_{0,3/2}^{\Sigma N} - g_{0,1/2}^{\Sigma N}]$$



Λ - Σ coupling

$$\hat{U}_X$$

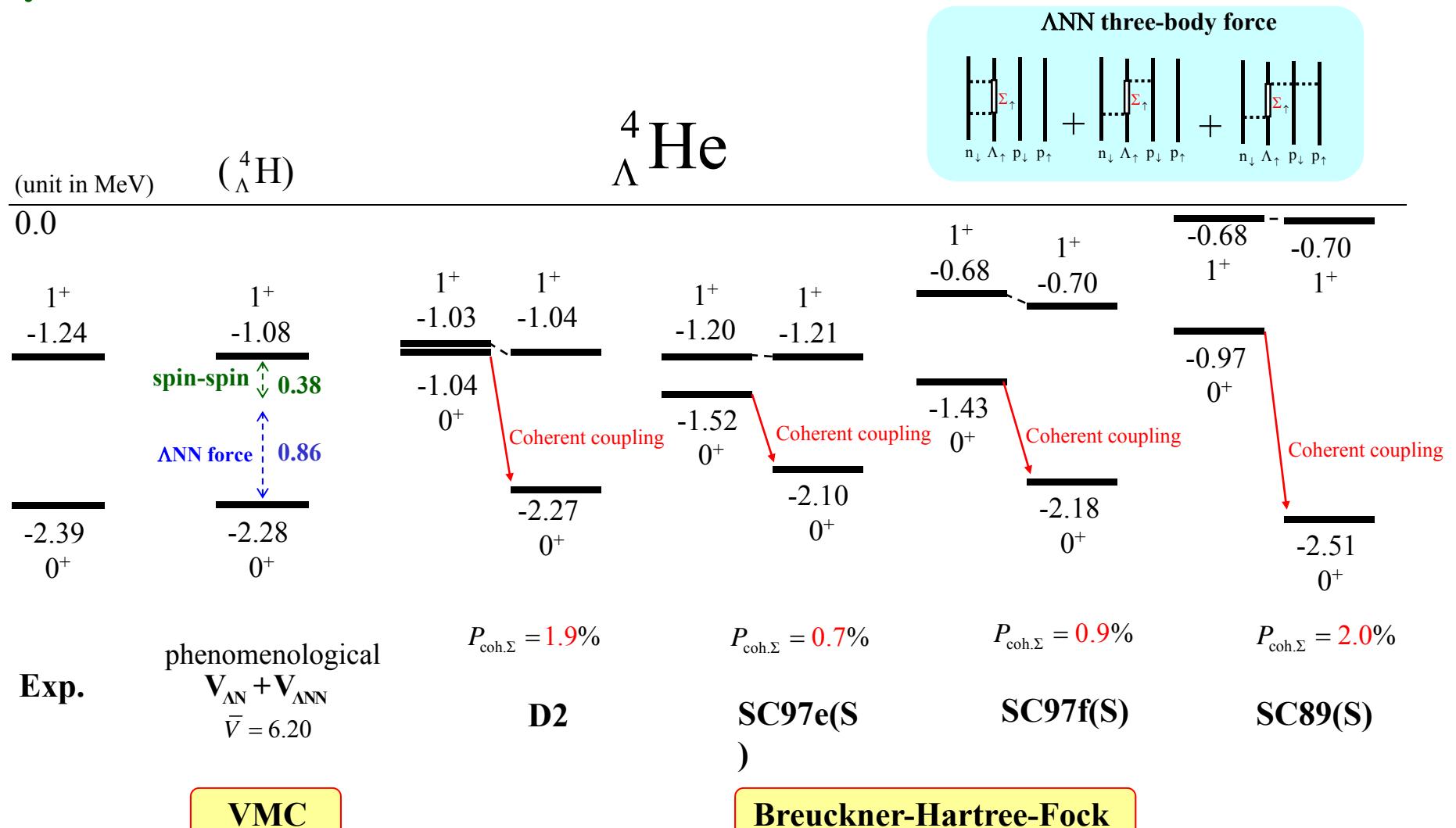
$$\frac{1}{2}g_{1,1/2}^{\Lambda N, \Sigma N} + \frac{1}{2}g_{0,1/2}^{\Lambda N, \Sigma N}$$



${}^4_{\Lambda}\text{He}$

$$\frac{5}{2}g_{1,1/2}^{\Lambda N} + \frac{1}{2}g_{0,1/2}^{\Lambda N}$$

“The 0^+ - 1^+ difference is not a measure of ΛN spin-spin interaction.”
by B.F. Gibson



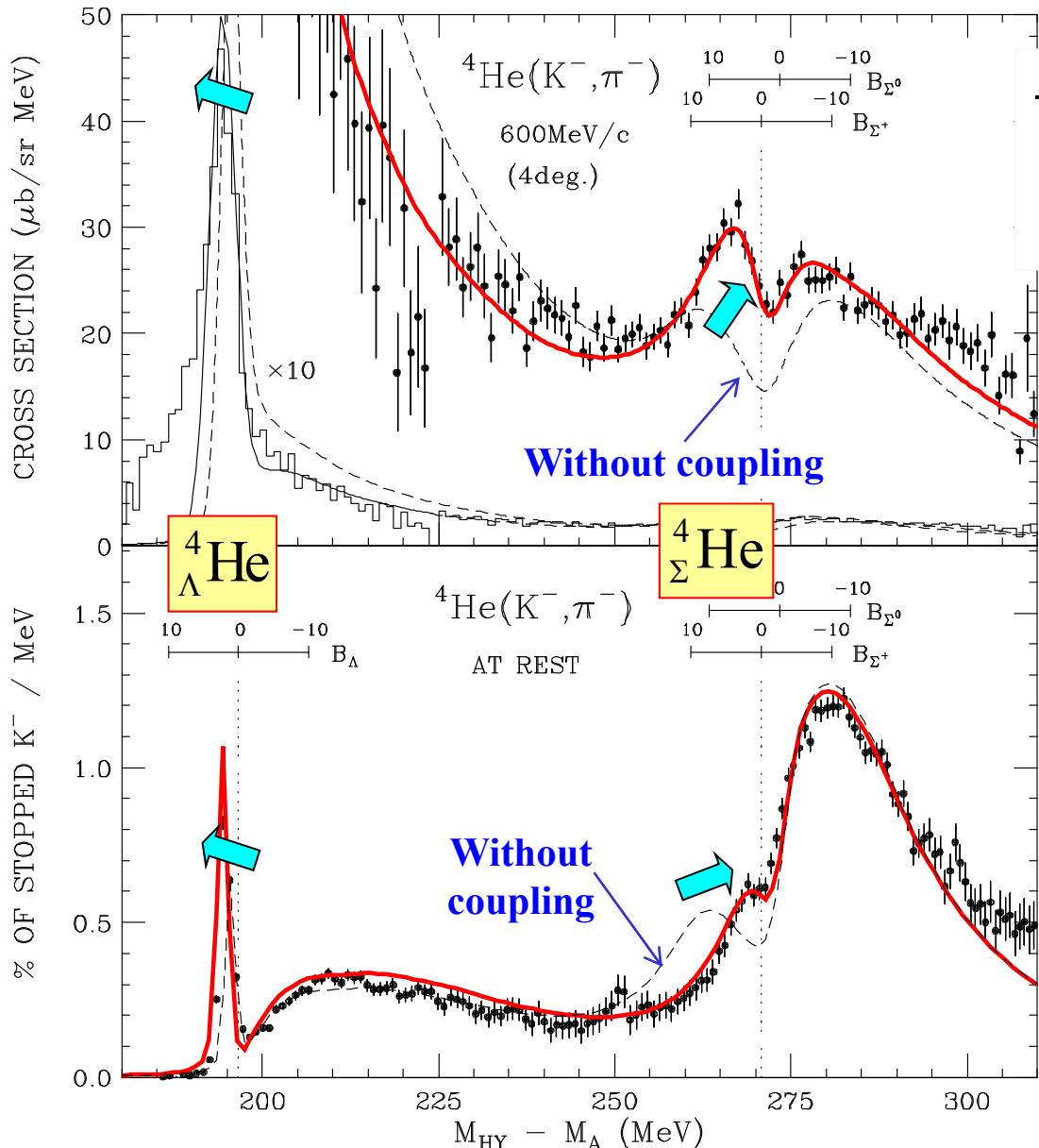
R. Sinha, Q.N.Usmani,
NPA684(2001)586c

Y. Akaishi, T.Harada, S.Shinmura, Khun Swe Myint,
PRL84(2000)3539

Λ - Σ coupling effects on the (K^- , π^-) spectrum

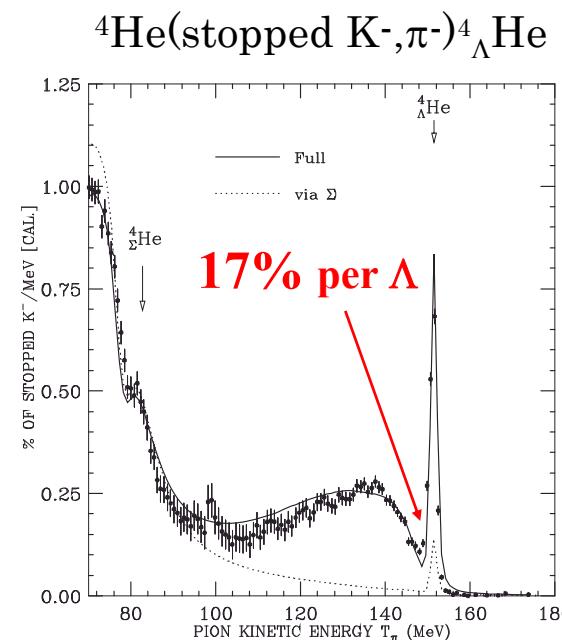
Hyperon-mixing

T.Harada, NPA507(1990)715.

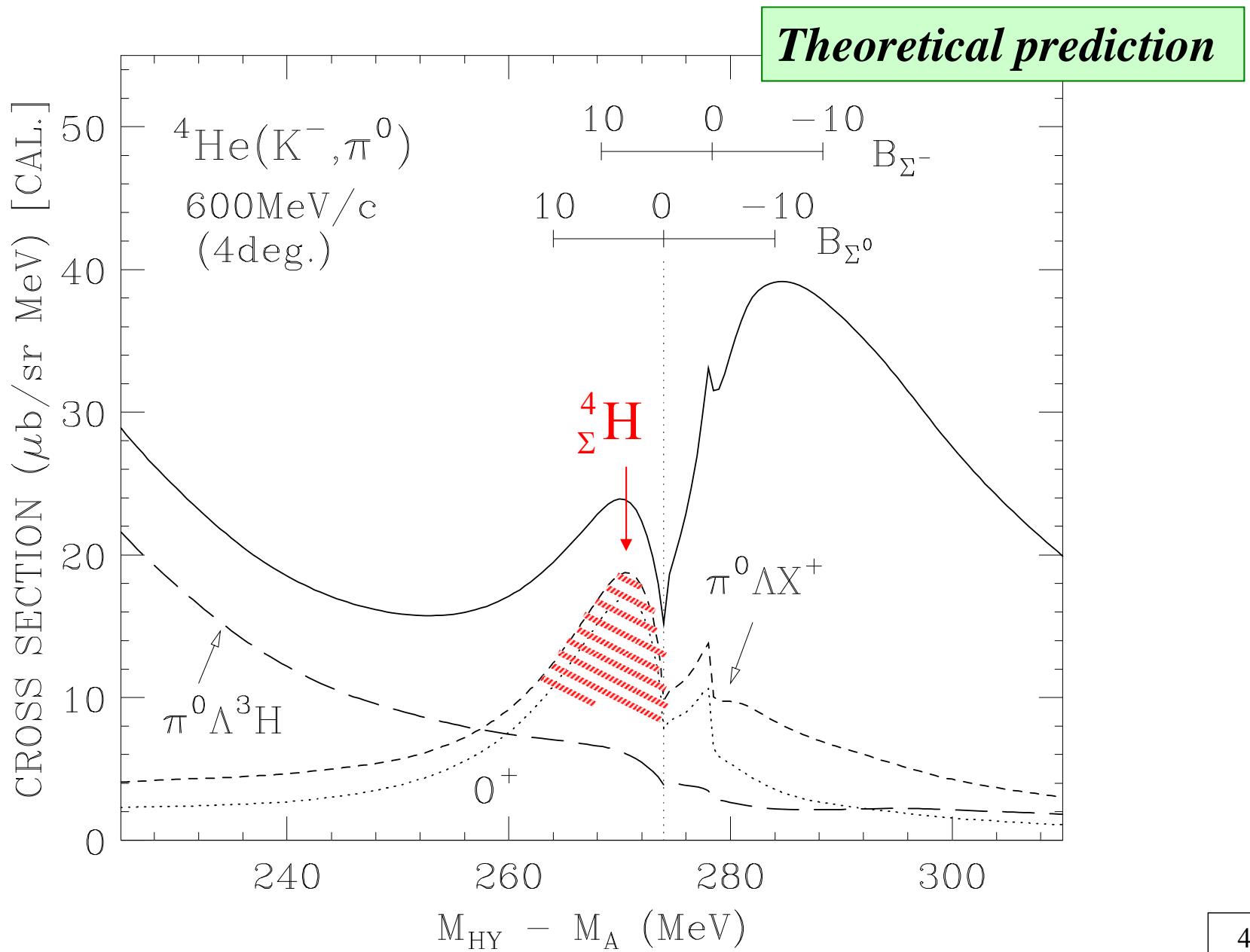


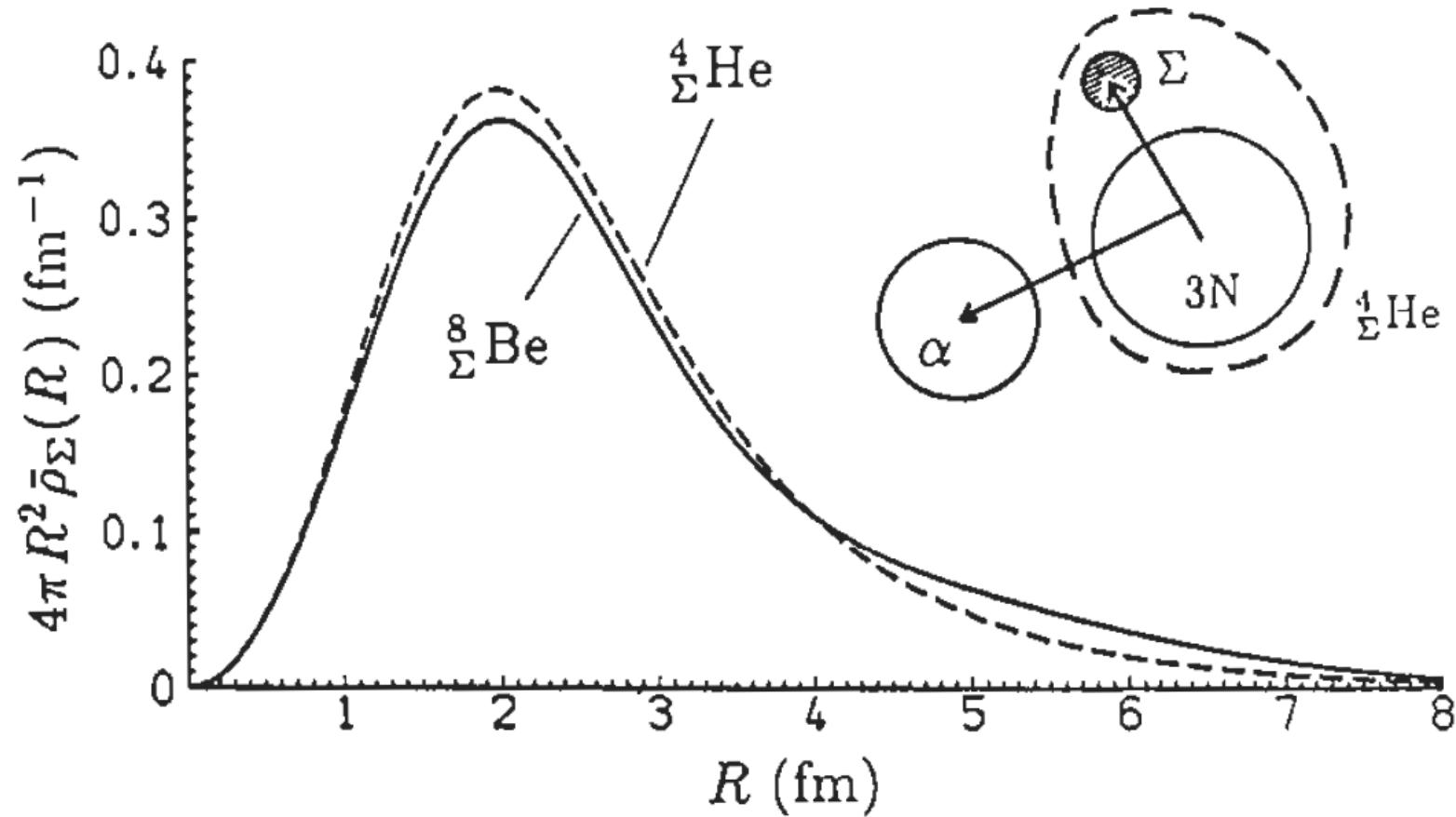
-The Λ - Σ coupling effects play a important role in reproducing the spectrum.

- The Λ state is produced via Σ components in the ground state.



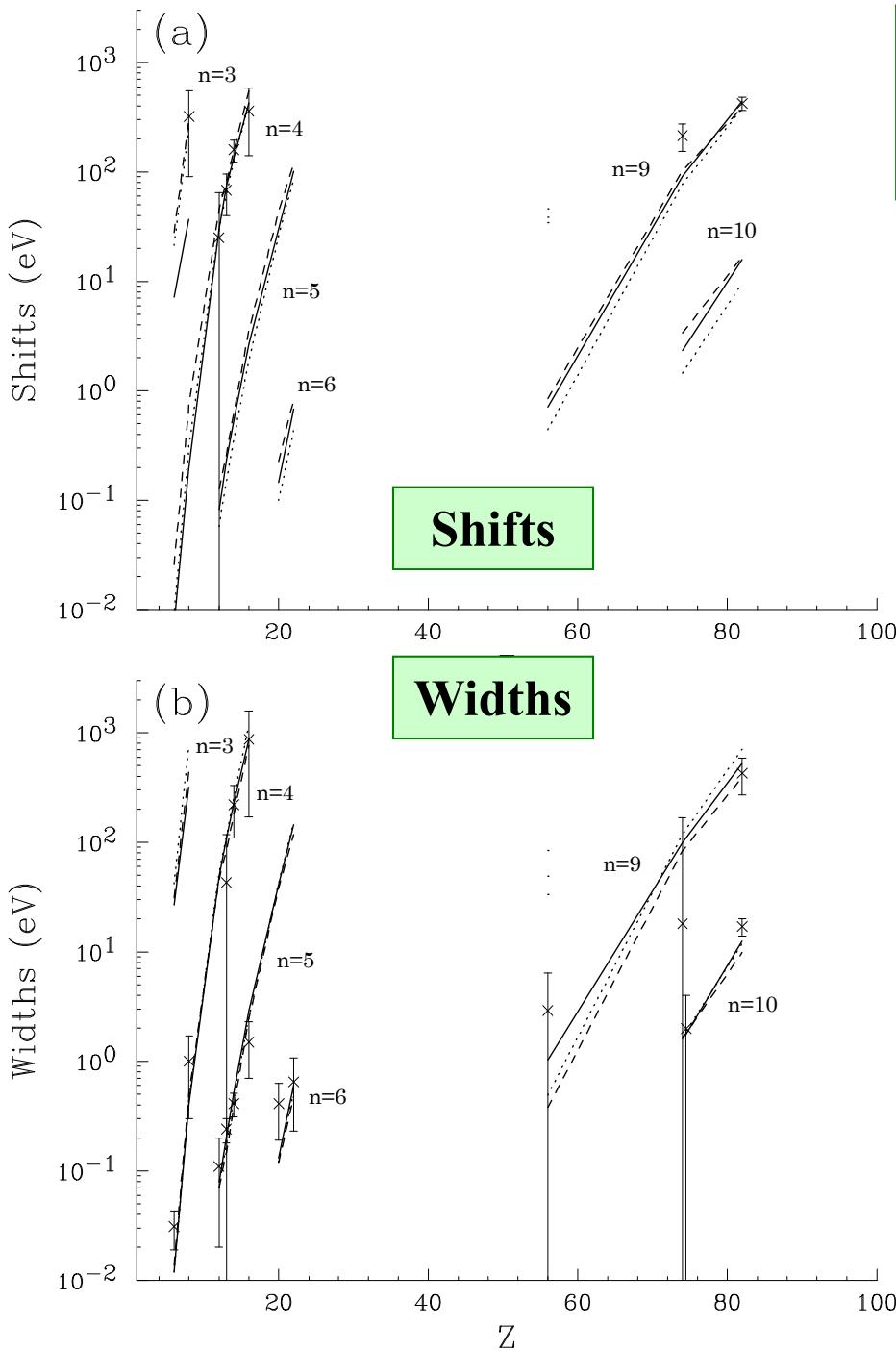
$^4\text{He}(K^-, \pi^0)$ spectrum at 600 MeV/c





Σ核ポテンシャルは斥力か？

Observation of Σ^- atomic X-ray



G. Backenstoss, et al., Z. Phys. A273(1975)137
 C.J. Batty, et al., Phys.Lett.B 74 (1978) 27
 R.J. Powers, et al., PRC47(1993)1263

C	$4 \rightarrow 3$	Γ_u
O	$4 \rightarrow 3$	ϵ, Γ_u
Mg	$5 \rightarrow 4$	ϵ, Γ_u
Al	$5 \rightarrow 4$	$\epsilon, \Gamma, \Gamma_u$
Si	$5 \rightarrow 4$	$\epsilon, \Gamma, \Gamma_u$
S	$5 \rightarrow 4$	$\epsilon, \Gamma, \Gamma_u$
Ca	$6 \rightarrow 5$	Γ_u
Ti	$6 \rightarrow 5$	Γ_u
Ba	$9 \rightarrow 8$	Γ_u
W	$10 \rightarrow 9$	$\epsilon, \Gamma, \Gamma_u$
Pb	$10 \rightarrow 9$	$\epsilon, \Gamma, \Gamma_u$

Only 23 measurements !!

Σ^- -nucleus potentials fitted to the Σ^- -atomic data

DD-A'

Density-dependent (DD) potential C.J.Batty et al., Phys.Rep.287(1997)385

$$2\mu U_\Sigma = -4\pi \left(1 + \frac{\mu}{m}\right) \left\{ \left[b_0 + B_0 \left(\frac{\rho(r)}{\rho(0)}\right)^\alpha \right] \rho(r) + \left[b_1 + B_1 \left(\frac{\rho(r)}{\rho(0)}\right)^\alpha \right] \delta\rho(r) \right\}$$

$\chi^2/N=20.1/23$

$\rho(r) = \rho_p(r) + \rho_n(r)$ $\delta\rho(r) = \rho_n(r) - \rho_p(r)$

RMF

Relativistic mean-field (RMF) potential J. Mares et al., NPA594(1995)311
 $\chi^2/N=18.1/23$

LDA-NF

Local density approximation (LDA) with YNG-NF

D. Halderson, Phys. Rev. C40(1989)2173

$\chi^2/N=20.4/23$

T. Yamada and Y. Yamamoto, PTP. Suppl. 117(1994)241

J. Dabrowski, Acta Phys. Pol. B31(2001)2179

Repulsive

Attractive

LDA-S3

Local density approximation (LDA) with SAP3 (simulates ND)

T.Harada, in: Proceedings of the 23nd INS Symp. 1995, p.211

WS-sh

Shallow Woods-Saxon potential: $(V_0, W_0) = (-10, -9)$ MeV

R.S.Hayano, NPA478(1988)113c

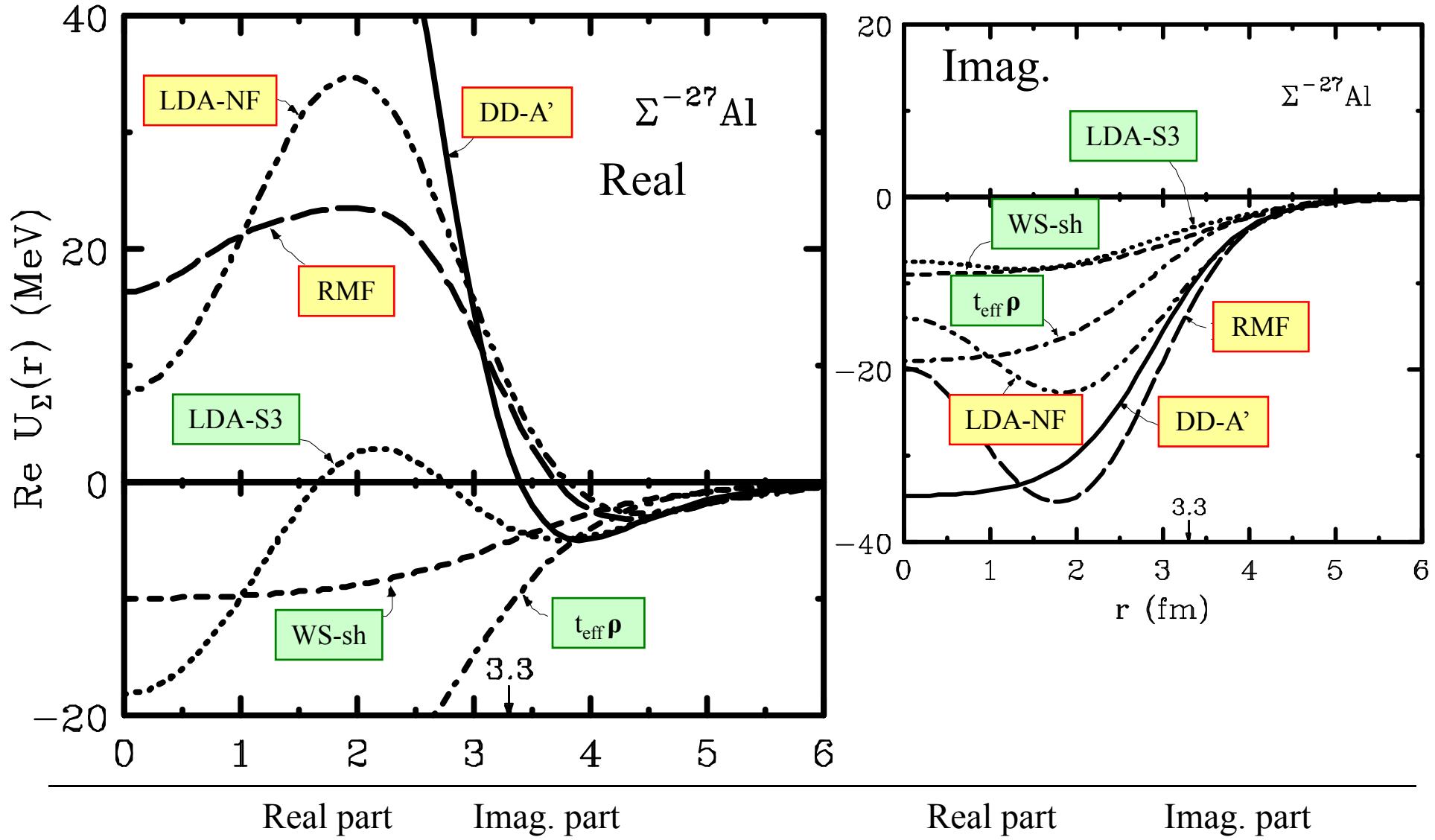
$t_{\text{eff}} \rho$

$t_{\text{eff}} \rho$ -type potential ($B_0=B_1=0$): $a_0=0.36+i0.20$ fm

C.J.Batty, E.Friedman, A.Gal, PTP. Suppl. 117(1994)227

$\chi^2/N=23.1/23$

Σ^- -nucleus optical potentials in $^{27}\text{Al} + \Sigma^-$



Type I

repulsive

strong (30-40MeV)

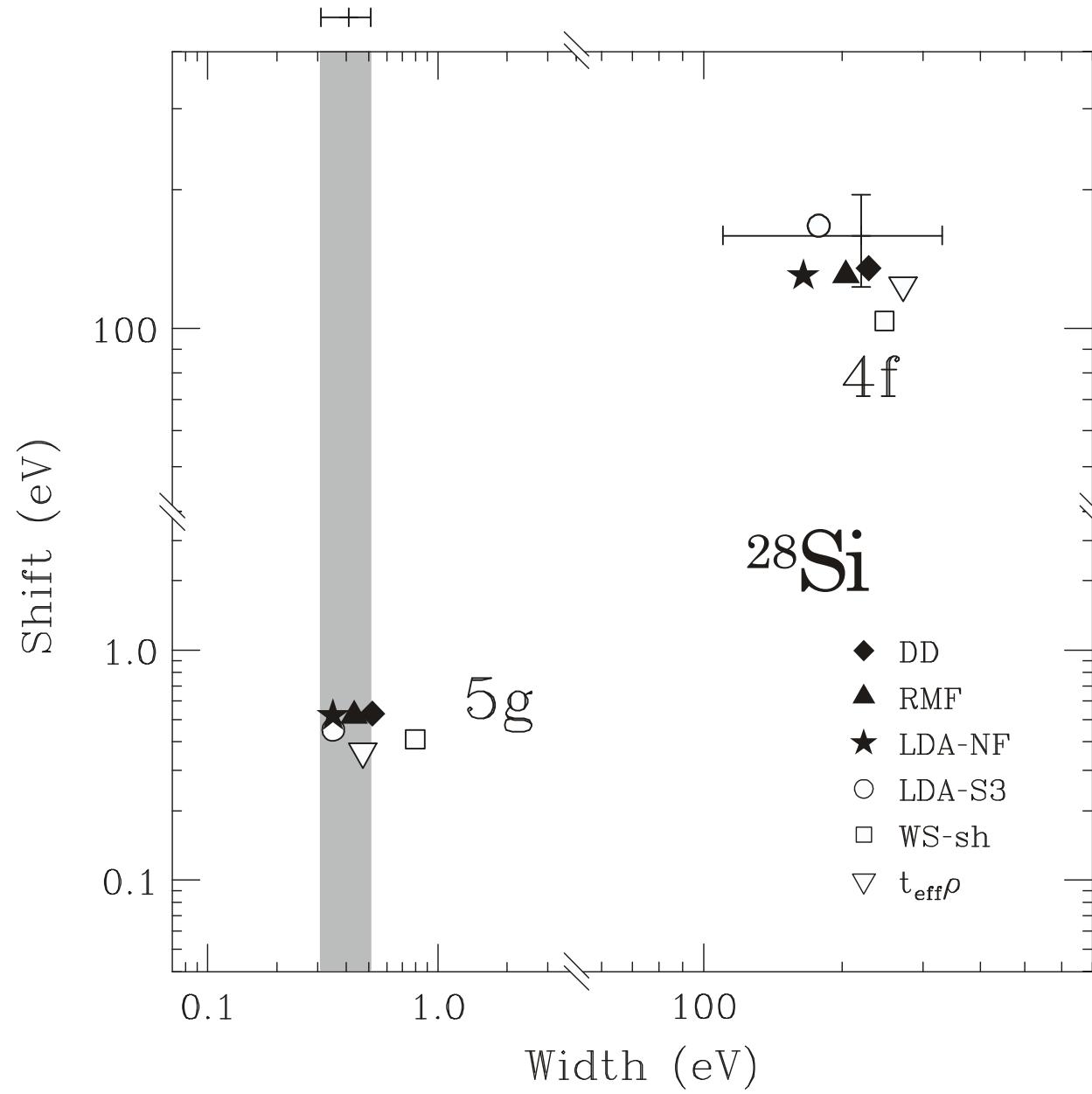
Type II

(weak) attractive

weak (< 10MeV)

Strong-shifts and widths on Σ^- atoms

Σ^- ^{28}Si

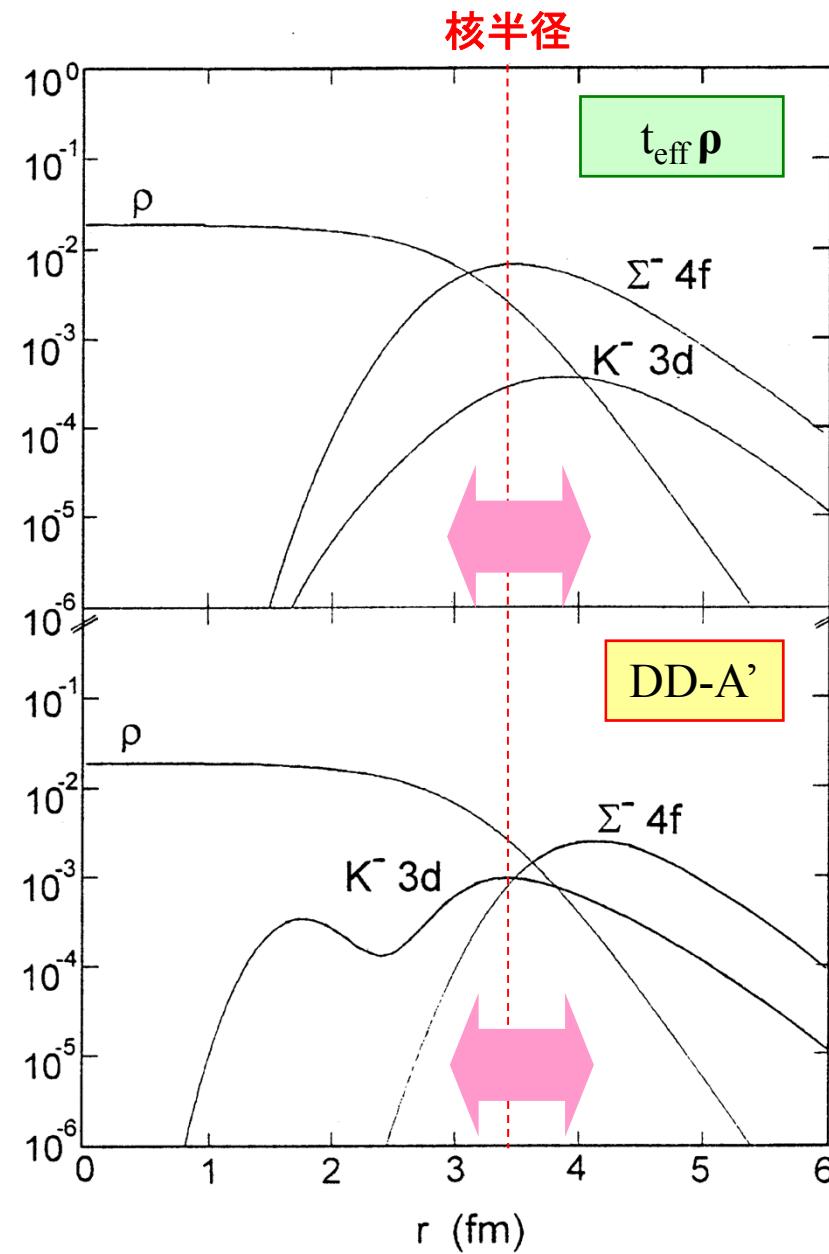


Σ^- 原子のX線データは核のどの領域をみているのか？

32S

C.J. Batty et al.,
Phys.Rep.287(1997)385

Cf. (stopped K^- , π^+)



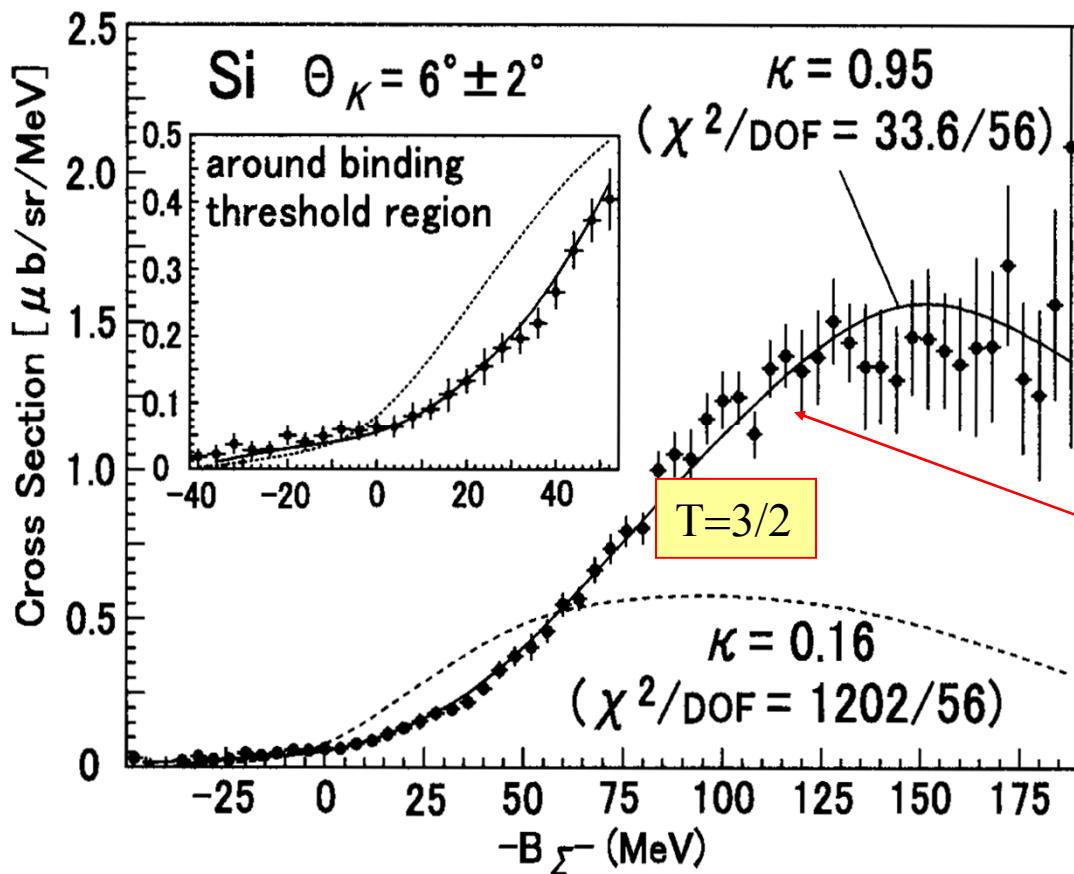
Σ^- spectrum by (π^-, K^+) reaction at 1.2GeV/c

Study of Σ s.p. potential by (π^-, K^+) reactions

Direct Σ production at the nuclear inside

^{28}Si

H.Noumi, et al. PRL89(2002)072301



Targets: ^{28}Si , ^{58}Ni , ^{115}In , ^{209}Bi

Woods-Saxon form

$$U_\Sigma = \frac{V_\Sigma + iW_\Sigma}{1 + \exp[(r - R)/a]}$$

$$R = r_0(A-1)^{1/3} \text{ fm}$$

$$a = 0.67 \text{ fm} \quad r_0 = 1.1 \text{ fm}$$

$V_\Sigma = +150 \text{ MeV}$

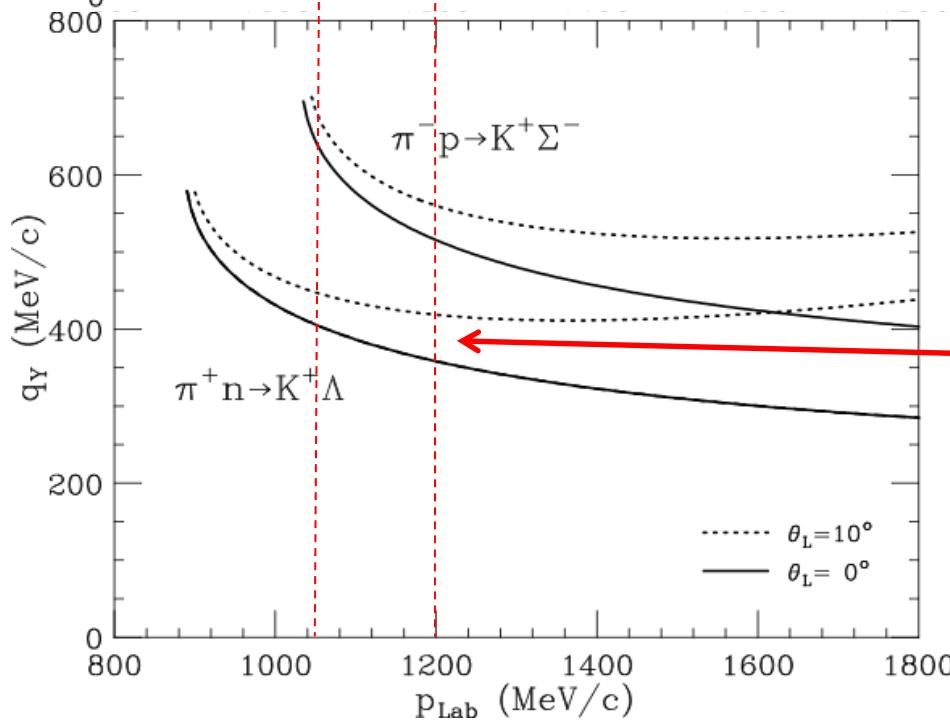
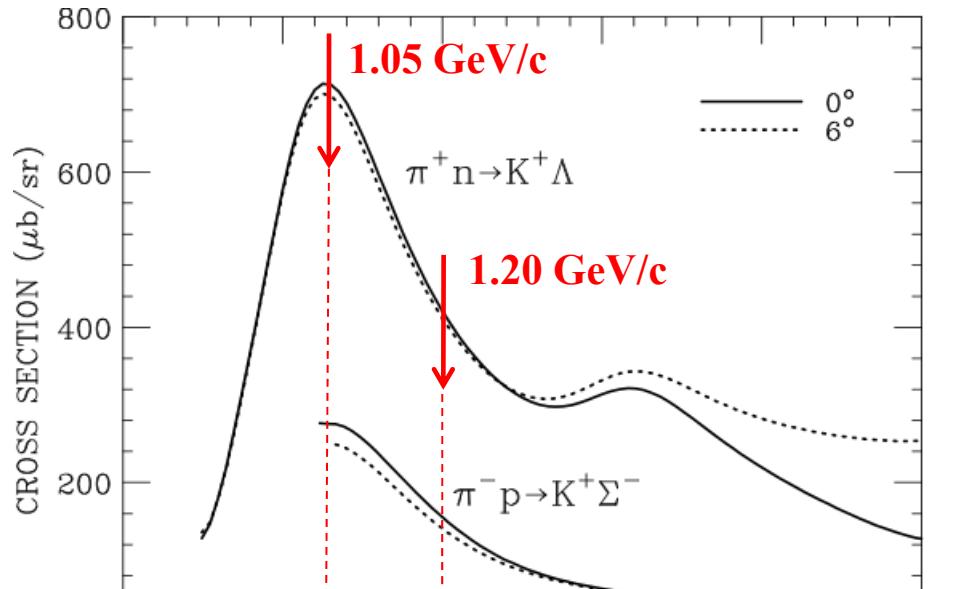
$W_\Sigma = -15 \text{ MeV}$

$+90 \text{ MeV}$

-40 MeV

(Revised)

P.K.Saha, et al., PRC70(2004)044613



Elementary processes of the $\pi^+ p \rightarrow K^+ \Lambda$ and $\pi^- p \rightarrow K^+ \Sigma^-$ reactions

Production cross sections

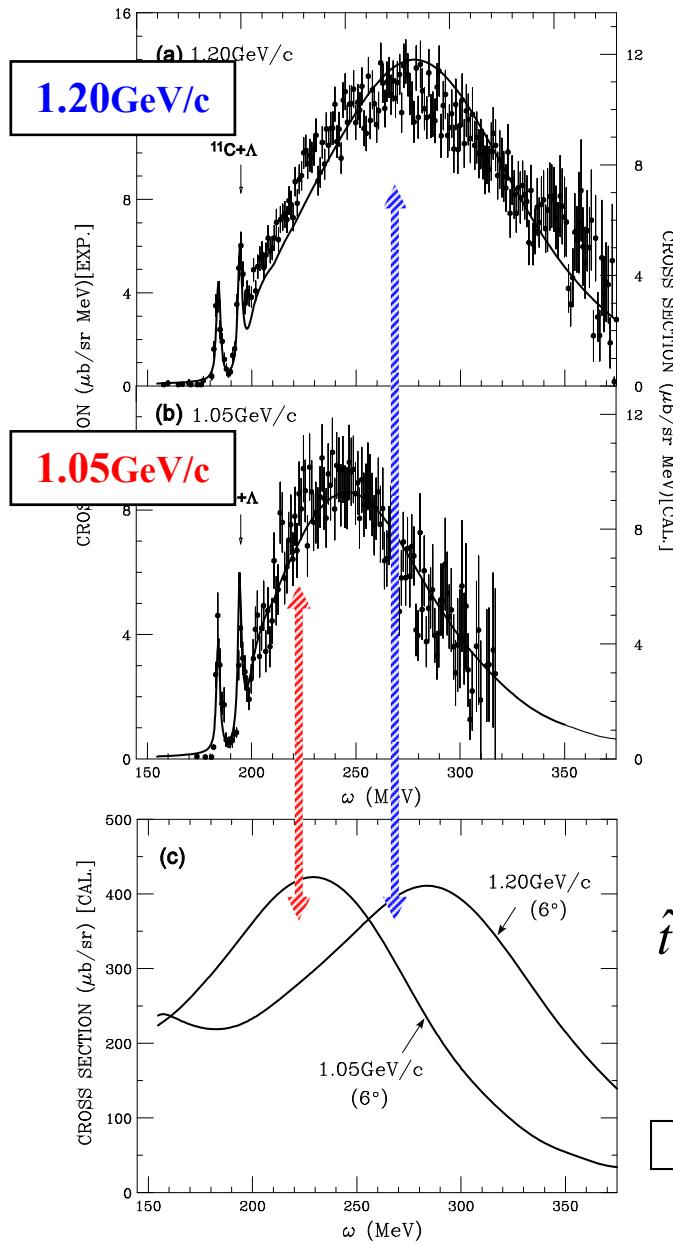
The reason comes from the fact that the cross section at 1.05 GeV/c is larger than that at 1.20 GeV/c .

Large momentum transfer

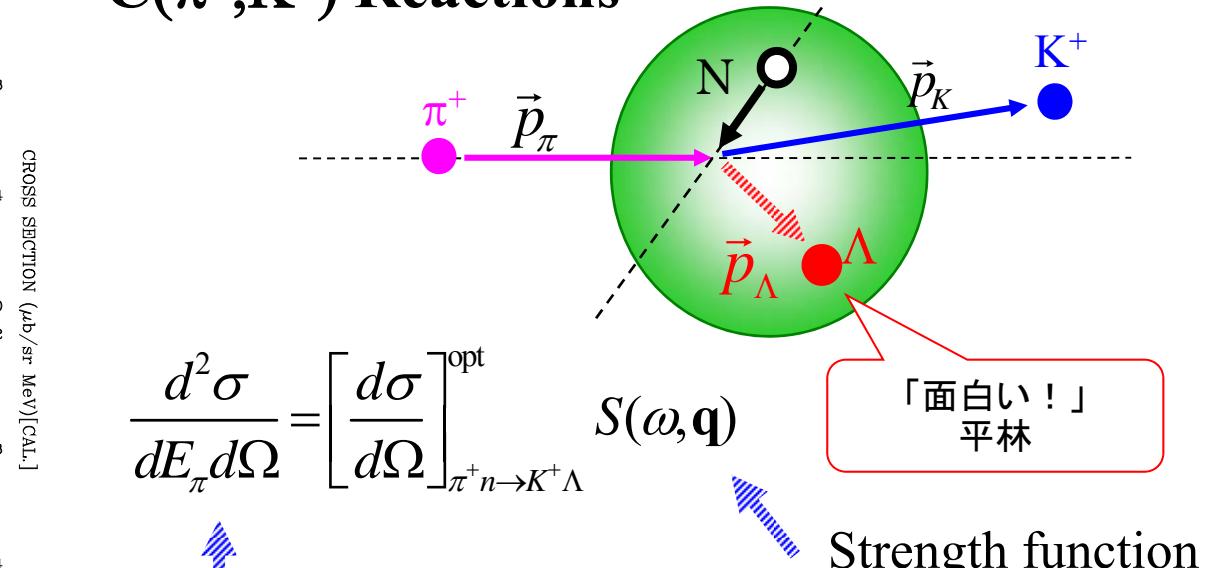
$$q_\Lambda \approx 400 \text{ MeV/c}$$

Optimal Fermi-averaging for an elementary t-matrix

T. Harada and Y. Hirabayashi, NPA744 (2004) 323.



$^{12}\text{C}(\pi^+, \text{K}^+)$ Reactions



“Optimal Fermi-averaging” t-matrix

$$\hat{t}^{\text{opt}}(p_\pi; \omega, \mathbf{q}) = \frac{\int_0^\pi \sin \theta d\theta \int_0^\infty p_N^2 dp_N \hat{t}_{\text{Lab}}(E_{\pi N}; p_\pi, p_N) \rho(p_N)}{\int_0^\pi \sin \theta d\theta \int_0^\infty p_N^2 dp_N \rho(p_N)} \Bigg|_{\mathbf{p}_N = \mathbf{p}_N^*}$$

実験データのエネルギー依存性をよく説明する

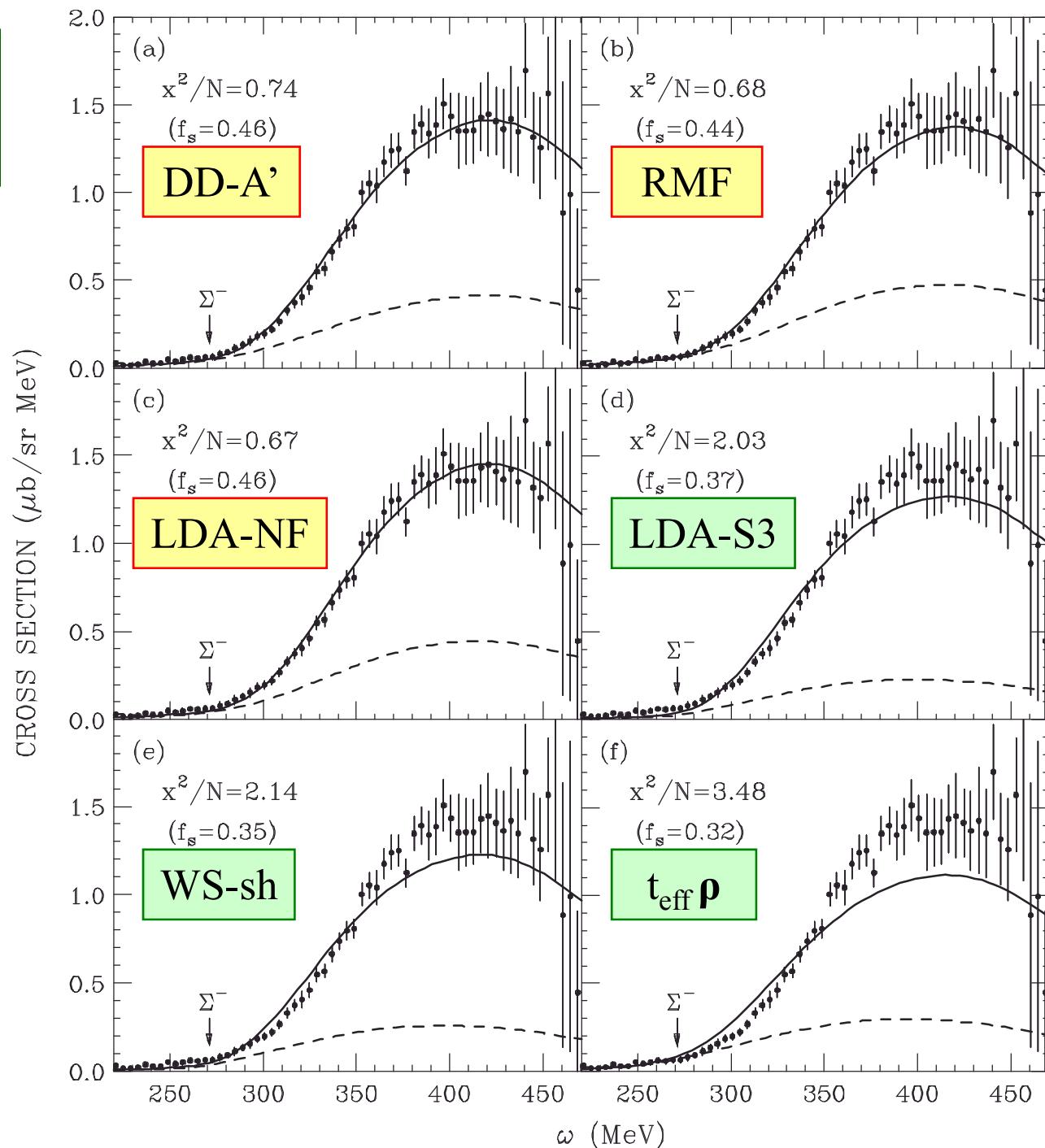
**(π^-, K^+) reaction
at 1.2GeV/c**

^{28}Si

Σ^-

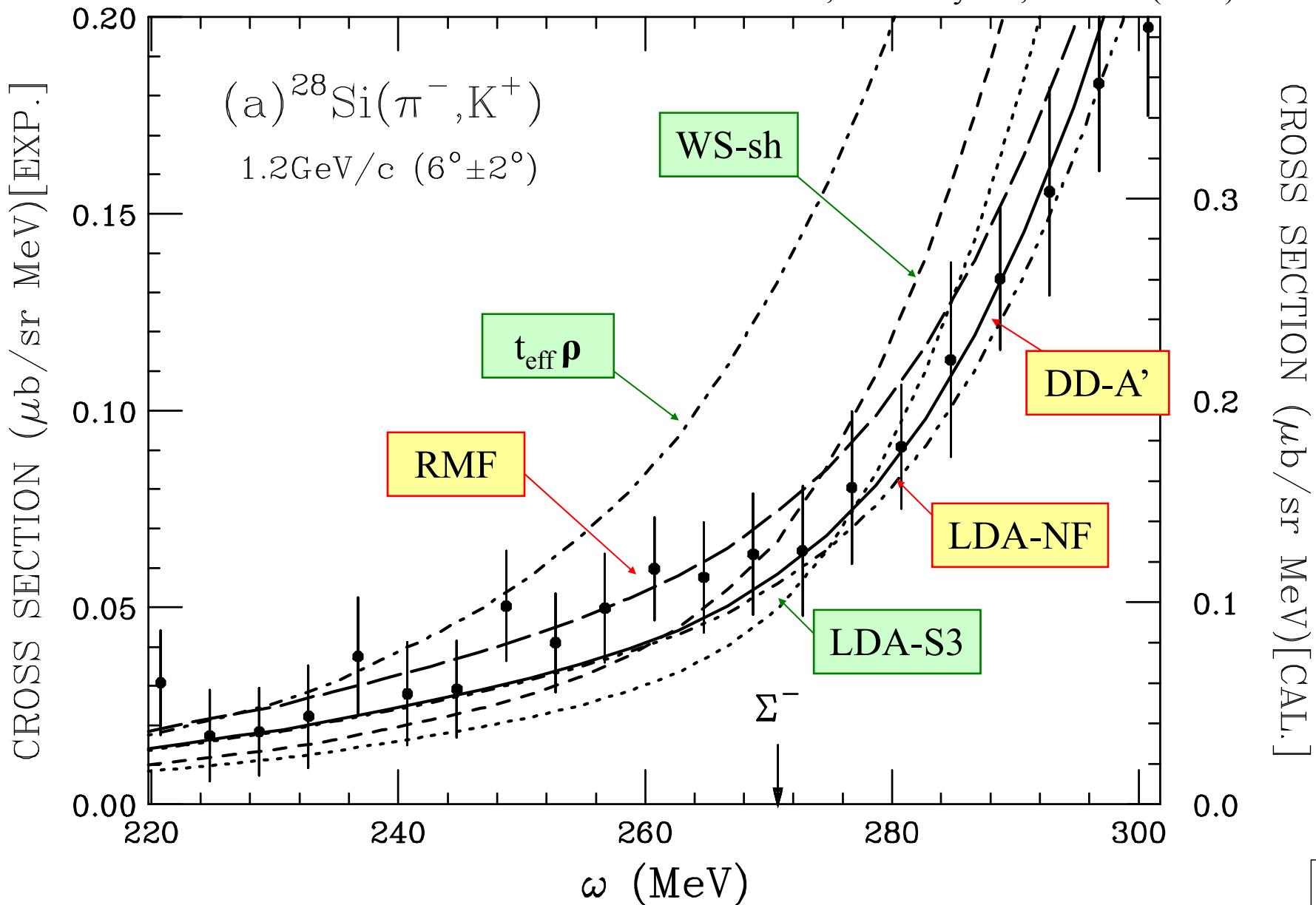
DWIA analysis with
the optimal Fermi-averaging

T.Harada, Y.Hirabayashi,
NPA759 (2005) 143



Σ^- spectrum by (π^-, K^+) reaction at 1.2GeV/c

T.Harada, Y.Hirabayashi, NPA759 (2005) 143



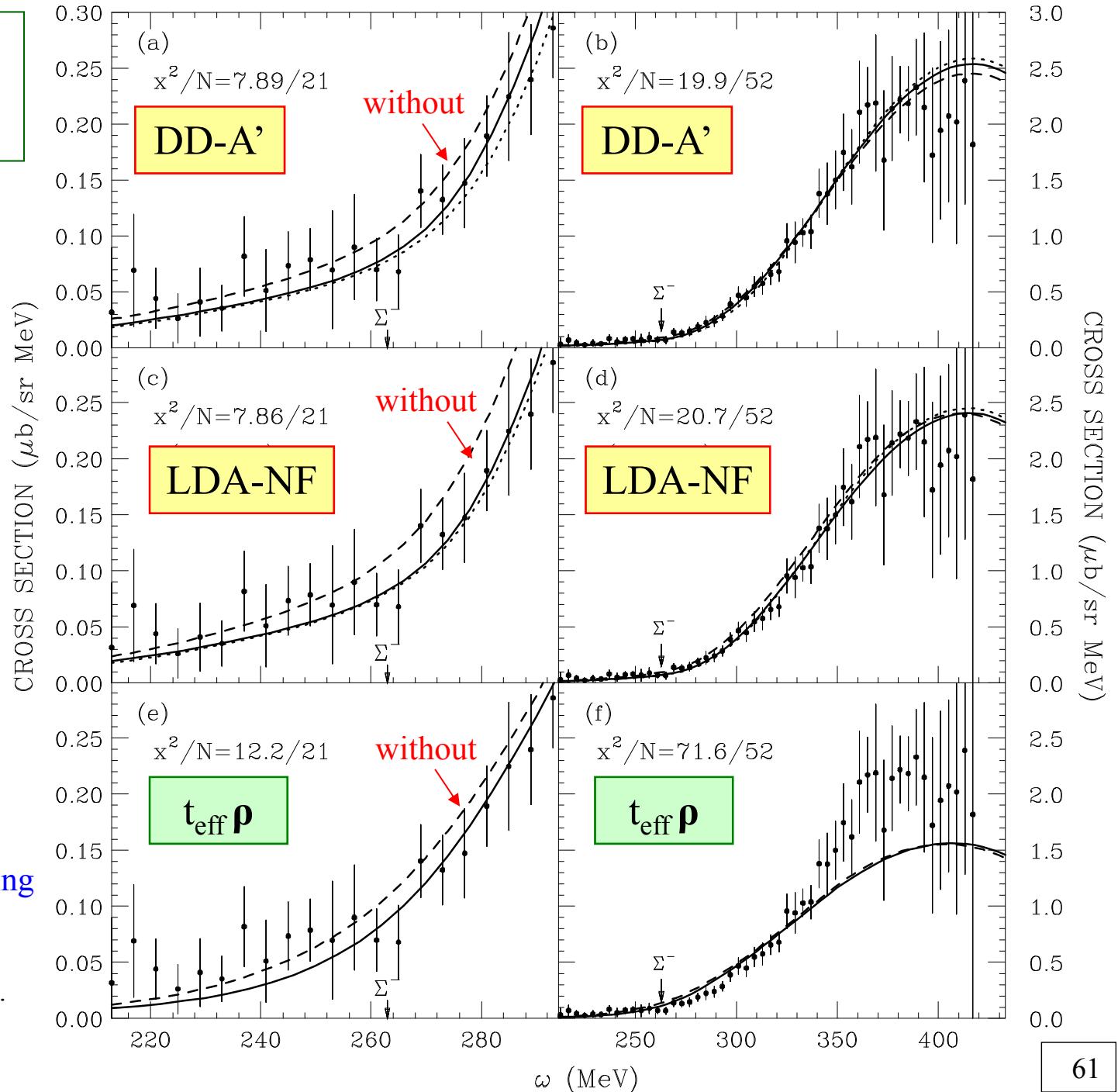
**(π^-, K^+) reaction
at 1.2GeV/c**

^{209}Bi

Σ^-

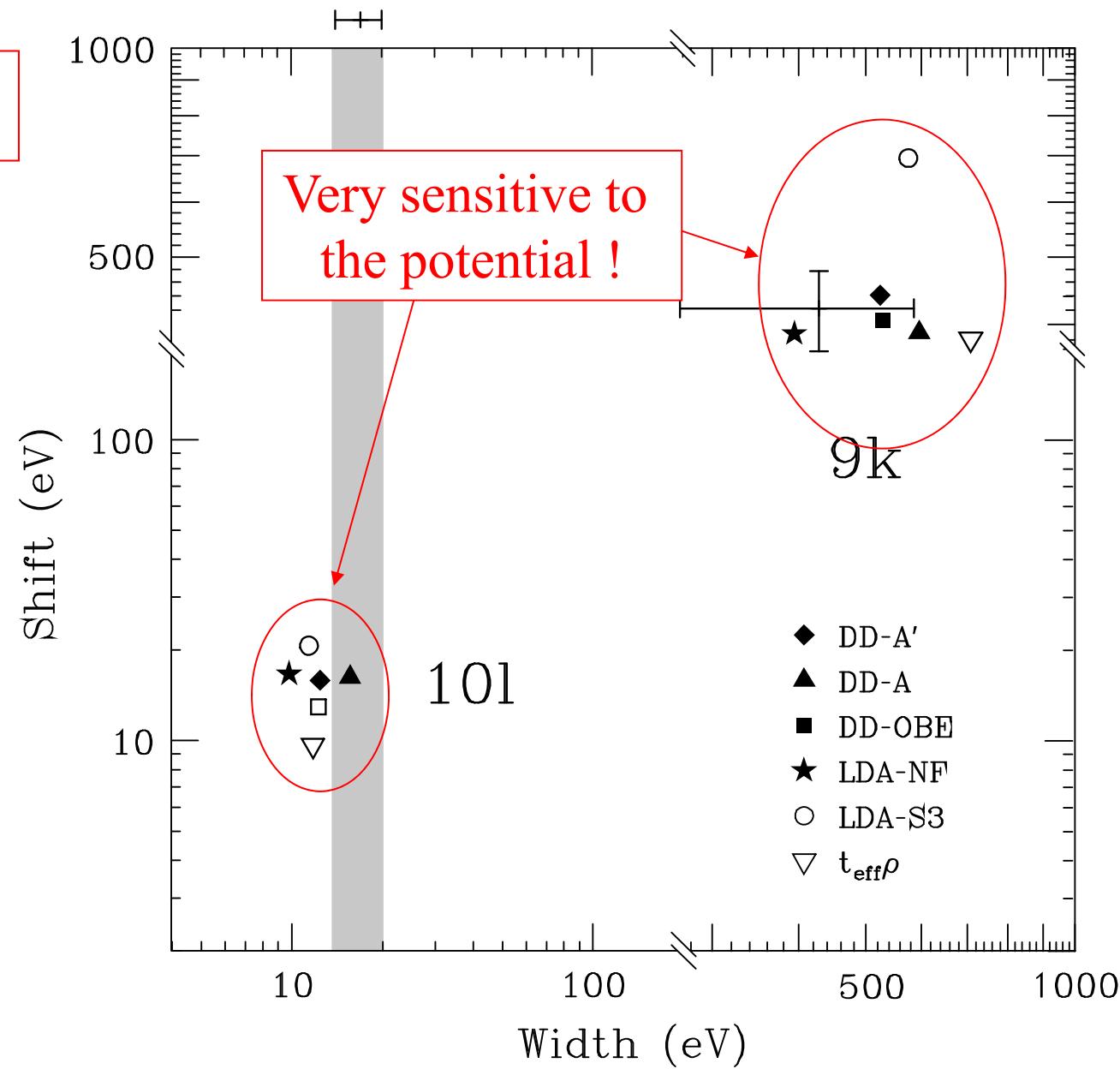
DWIA analysis with
the optimal Fermi-averaging

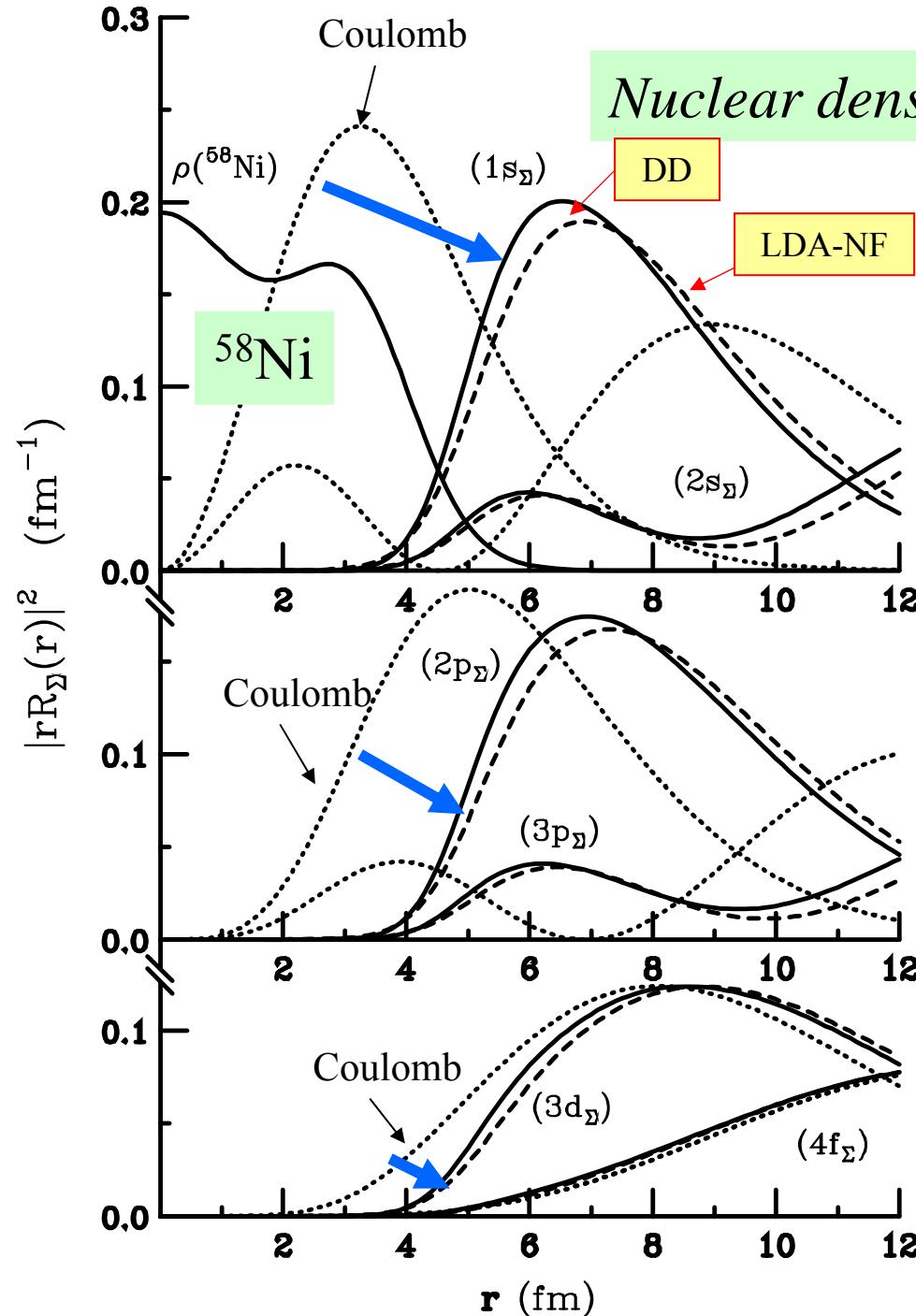
T.Harada, Y.Hirabayashi,
Nucl. Phys. A767 (2006)206.



Strong-shifts and widths on Σ^- atoms

$\Sigma^- \text{ } 208\text{Pb}$





Attraction:
Coulomb-assisted
+
Repulsion:
push out the Σ -wave functions.

Narrow Σ^- bound state !!

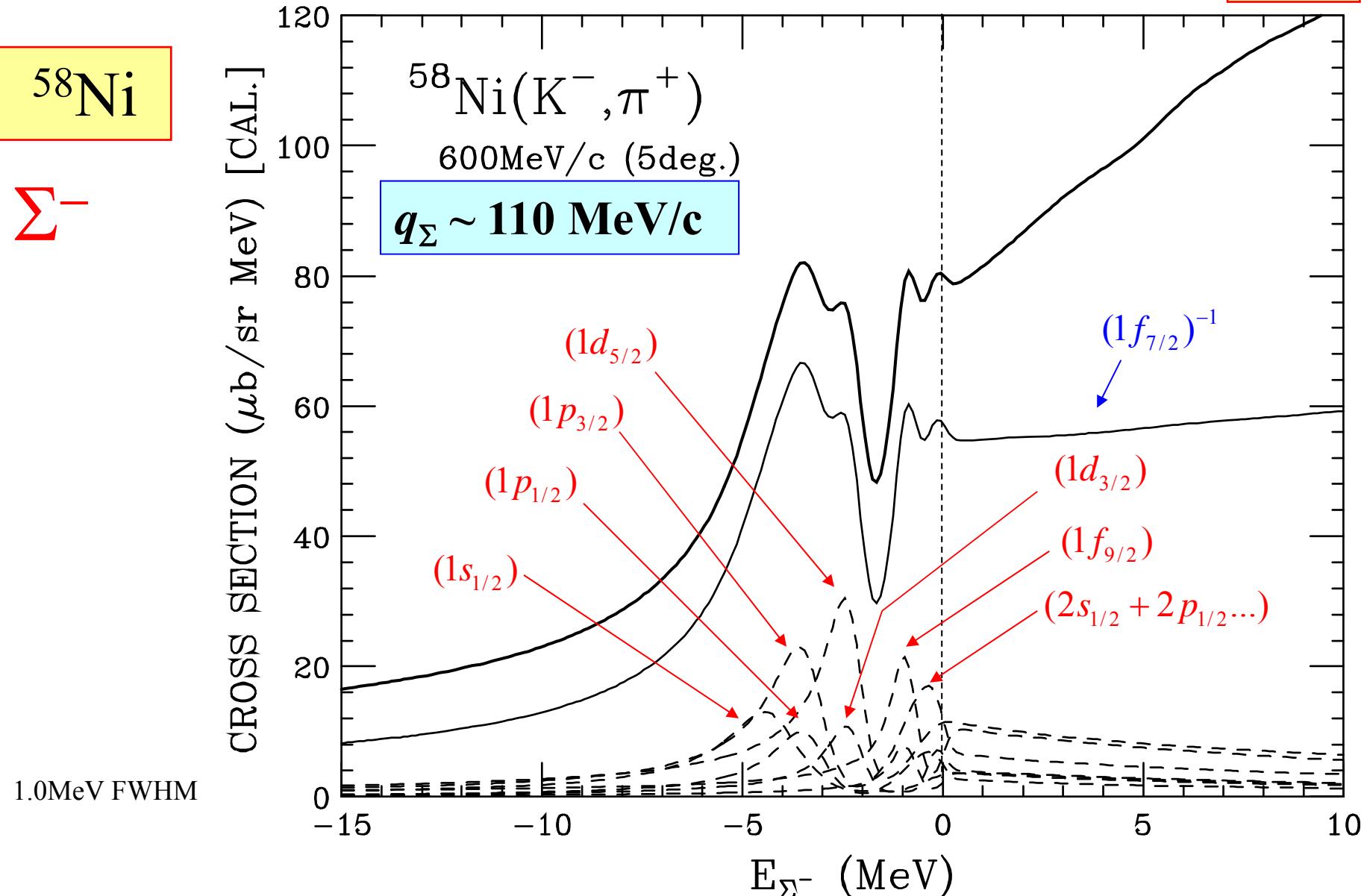
Cf. deeply pionic atoms

Σ^- substitutional states by (K^-, π^+) reaction (I)

DD-A'

^{58}Ni

Σ^-



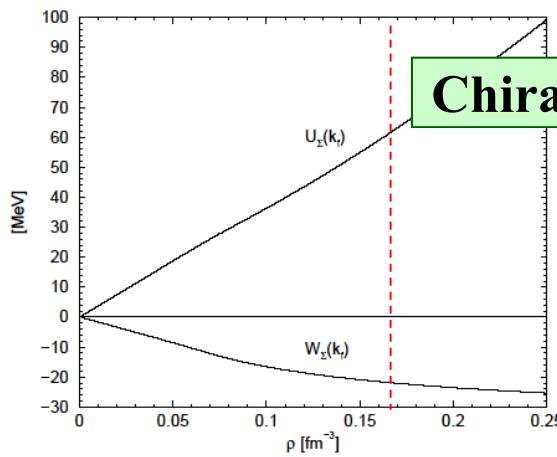
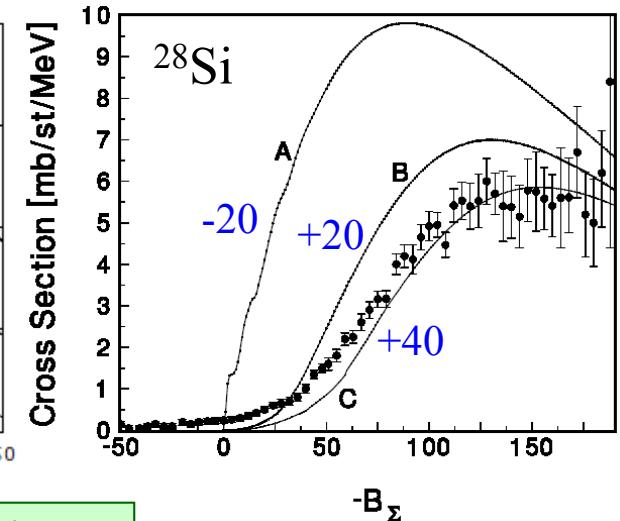
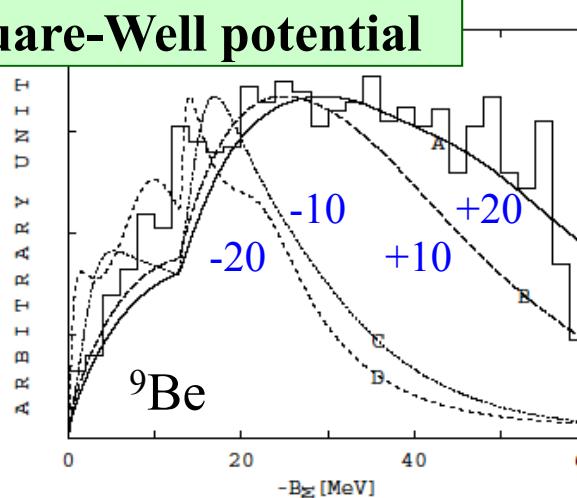
The recoilless reaction provides to produce a promising Σ^- bound state.

Comparison with resent studies

PWIA Analysis with the Square-Well potential

J. Dabrowski, PRC60 (1999) 025205.
 J. Dabrowski, J. Rozynek, Acta. Phys. Pol. B35 (2004) 2303.

“The Σ s.p. potential is **repulsive** inside nucleus. Only NHC-F is acceptable.”



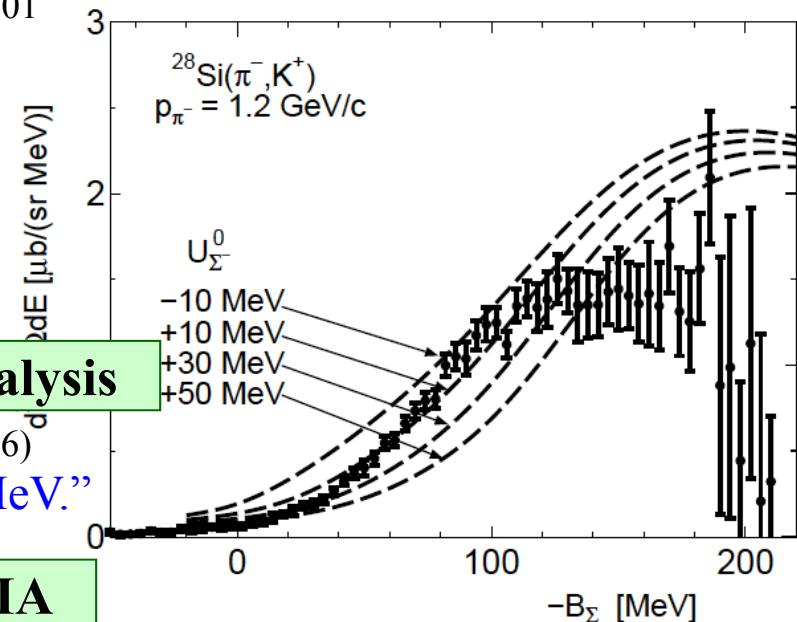
Chiral dynamics in the nuclear medium

N. Kaiser, PRC71 (2005) 068201

$$U_\Sigma(\rho_0) \sim 59 \text{ MeV}$$

repulsive

$$W_\Sigma(\rho_0) \sim -21 \text{ MeV}$$



Semi-Classical Distorted Wave Model Analysis

M. Kohno, Y. Fujiwara, et al., nucl-th/0611080 (2006)

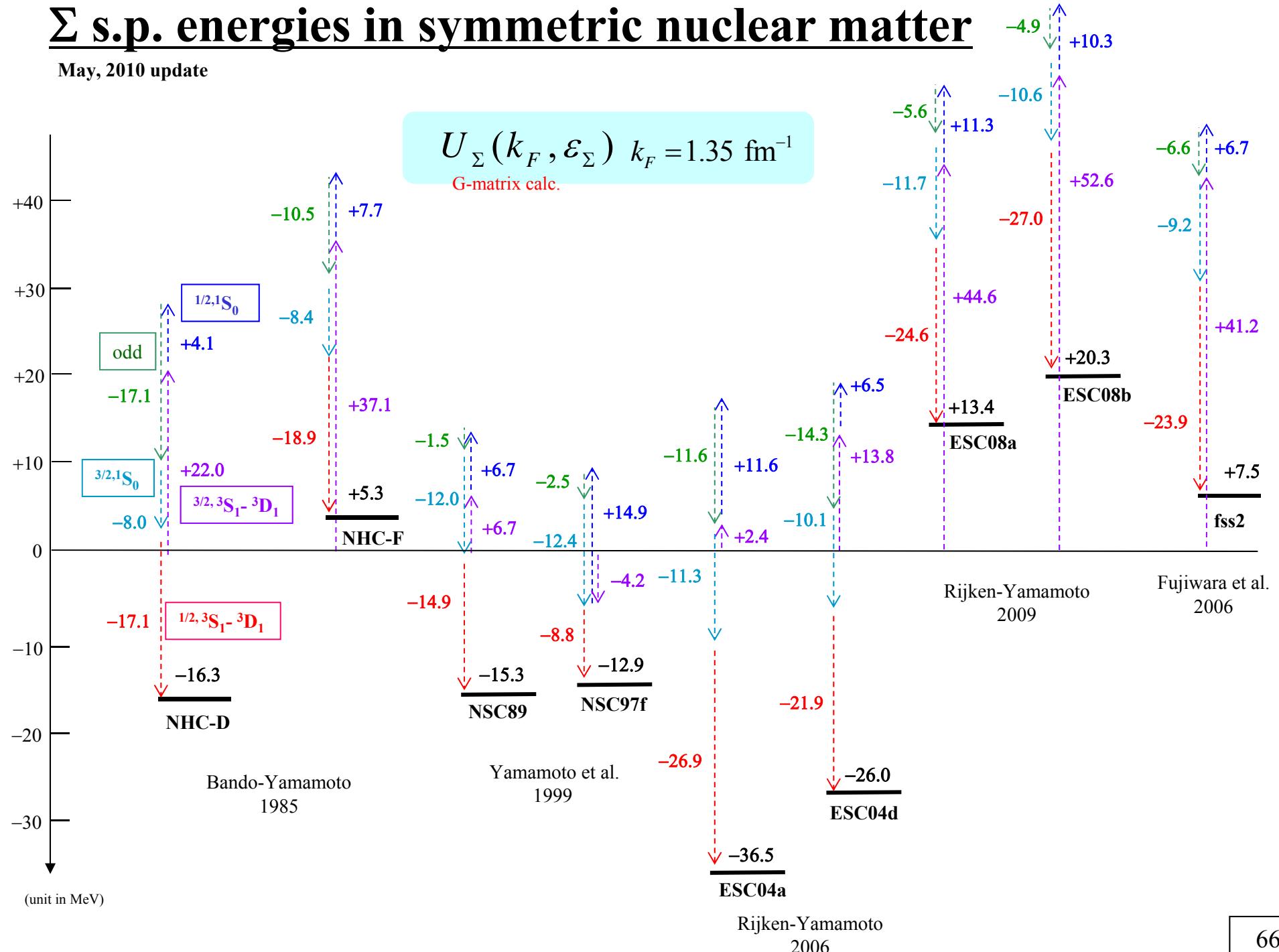
“The repulsive Σ potential is not so strong as ~ 100 MeV.”

Local Optimal Fermi-averaged t-matrix DWIA

H. Maekawa, A. Ohnishi, et al., Eur.Phys.J.A33(2007)269.

Σ s.p. energies in symmetric nuclear matter

May, 2010 update



シグマハイパー核の諸問題(1980s-)

- シグマハイパー核は存在するのか？

狭い幅の状態の問題は?  存在しない！

$\Sigma N(T=1/2, ^3S_1)$ の束縛状態は?  カスプ状態か

$A=4$ の束縛状態の存否は?  存在した(確立)

- Σ ポテンシャルは引力か斥力か？

シグマ原子のX線データ v.s.  斥力らしい

(π^-, K^+) 反応によるシグマ生成スペクトル

- ラムダ核における Σ 混合の割合は?  <1%?

- アイソスピニンは良い量子数か?  OK?

- スピン-軌道力の大きさは?  ??

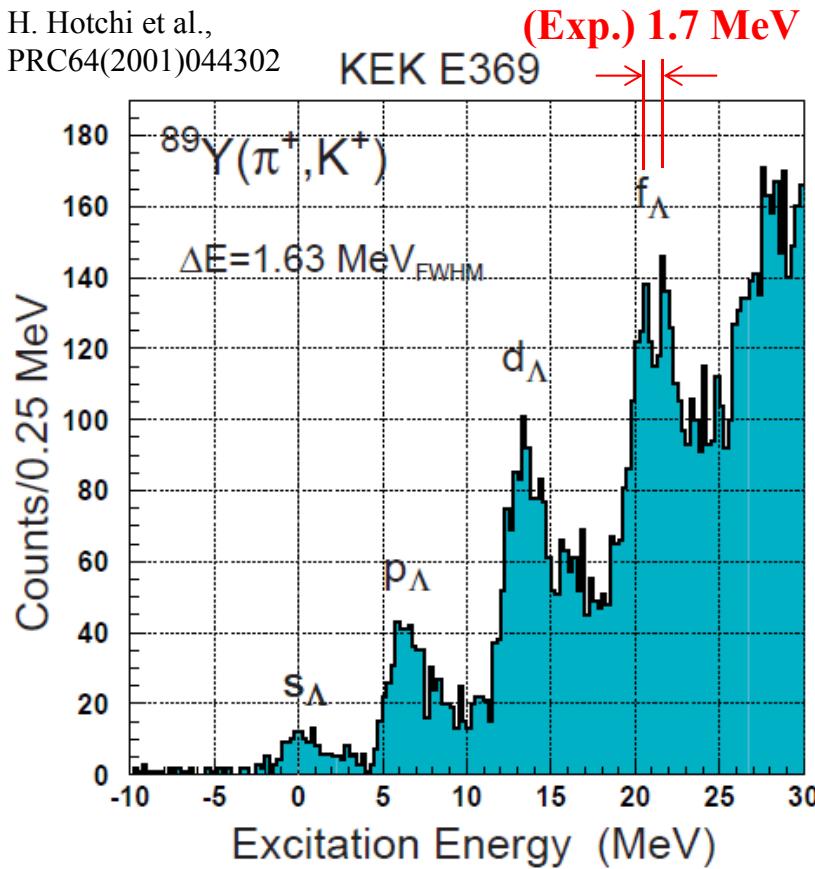
3. Λハイパー核

Λ ハイパー核

- (π^+, K^+) 反応によるハイパー核の生成
芯核の励起状態, ハイパー核らしい状態, etc.
- Λ 粒子の1粒子ポテンシャルとスピン軌道力
- 核内 Λ 粒子の働き
- Gamma-ray spectroscopy of light hypernuclei
- Overbinding Problem on s-Shell Hypernuclei
- 中性子過剰ハイパー核
- Λ ハイパー核の弱崩壊

Λ s.p. potential and Λ spin-orbit splitting in $^{89}\Lambda Y$

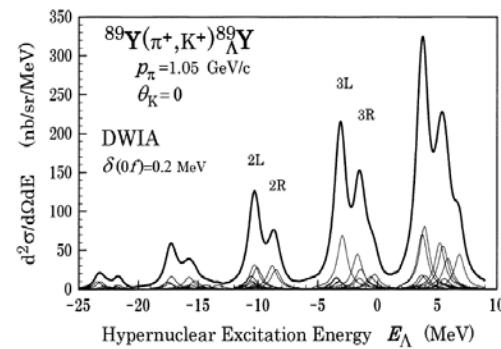
H. Hotchi et al.,
PRC64(2001)044302



T. Motoba et al.,
PTPS185(2010)197

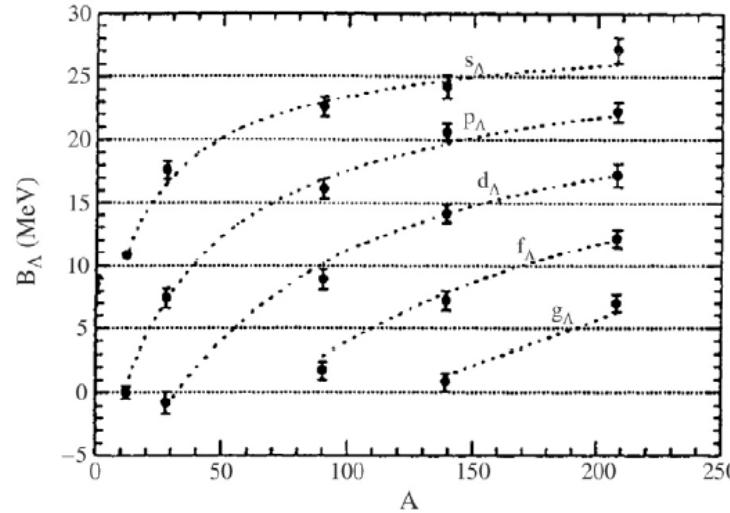
SM analysis
➤ ΛN^{-1} particle-hole ex.
➤ inter-shell coupling

$$V_{LS}^\Lambda \simeq 0.2 \text{ MeV}$$



$$U_\Lambda = V_0^\Lambda f(r) + V_{LS}^\Lambda \left(\frac{\hbar}{m_\pi c} \right)^2 \frac{1}{r} \frac{df(r)}{dr} ls$$

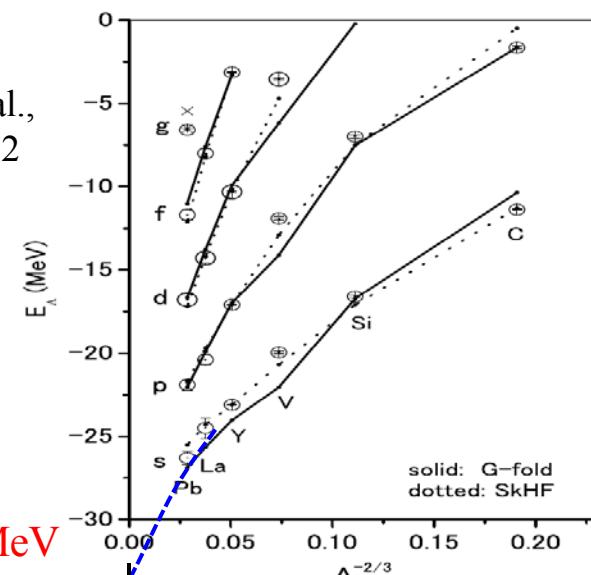
$V_\Lambda ?$



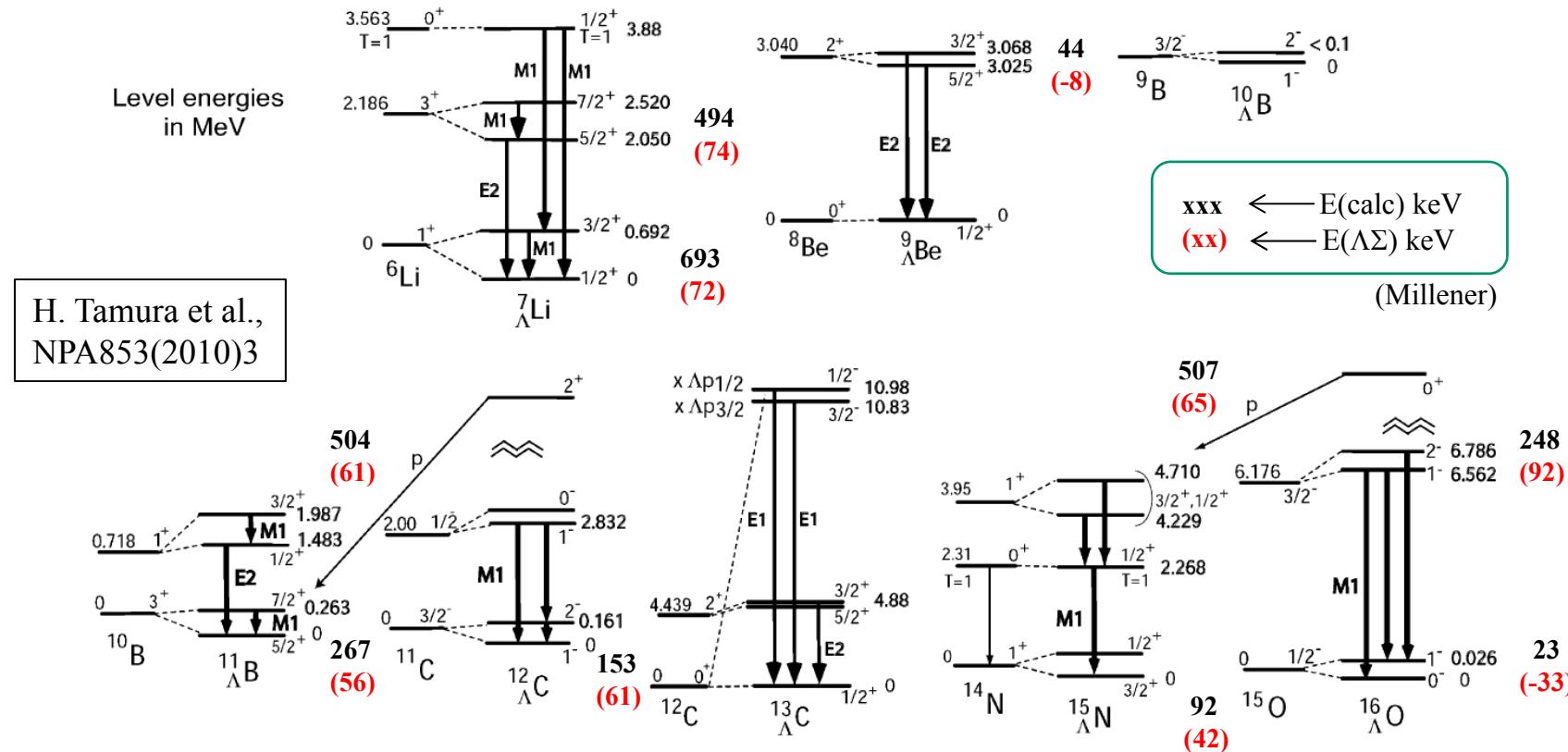
[O. Hashimoto, T. Tamura, PPNP57(2006)564]

Y. Yamamoto et al.,
PTPS185(2010)72

G-matrix
folding model



Gamma-ray spectroscopy of light hypernuclei



Spin-dependence of the effective ΛN interaction

[R.H.Dalitz, A.Gal, AnnPhys.116(1978)167]

$$V_{\Lambda N} = \bar{V} + \Delta \vec{s}_N \cdot \vec{s}_\Lambda + S_\Lambda \vec{l}_N \cdot \vec{s}_\Lambda + S_N \vec{l}_N \cdot \vec{s}_N + T S_{12}$$

Microscopic Shell-Model

$$A = 7, 9 \quad \Delta = 430, \quad S_\Lambda = -15, \quad S_N = -390, \quad T = 30 \text{ (keV)}$$

including $\Lambda N - \Sigma N$ coupling effects

$$A > 9 \quad \Delta = 330, \quad S_\Lambda = -15, \quad S_N = -350, \quad T = 23.9 \text{ (keV)}$$

[D.J.Millener,NPA835(2010)11]

E13@J-PARC

- ΛN spin-dependent force/ $\Lambda N - \Sigma N$ coupling force/Charge symmetry breaking ($\Lambda p \neq \Lambda n$)
- Magnetic moments μ_Λ in a nucleus from $B(M1)$

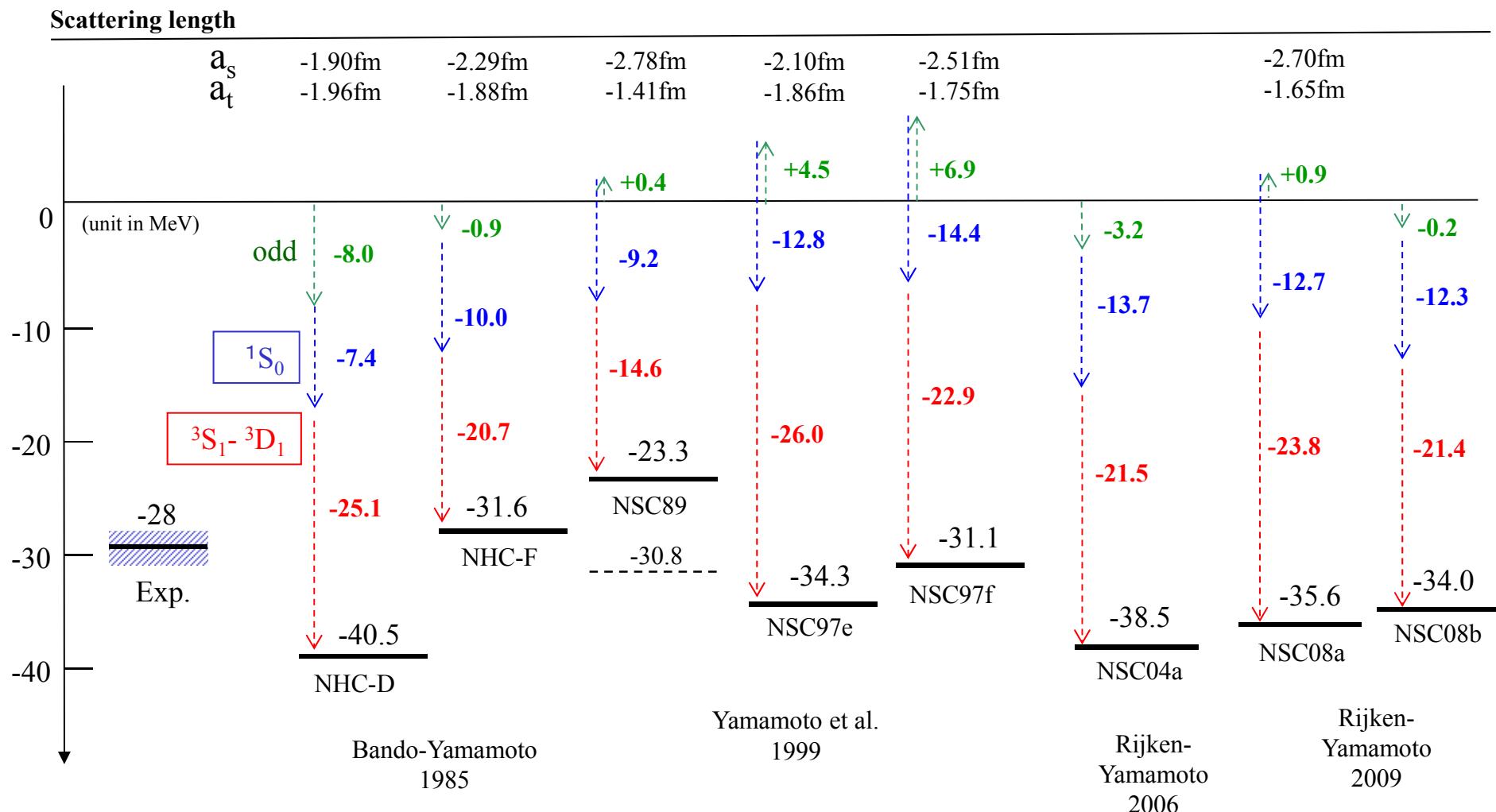
${}^4_\Lambda He, {}^{10}_\Lambda B, {}^{11}_\Lambda B, {}^{19}_\Lambda F$

Λ single-particle energies in symmetric nuclear matter

OBEP: Nijmegen YN potential Models

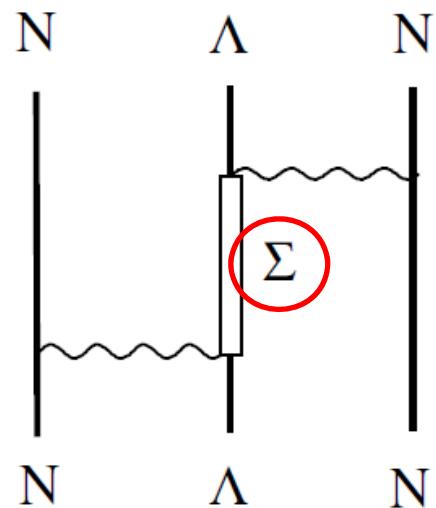
$$U_{\Lambda}(k_F, \varepsilon_{\Lambda}) \quad k_F = 1.35 \text{ fm}^{-1}$$

G-matrix calc. QTQ



Y. Yamamoto, H. Bando, PTP Suppl. 81(1985)9; Y. Yamamoto, et al., PTP Suppl. 117(1994)361;
 Th.A.Rijken, V.G.J.Stoks, Y.Yamamoto, PRC59(1999)21; Th.A.Rijken, Y.Yamamoto, PRC73(2006) 044008;
 Y.Yamamoto, T.Motoba, T.A.Rijken, PTP Suppl. 185(2010)72.

核物質中の Σ ハイペロンの役割

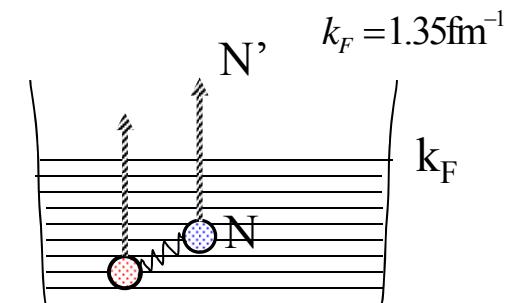


G-matrix calculation in symmetric nuclear matter

Λ single-particle potential depth

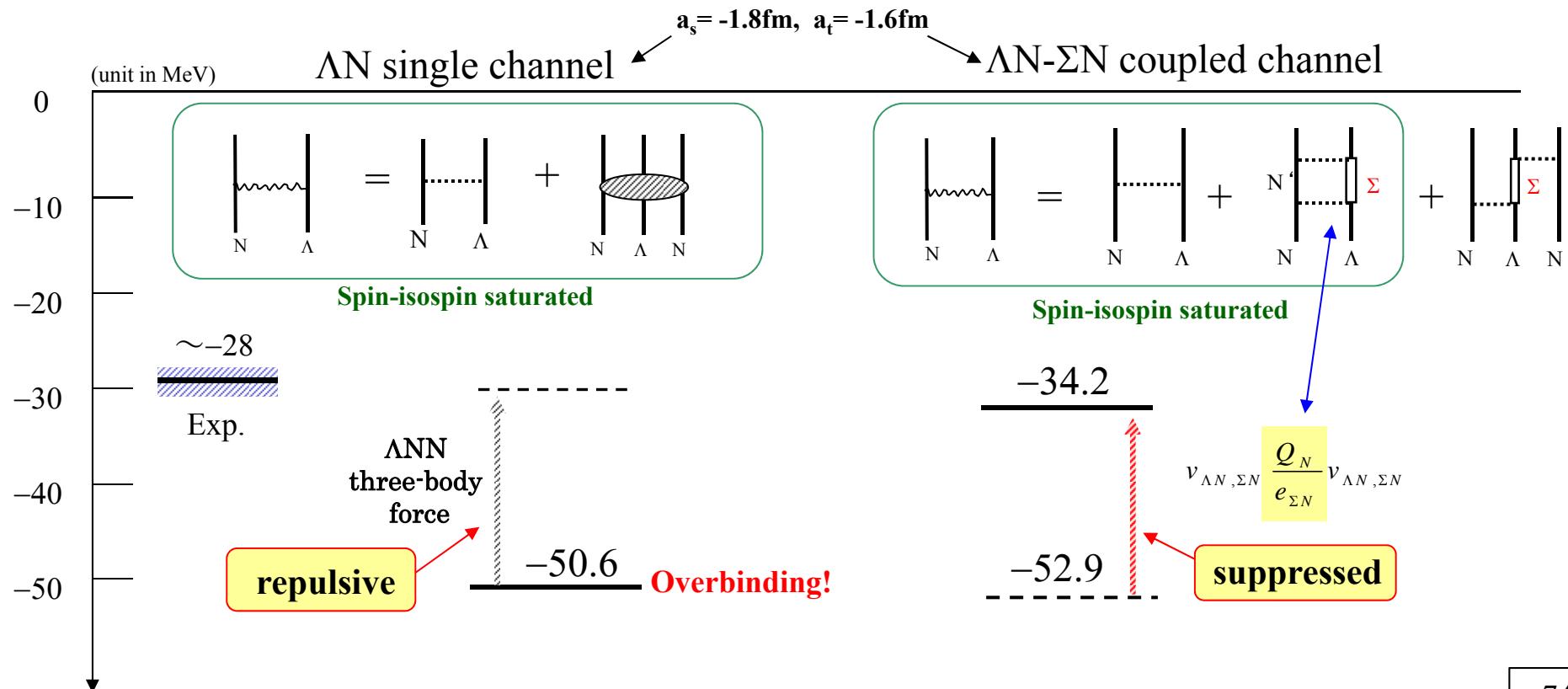
$$U_\Lambda(k_F, \varepsilon_\Lambda) = \sum_{\mathbf{k}_N} \langle \mathbf{k}_\Lambda, \mathbf{k}_N | g_{\Lambda N}(\omega = \varepsilon_\Lambda + \varepsilon_N) | \mathbf{k}_\Lambda, \mathbf{k}_N \rangle$$

$g_{YN}(\omega) = v_{YN} + v_{YN} \frac{Q_N}{\omega - QTQ} g_{YN}(\omega)$
G-matrix Pauli-operator



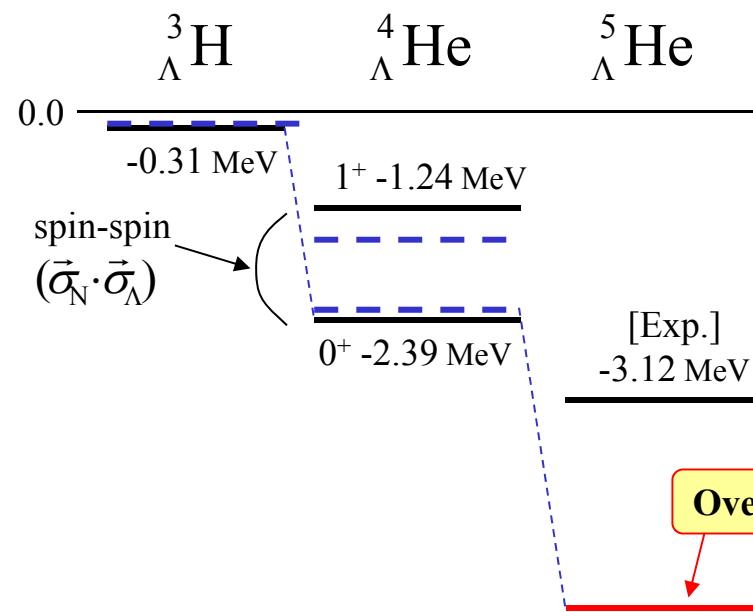
Effects of the $\Lambda N - \Sigma N$ coupling in nuclear matter

Y.Nogami, E.Satoh, NPB19(1970)93

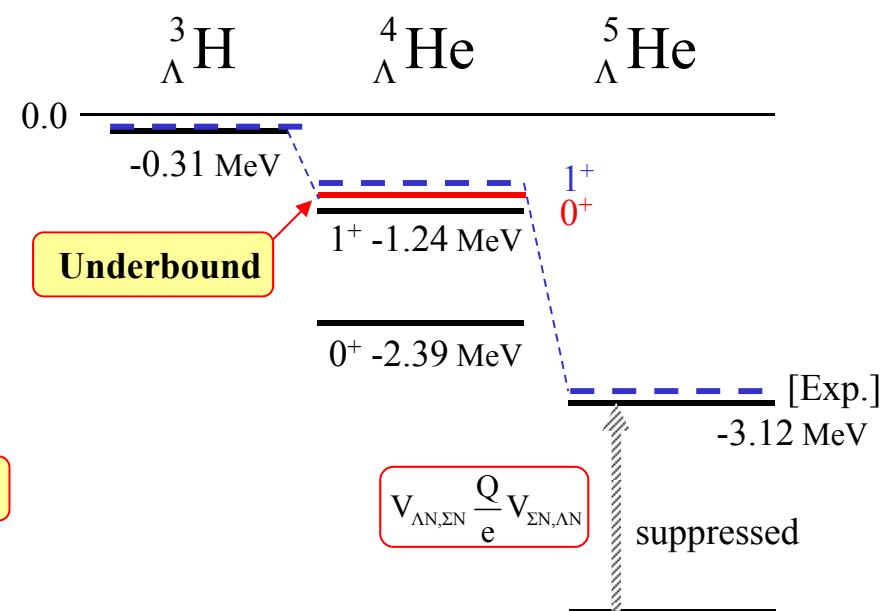


Overbinding Problem on s-Shell Hypernuclei

The Overbinding Problem



The Underbinding Problem



ΛN single-channel calc.

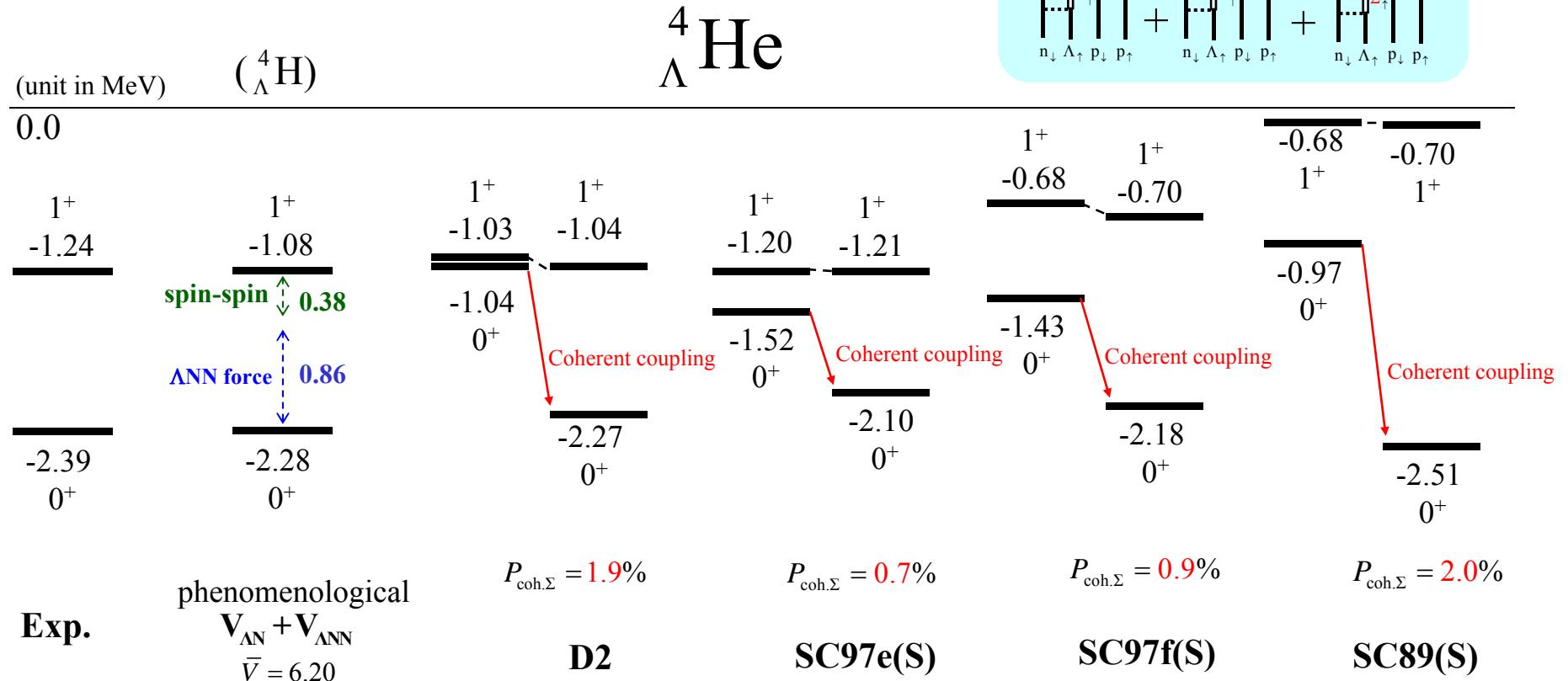
Dalitz et al., NP **B47** (1972) 109.

g-matrix calc. with $\Lambda\text{N}-\Sigma\text{N}(\text{D}2)$

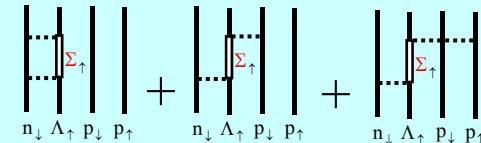
Akaishi et al., PRL **84** (2000) 3539.

“The 0^+-1^+ difference is not a measure of ΛN spin-spin interaction.”
by B.F. Gibson

Hyperon-mixing



ANN three-body force



VMC

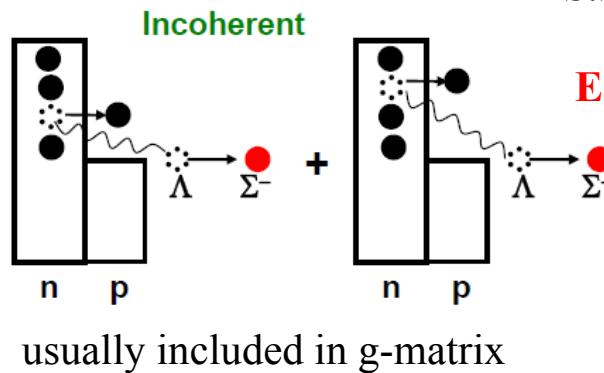
R. Sinha, Q.N.Usmani,
NPA684(2001)586c

Breuckner-Hartree-Fock

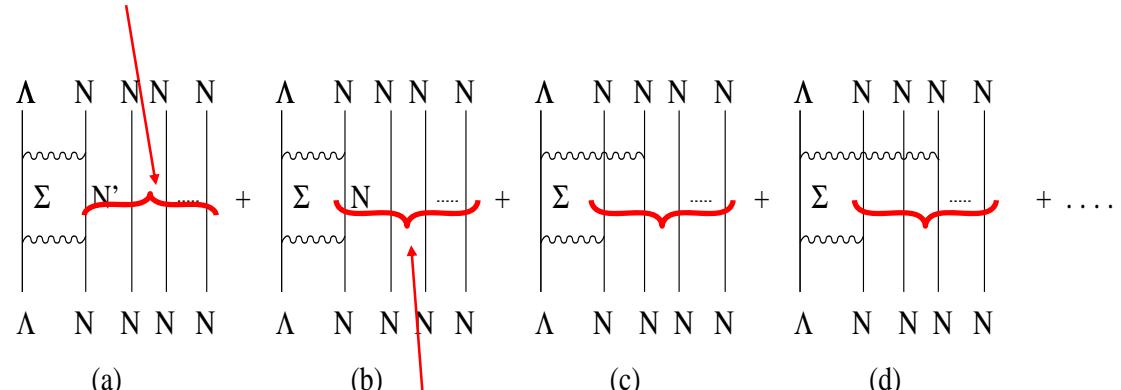
Y. Akaishi, T.Harada, S.Shinmura, Khun Swe Myint,
PRL84(2000)3539

The Λ - Σ coupling effects in neutron matter

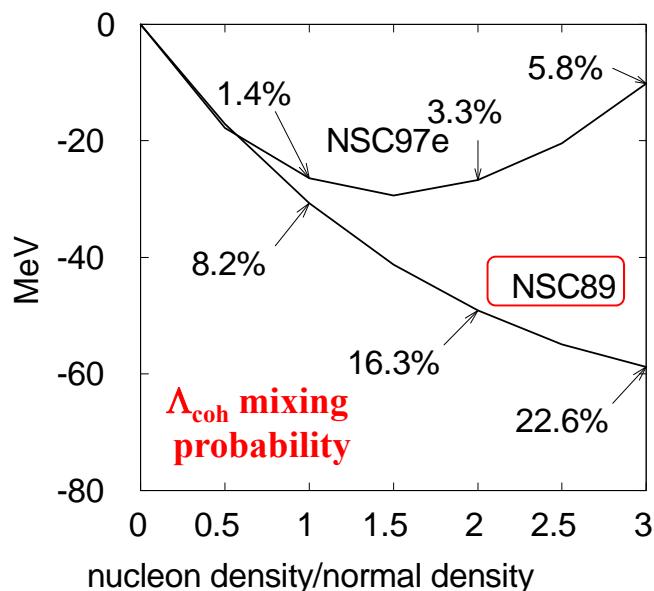
S.Shinmura, Khin Swe Myint, T.H., Y.Akaishi, J.Phys.G28(2002)L1



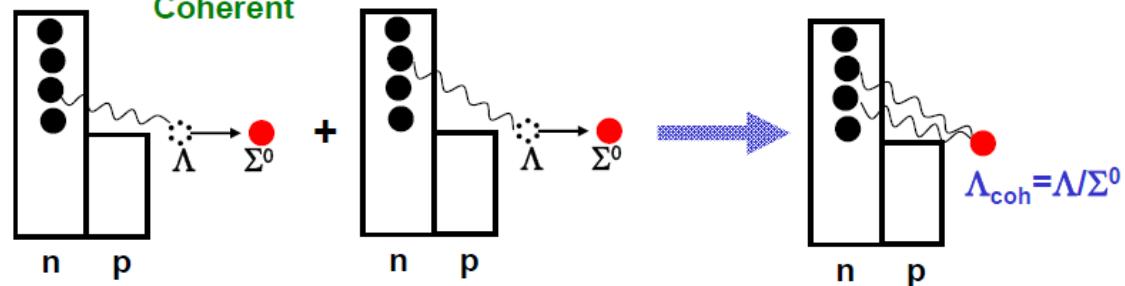
Excited (1p1h) states



Single particle potential for Λ_{coh} .



Coherent

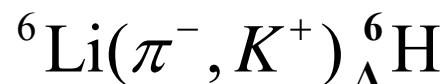


coherent Λ - Σ coupling

The Λ_{coh} mixing is enhanced in the neutron-excess environment.

Production of neutron-rich Λ -hypernuclei with the DCX reaction

E10@J-PARC

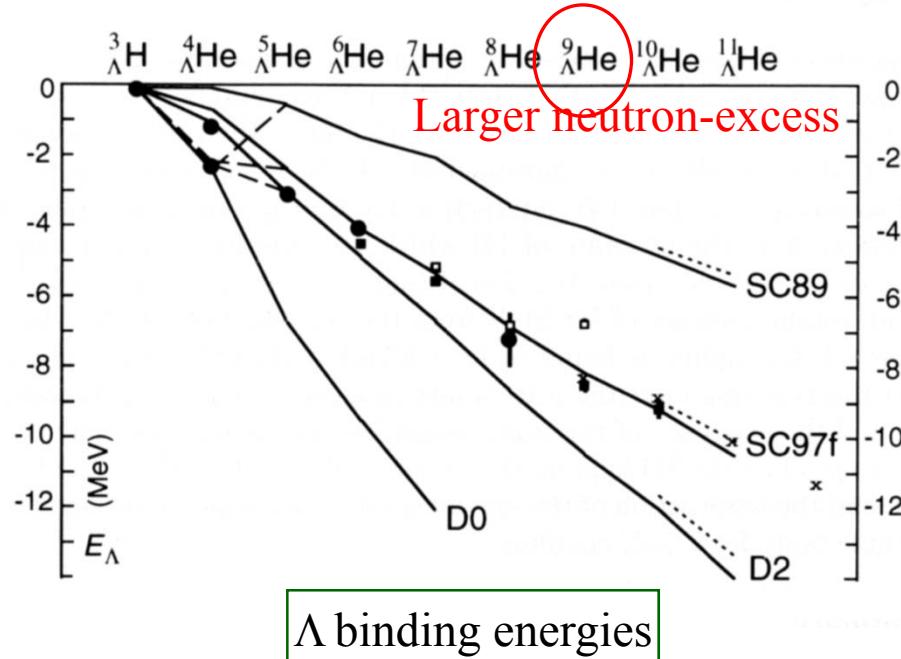


“Hyperheavy hydrogen”

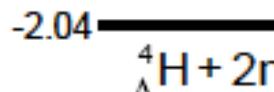
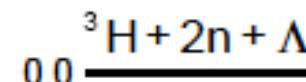
Y.Akaishi, NPA738(2004)80c



Khin Swe Myint et al.,
FBS. Suppl. 12(2000)383

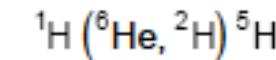


Superheavy hydrogen



Attraction

"Hyperheavy hydrogen"



1.7

-4.4 MeV

-1.4 MeV

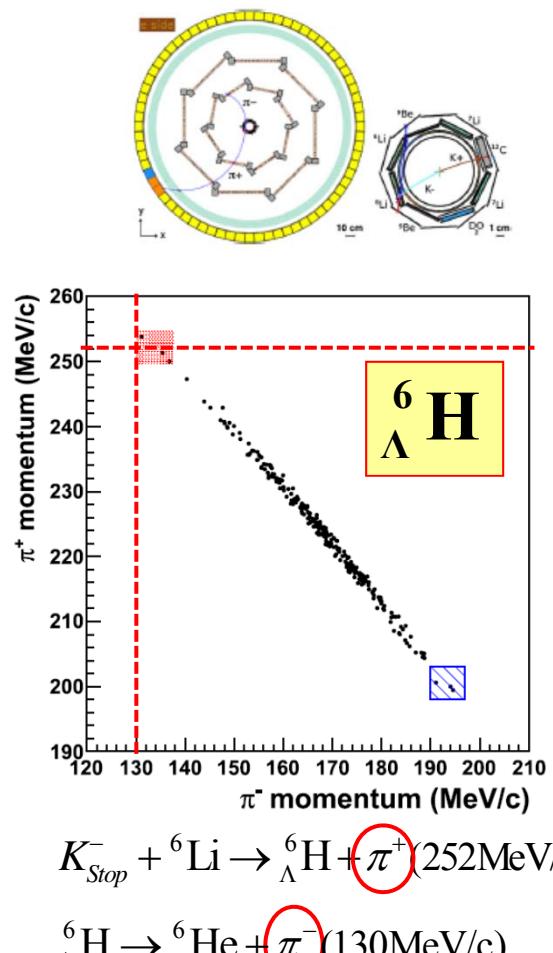
-4.1

Extremely
enhanced

Coherent Λ - Σ
coupling

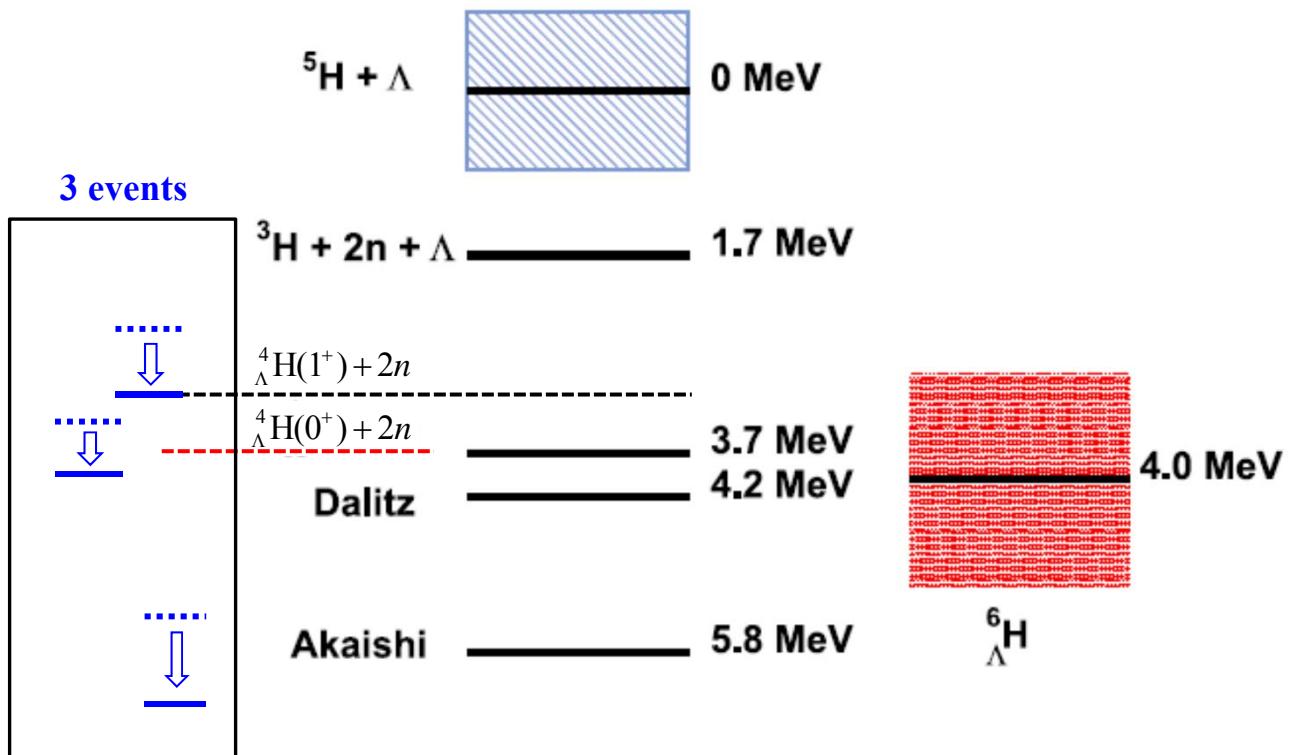
➤ Coherent Λ - Σ coupling in neutron-excess environment

First observation of the superheavy hydrogen ${}^6_{\Lambda}\text{H}$



M. Agnello et al., NPA881(2012)269.
M. Agnello, et al., PRL108 (2012) 042501.

- observation of 3 candidate events of ${}^6_{\Lambda}\text{H}$ bound state
 $B_A = 4.0 \pm 1.1 \text{ MeV}$
- $\text{BR}(\text{DCX}) / \text{BR}(\text{NCX}, 12\text{LC}) \sim 3 \times 10^{-3}$
 $R = (5.9 \pm 4.0) \cdot 10^{-6} / K_{\text{stop}}$

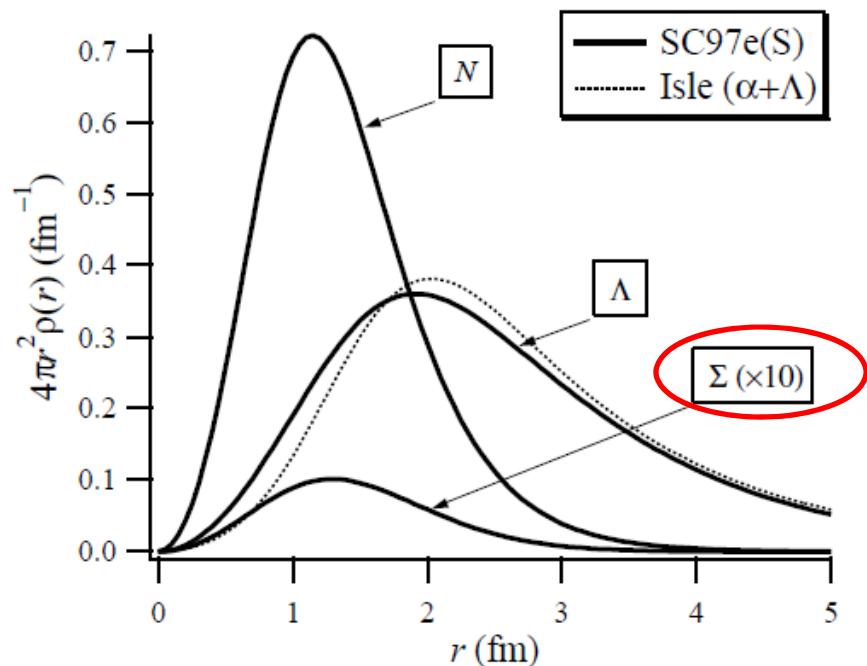


→ E10@J-PARC

- Produce neutron-rich hypernuclei: ${}^6_{\Lambda}\text{H}$ and ${}^9_{\Lambda}\text{He}$
- precise measurement of B.E. of ${}^6_{\Lambda}\text{H}$ is possible

Ab initio calculation of ${}_{\Lambda}^5\text{He}$ with full realistic interactions

H.Nemura et al., PRL89(2002)142504



Better understanding of the Λ - Σ coupling and Tensor force

Hyperon-mixing

α^* $T_C = 1 \otimes \Sigma$ ~ 1.5 % admixture

“Incoherent Λ - Σ coupling”

$$\alpha \quad T_C = 0 \otimes \Lambda$$

- The Σ admixture of ~1.5 % appears in ${}_{\Lambda}^5\text{He}$.
- The α -particle is not a rigid core.



The incoherent Σ admixture is also important.

	$L = 0$		$L = 2$		
	$S = \frac{1}{2}$	$S_c = 0$	$S = \frac{3}{2}$	$S_c = 1$	$S = \frac{5}{2}$
${}_{\Lambda}^5\text{He}$					
$(T_c = 0) \otimes \Lambda$	89.14	0.03	0.19	3.74	5.36
$(T_c = 1) \otimes \Sigma$	0.10	0.09	1.34	~ 0	0.01
${}^4\text{He}$	89.56			10.44	

The Λ - Σ coupling effect in $^{10}_{\Lambda}\text{Li}$ hypernucleus

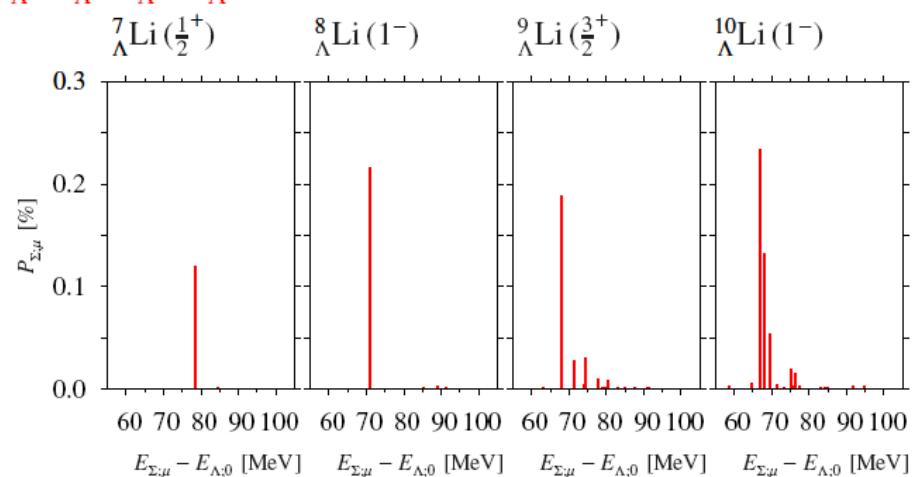
microscopic shell model

Σ - mixing probability

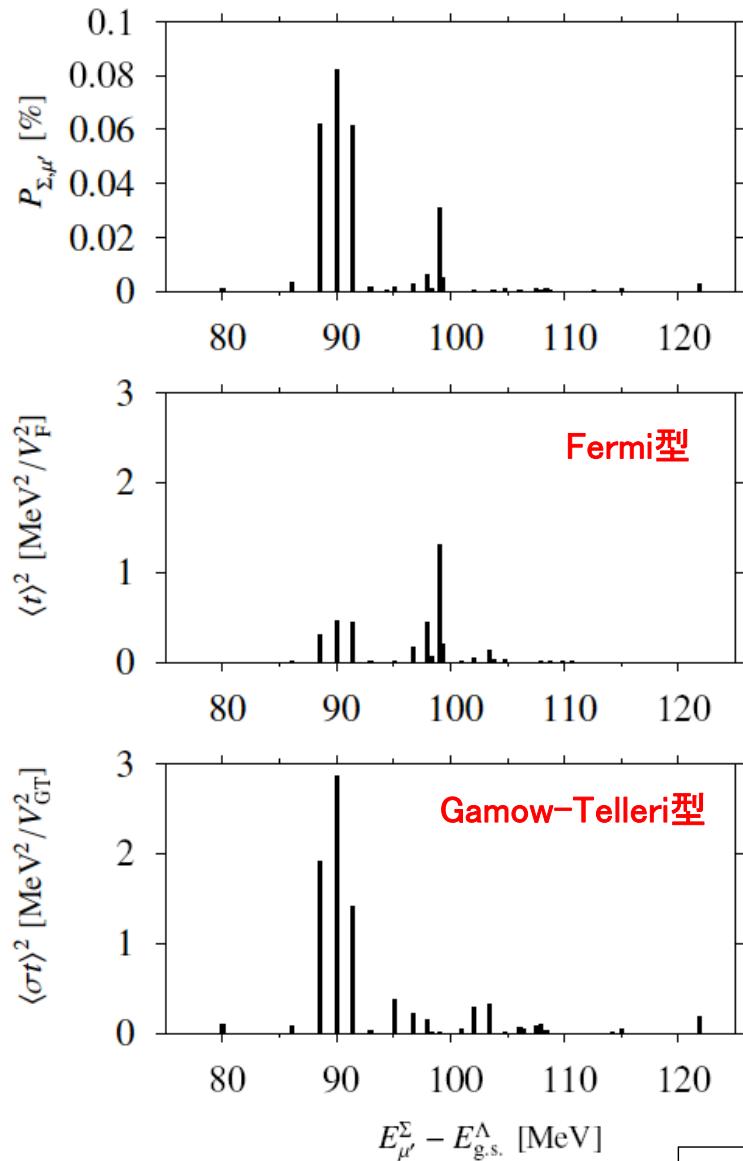
$$P(^{10}_{\Lambda}\text{Li}) = 0.48 \%, \Delta E = 0.33 \text{ MeV}$$

- (1) コヒーレントな Fermi型 and GT型結合
- (2) 中性子過剰核では $T(T+1)$ に比例
- (3) $^7_{\Lambda}\text{Li}$ に比較して 5 倍大きい

$^7_{\Lambda}\text{Li}, ^8_{\Lambda}\text{Li}, ^9_{\Lambda}\text{Li}, ^{10}_{\Lambda}\text{Li}$ の基底状態における Λ - Σ 結合強度

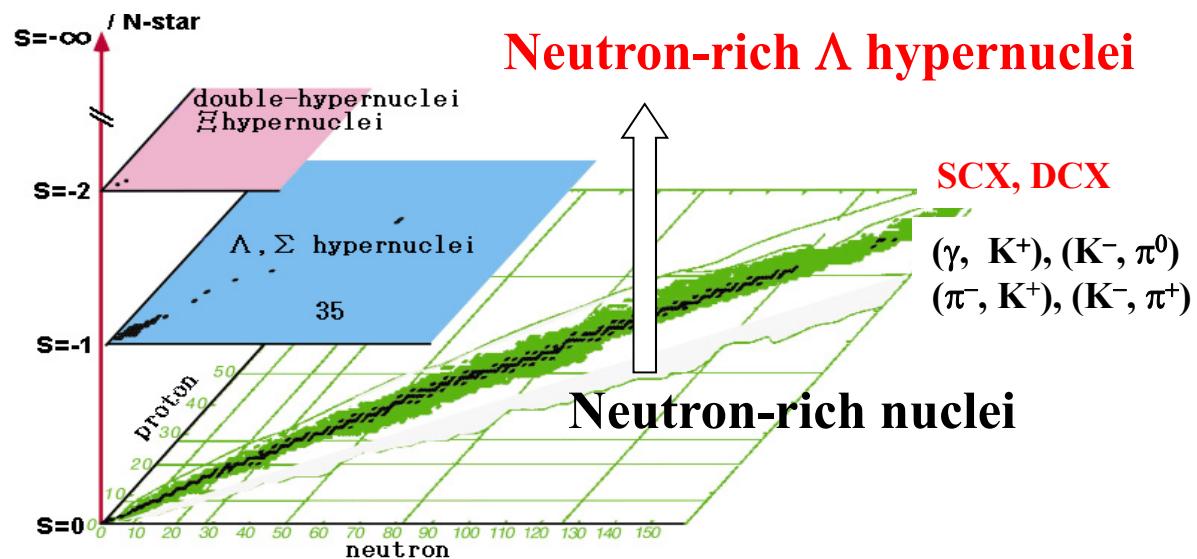


Umeya, Harada, PRC79(2009)024315



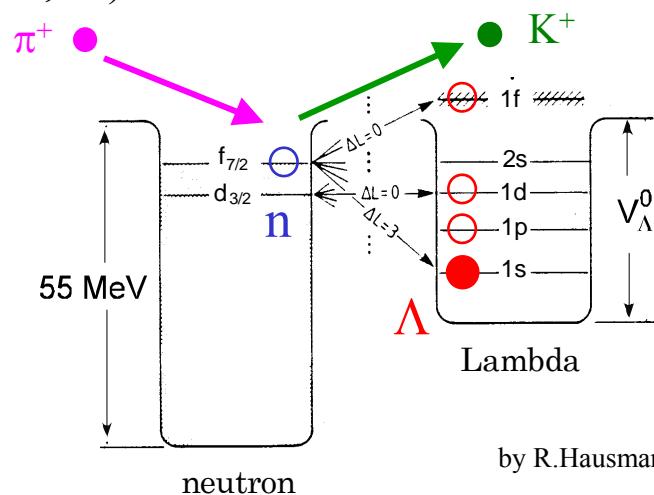
中性子過剰 Λ ハイパー核の生成

E10@J-PARC



Hypernuclear Production Reactions

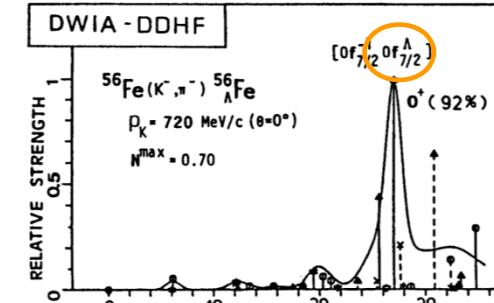
(π^+, K^+) reaction



Theoretical calculations

^{56}Fe target

H.Bando, T.Motoba, J.Zofka, Int.J.Mod.Phys. A5(1990)4021



(K^-, π^-)
720 MeV/c

$q_\Lambda \sim 60-100 \text{ MeV}/c$
“Substitutional”

$\Delta\ell = 0$

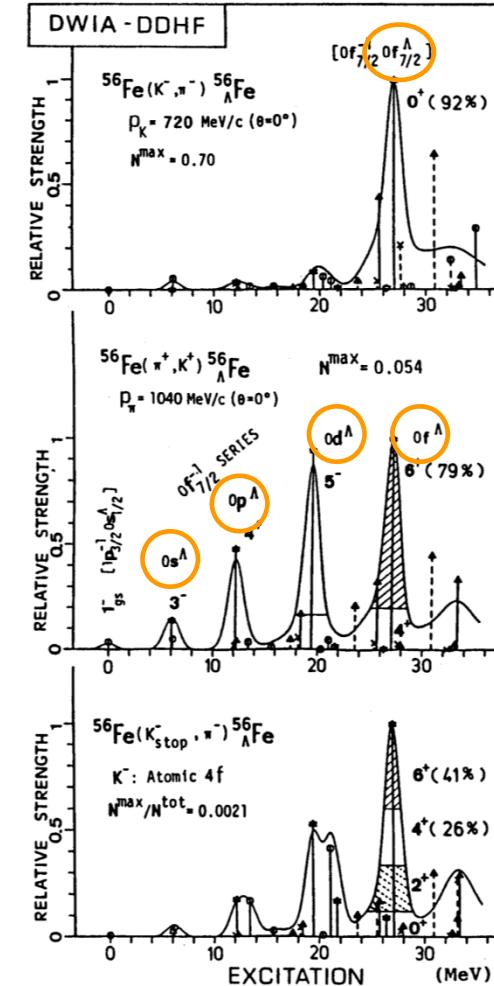
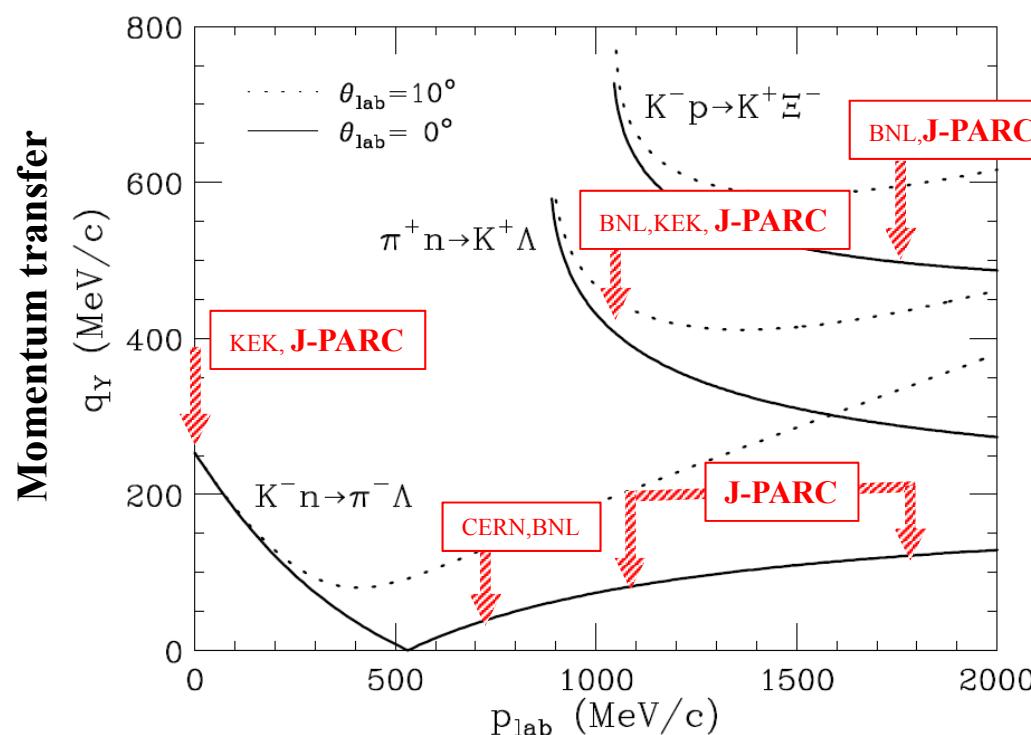
(π^+, K^+)
1040 MeV/c

$q_\Lambda \sim 400 \text{ MeV}/c$
“Spin-Stretched”

$[(nlj)_N^{-1}(nlj)_\Lambda]_J$
 $[j_{N <}^{-1} j_{\Lambda >}]_{J=J_{\max}}$

(K^-, π^-)
Stooped K-

$q_\Lambda \sim 280 \text{ MeV}/c$



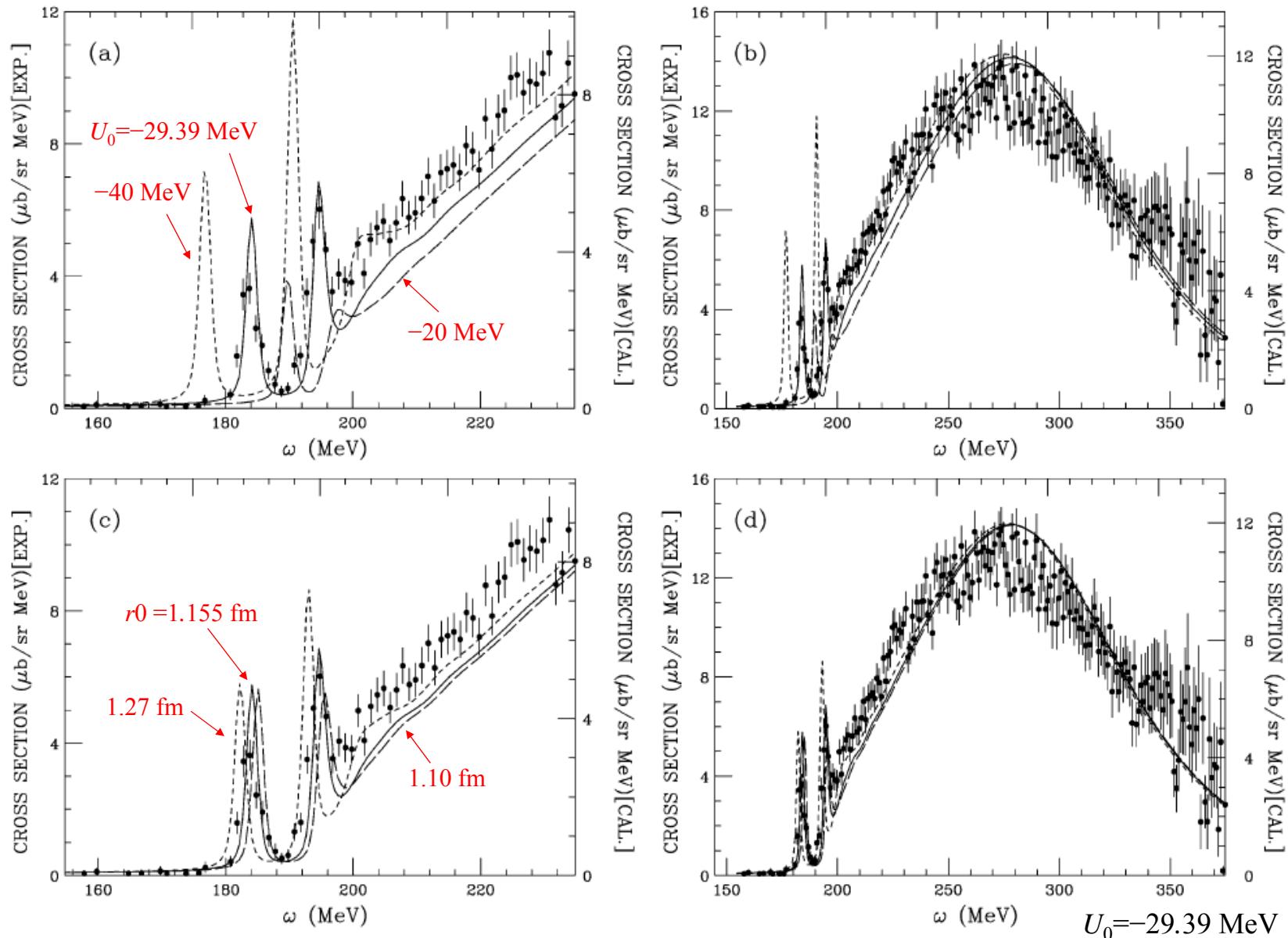
^{12}C

Λ spectrum by (π^+, K^+) reaction at 1.2 GeV/c (6°)

Harada, Hirabayashi, NPA744 (2004) 323.

Sensitivity of the spectrum to the Λ -nucleus potential parameters

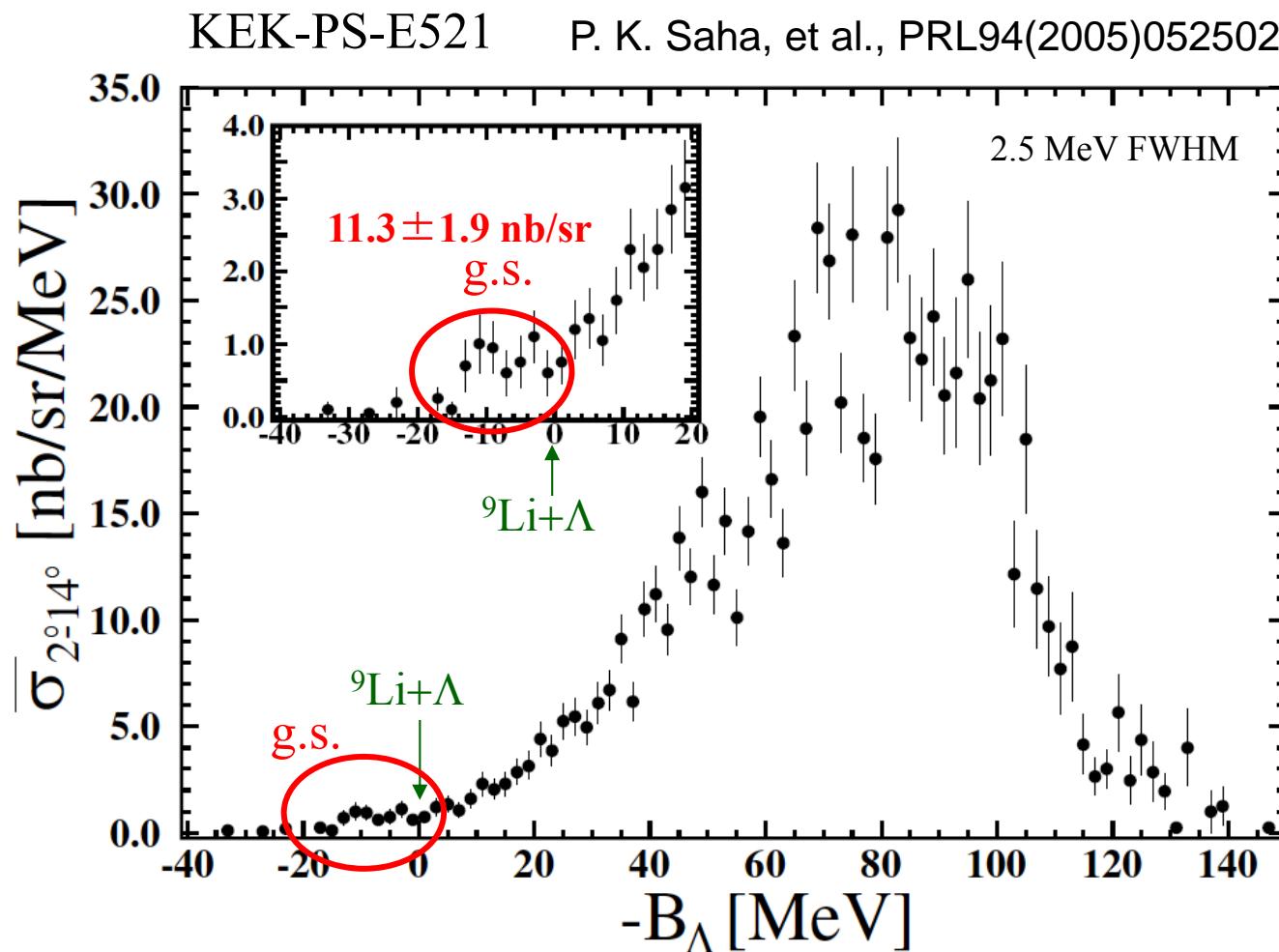
$r_0 = 1.155 \text{ fm}$



First production of neutron-rich Λ hypernuclei



Λ spectrum by DCX (π^- , K^+) reaction at 1.2GeV/c



Cross sections

- $p_\pi = 1.20 \text{ GeV}/c$

$$\frac{d\sigma}{d\Omega_\Lambda} \approx 11.3 \pm 1.9 \text{ nb/sr}$$

- $p_\pi = 1.05 \text{ GeV}/c$

$$\frac{d\sigma}{d\Omega_\Lambda} \approx 5.8 \pm 2.2 \text{ nb/sr}$$

$\sim 1/1000$

${}^{12}\text{C}(\pi^+, K^+) {}_{\Lambda}^{12}\text{C}$ (1.2 GeV/c)

$$17.5 \pm 0.6 \mu\text{b/sr}$$

$(\pi^-, K^+) - \text{Double Charge Exchange (DCX) Reaction}$

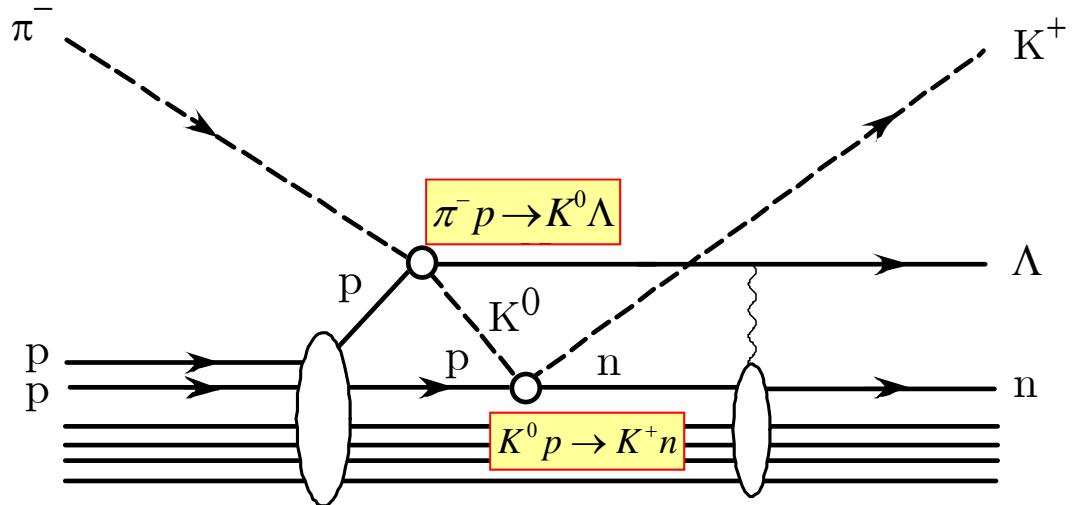
Two-step process:

$$\pi^- p \rightarrow K^0 \Lambda$$

$$K^0 p \rightarrow K^+ n$$

$$\pi^- p \rightarrow \pi^0 n$$

$$\pi^0 p \rightarrow K^+ \Lambda$$

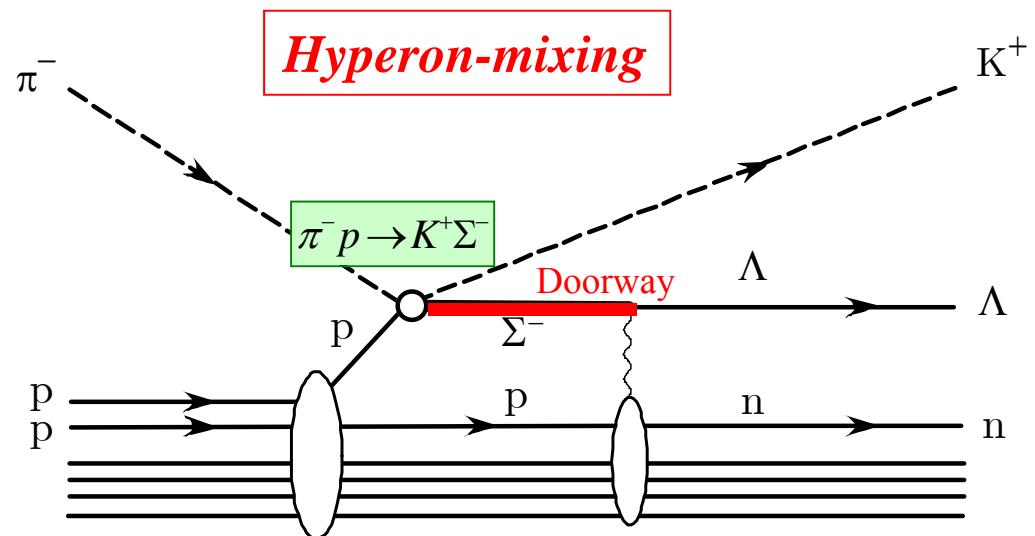


One-step process:

$$\pi^- p \rightarrow K^+ \Sigma^-$$

$$\Sigma^- p \leftrightarrow \Lambda n$$

via Σ^- doorways caused by $\Lambda N - \Sigma N$ coupling

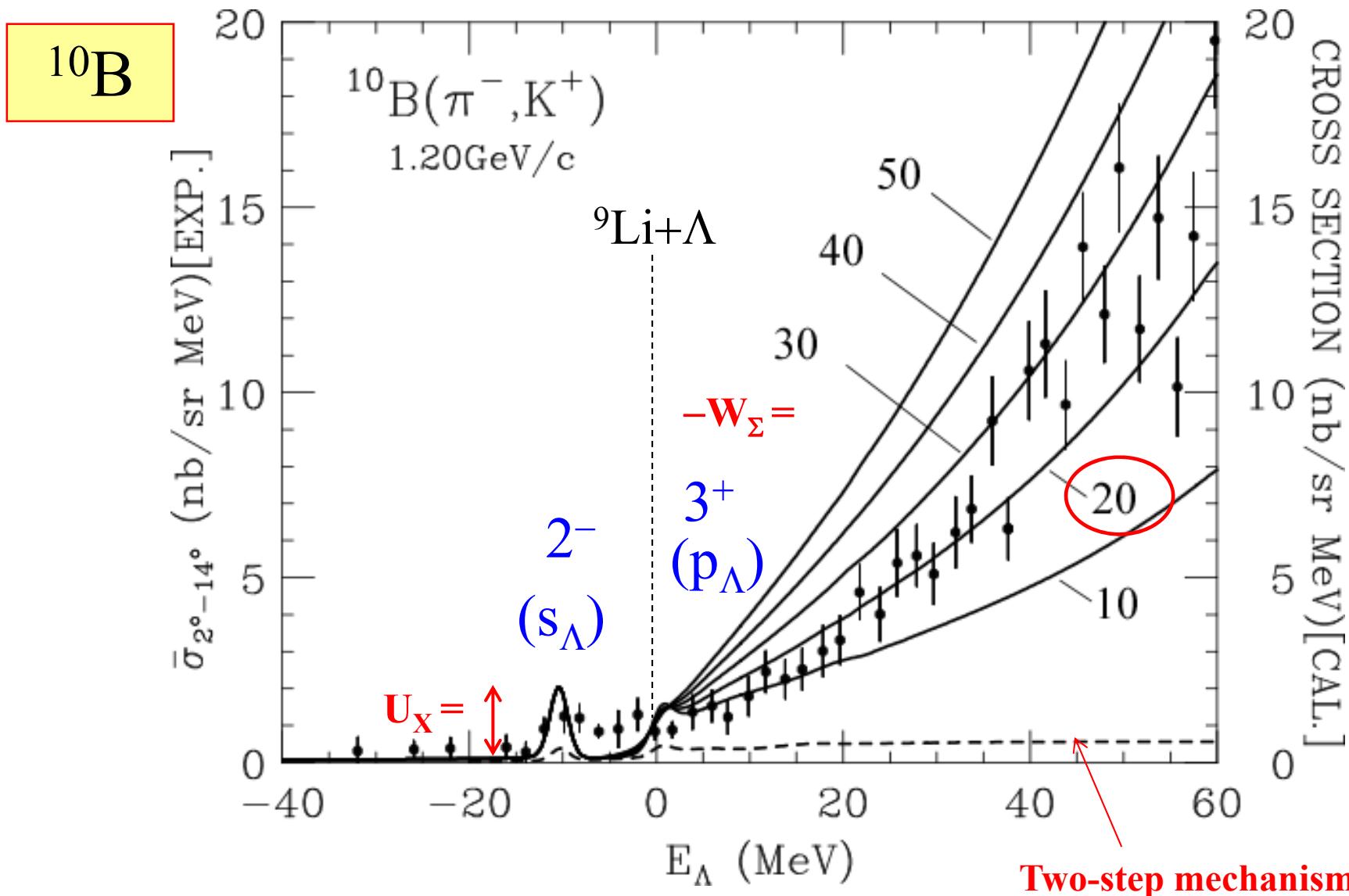


Λ spectrum by DCX (π^- , K^+) reactions at 1.2GeV/c

Harada, Umeya,Hirabayashi, PRC79(2009)014603

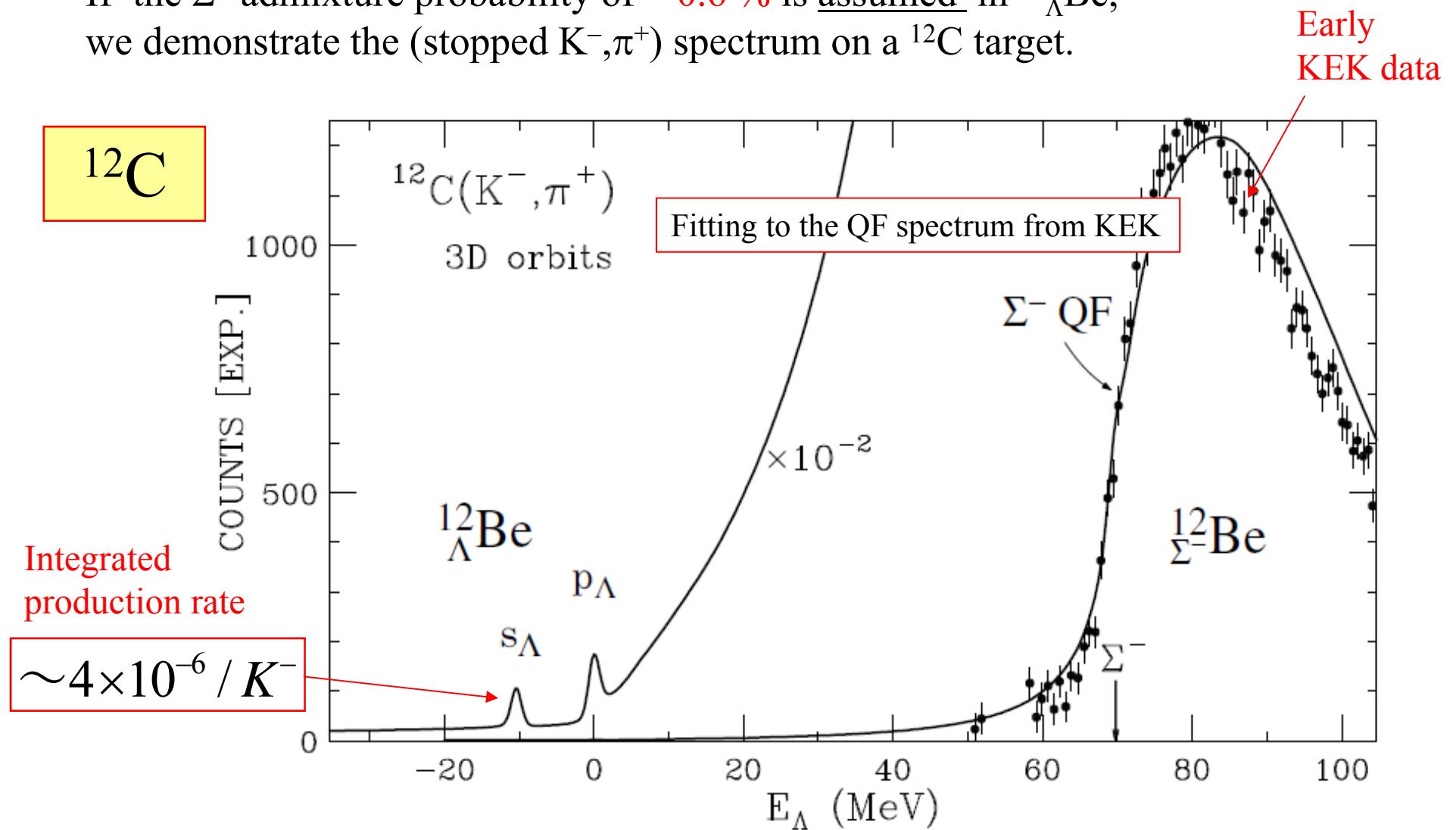
Spreading potential dep. W_Σ

$U_X = 11$ MeV is fixed. $P_{\Sigma^-} = 0.57\%$



Λ spectrum by DCX (stopped K^- , π^+) reactions

If the Σ^- admixture probability of $\sim 0.6\%$ is assumed in $^{12}\Lambda\text{Be}$,
we demonstrate the (stopped K^- , π^+) spectrum on a ^{12}C target.



DAΦNE data: $UL \square (2.0 \pm 0.4) \times 10^{-5} / K^-$

M.Agnello, et al., PLB640(2006)145.

4. まとめ

核物質中の Σ ハイペロン

- ΣN 3S_1 [10*]: Strangeness partner of deuteron
- Repulsive core: Quark Pauli forbidden states [51]
- ANN three-body force: ΛN - ΣN coherent coupling
- Production of neutron-rich Λ hypernuclei: Σ doorways
- Magnetic moments
-

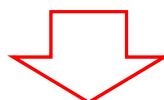
■ Keywords

Hyperon mixing + DCX

Conclusion

Studies of
the production and spectroscopy of
strangeness nuclei are
very interesting and exciting
at J-PARC.

- ストレンジネスが拓く新しい状態の発見、”エキゾチック”な原子核
- バリオン-バリオン間相互作用の理解、短距離斥力の起源
- ハイペロン混合と中性子星の2大問題



中性子星物質の状態方程式の解明

Thank you very much.